

THE SCIENCE OF COMPLEXITY

By

Aibanjali Venkatesan

INTRODUCTION

REDUCTIONISM - UNDERSTANDING THE PARTS HELP UNDERSTAND THE WHOLE - HAS HELPED SCIENCE FLOURISH SINCE THE DAYS OF DESCARTES AND GALILEO.

ALONG COMES ANOTHER IDEA THAT SOMETIMES UNDERSTANDING THE PARTS DO NOT HELP IN WORKING OUT THE WHOLE.

FOR EXAMPLE: THE WATER THAT MAKES THE WEATHER, THE CELLS THAT JOIN UP TO CREATE LIFE FORMS OR THE SHOPS THAT BUILD THE ECONOMY.

THIS IS COMPLEXITY, A NEW SCIENCE THAT HAS THE AUDACITY TO BRING SNOWFLAKES, PENDULUMS AND VIRUSES INTO THE SAME CONVERSATION.

WE STEP THROUGH THE LANDMARKS THAT HAVE BUILT THE SCIENCE AND THE PROBLEMS IT SEEKS TO TACKLE, KNOWING THAT THERE ARE SOME THINGS THAT CAN NEVER BE PRECISELY MEASURED OR PREDICTED.

SCOPE

COMPLEX SYSTEMS

- CONTEXT & INTRODUCTION
- DEFINITION & EXAMPLES
- QUESTIONS ADDRESSED
- FEATURES

THE SCIENCE

- THE GOAL
- CORE DISCIPLINES

DYNAMICS

- COMPLEX BEHAVIOURS
- ITERATION
- NON LINEARITY
- FRACTALS
- BUTTERFLY EFFECT
- CHAOS

INFORMATION

- DEFINITION
- MAXWELL'S DEMON
- ENTROPY
- SHANNON INFORMATION

COMPUTATION

- IDEAS IN COMPUTATION
- WHAT NATURE DOES
- PROCESSING INFORMATION

EVOLUTION

- A HISTORY
- GENETIC ALGORITHM
- EXAMPLE

SIMULATING COMPLEX SYSTEMS

CELLULAR AUTOMATA

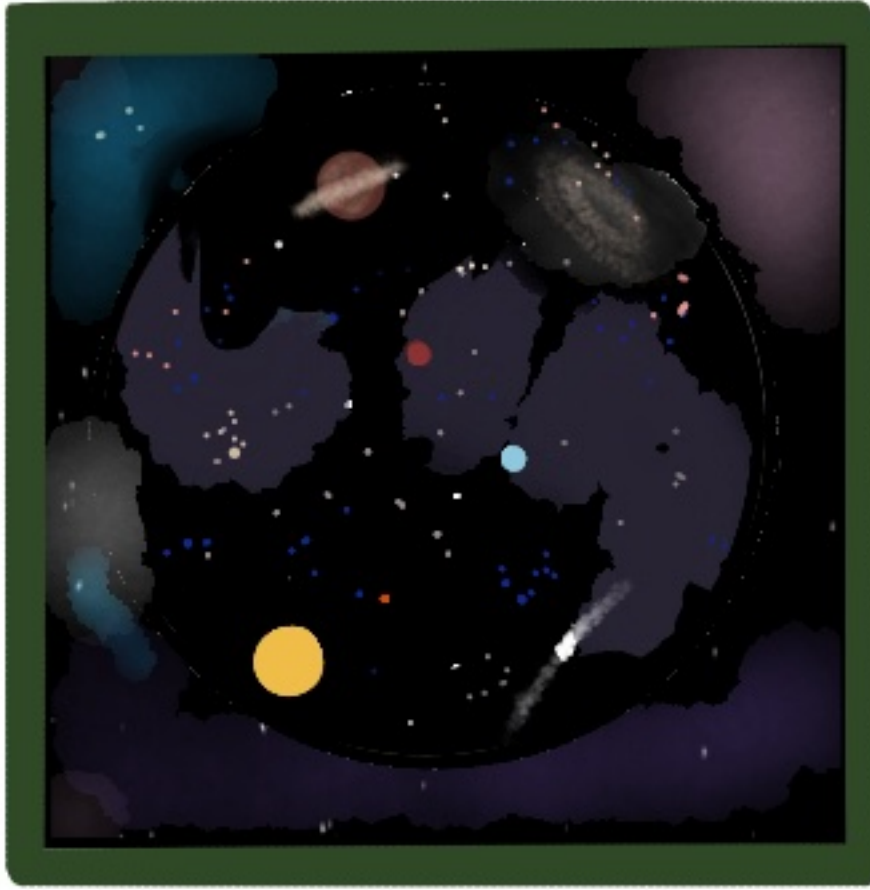
- ONE & TWO DIMENSIONS
- STEPHEN WOLFRAM
- IDEAL COMPLEX SYSTEMS
- GAME OF LIFE
- LEGACY & USES OF CA

A BRIEF OUTLOOK

MORE TO EXPLORE

REFERENCES

THE PLACE TO START



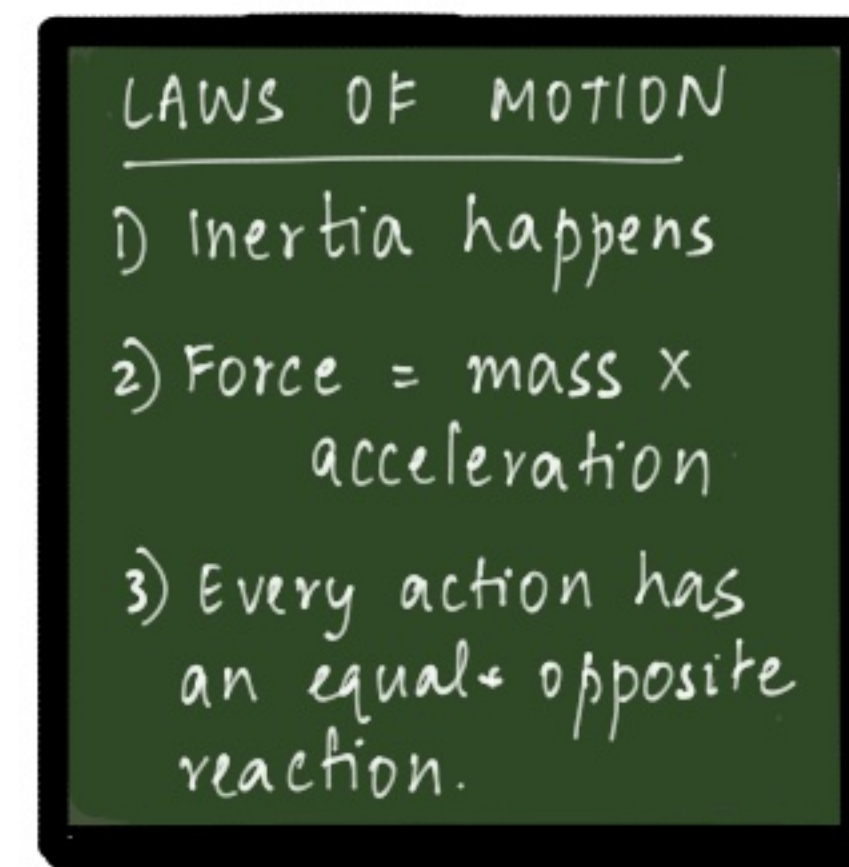
THE UNIVERSE

IS
A
COMPLEX PLACE



ISAAC NEWTON

WAS ONE AMONG
MANY WHO HELPED
MAKE SENSE OF IT.



velocity
 $v = u + at$
 $v^2 = u^2 + 2as$
force = ma
acceleration
displacement
 $s = \frac{u+v}{2}t$
 $s = ut + \frac{1}{2}at^2$
 $s = vt - \frac{1}{2}at^2$
 $F = \frac{GMm}{r^2}$

HIS EQUATIONS

PERFECTLY DESCRIBE
MOVEMENT ON EARTH
AND IN THE SKIES

THIS DETERMINISM WAS SO APPEALING THAT PHYSICIST PIERRE-SIMON
LA PLACE IS THOUGHT TO HAVE DESCRIBED AN ALL-KNOWING DEMON :

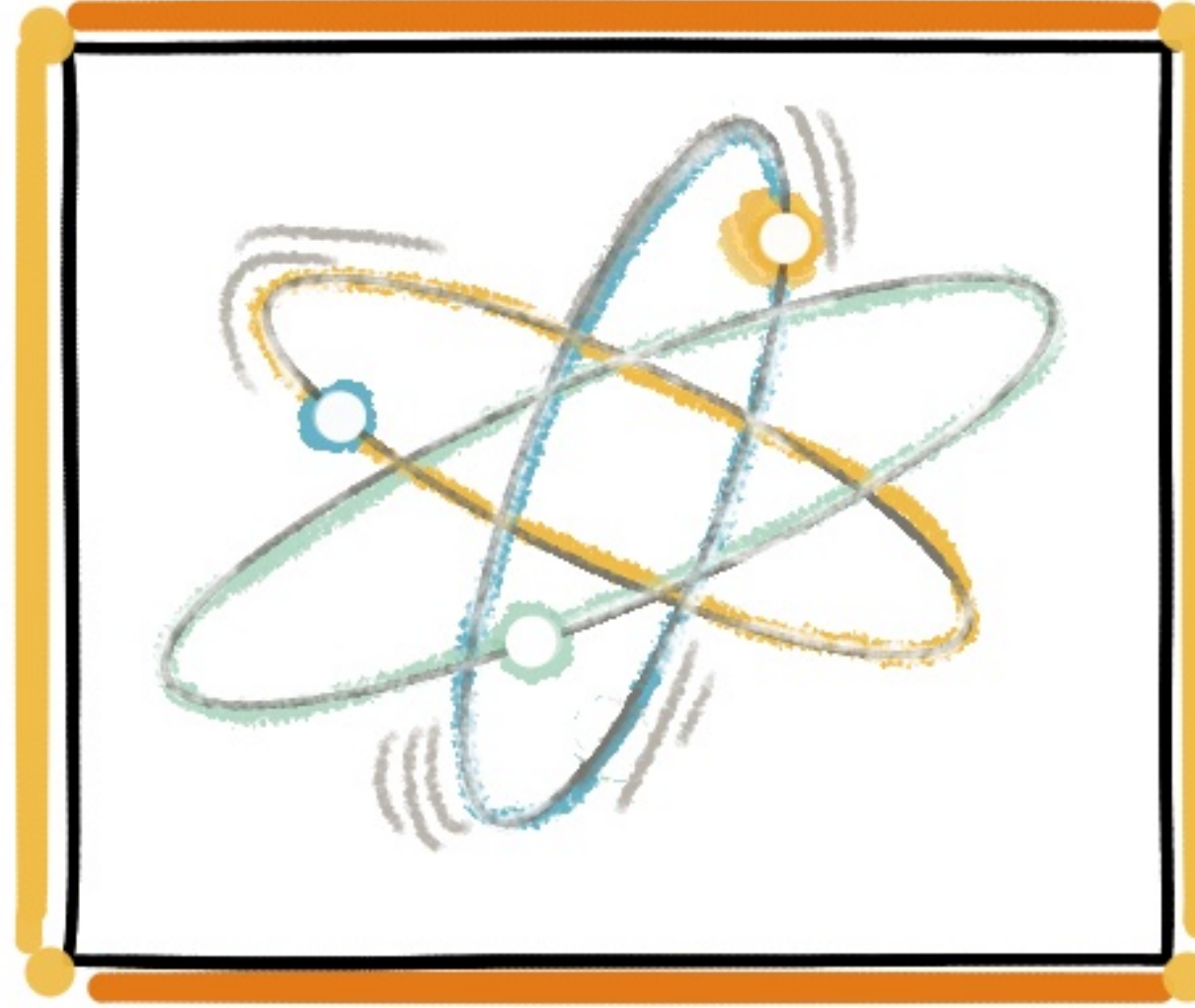
"An intellect which at any given moment knew all
of the **forces** that animate nature and **positions** of
the beings for such an intellect, nothing
could be **uncertain** and **future** just like **past** would
be **present** before its eyes."

EXCEPT...

NOT EVERYTHING IN THE UNIVERSE CAN BE EXPLAINED THIS WAY.

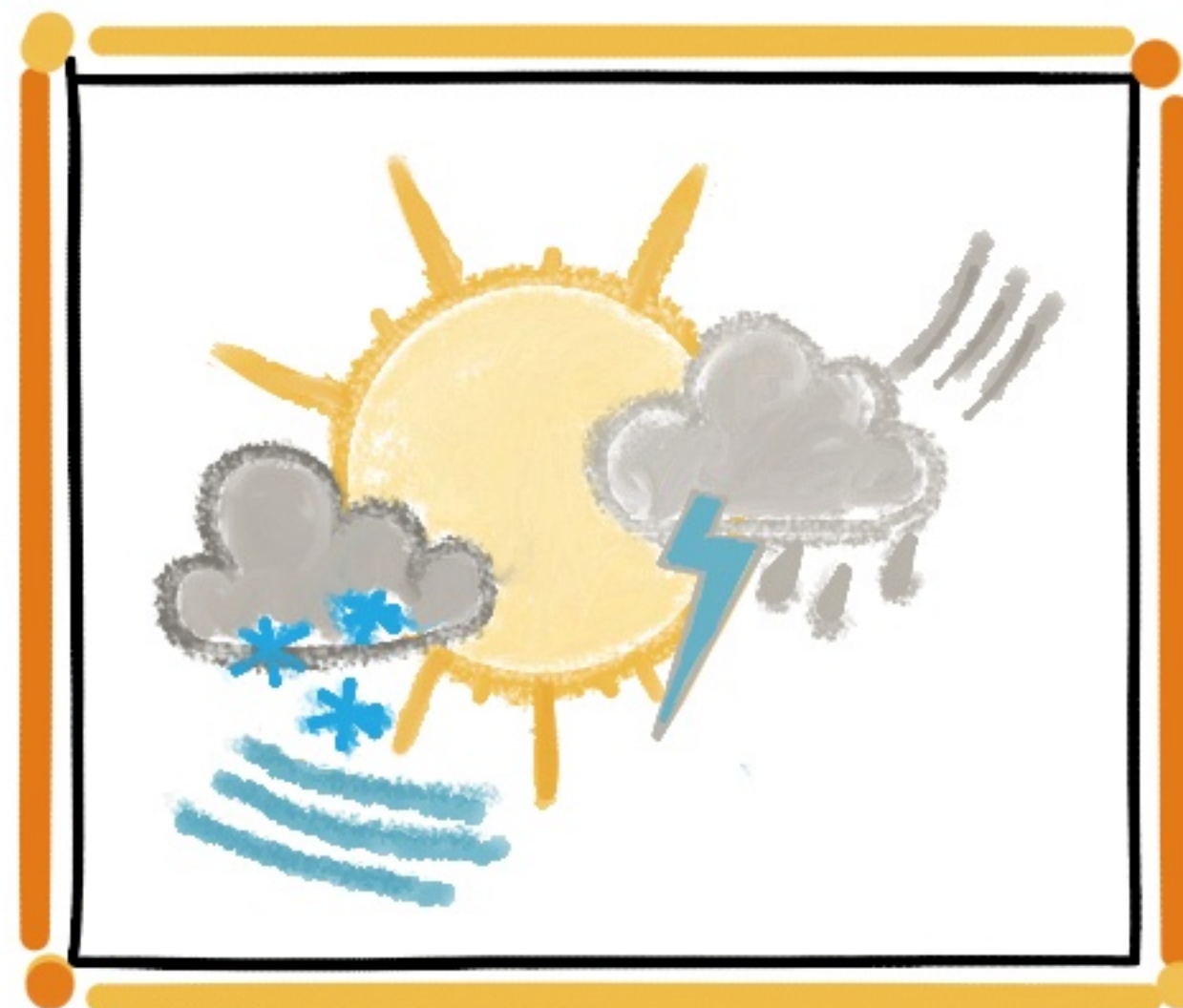
FOR EXAMPLE:

QUANTUM MECHANICS



THE SUBATOMIC WORLD DEFIES IDEAS OF CERTAINTY AND MEASUREMENT
UNLIKE CLASSICAL PHYSICS

PREDICTING THE WEATHER



THE NOTION OF CHAOS WHERE APPROXIMATE MEASUREMENTS DO NOT PREDICT
APPROXIMATE, BUT WILDLY DIFFERENT OUTCOMES.

UNDERSTANDING NATURAL PHENOMENON LIKE THE WEATHER, SWARM
BEHAVIOUR OF CREATURES LIKE ANTS LED TO A NEW SCIENCE.
THE SCIENCE OF COMPLEXITY

THE SCIENCE

COMPLEXITY CAN BE THOUGHT OF AS ASKING THE OPPOSITE QUESTION TO REDUCTIONISM.

GIVEN THE INTERACTING PARTS
WHAT MAKES THE WHOLE WORK?

THIS QUOTE SUMS IT UP

the whole is more than
the sum of its parts



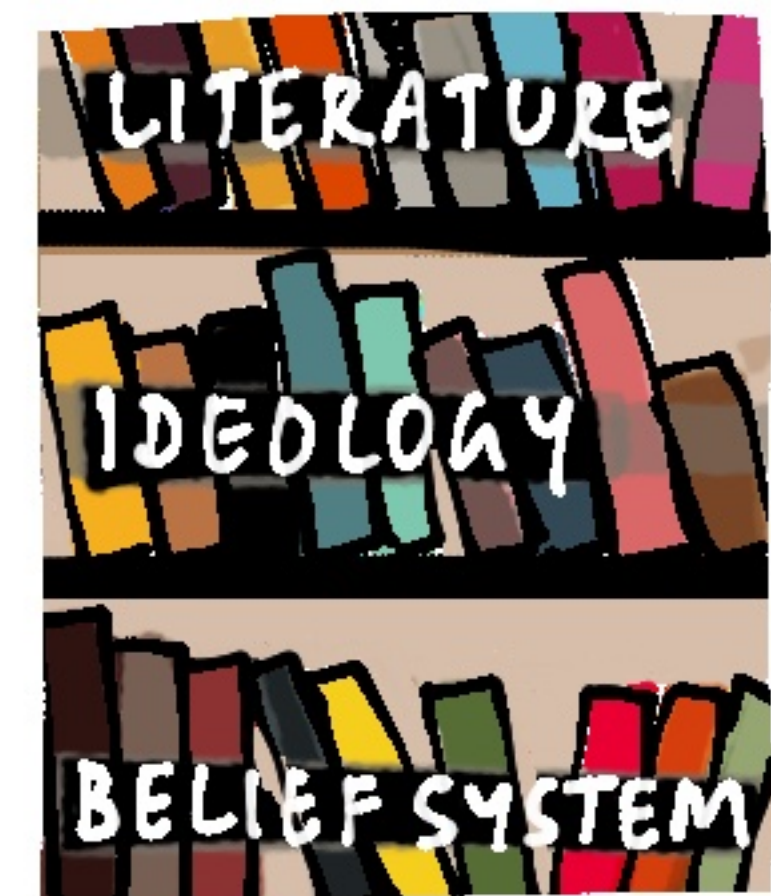
ARISTOTLE

FOR EXAMPLE

PARTS

q e w z i d
g b l n s a r
m c s o x p y j k h v

WHOLE



ALSO KNOWN AS

● COMPLEX SYSTEM SCIENCE

● PLECTICS

HAS APPLICATIONS IN

● INFORMATION THEORY

● GEOLOGY

● NEUROSCIENCE

● ECONOMICS

● BIOLOGY

THE FIELD TOOK OFF IN THE 1980s WITH THE DEVELOPMENT OF
COMPUTERS TO PROCESS NUMBERS AND WITH ENOUGH GRAPHICS TO
VISUALISE EXPERIMENTS

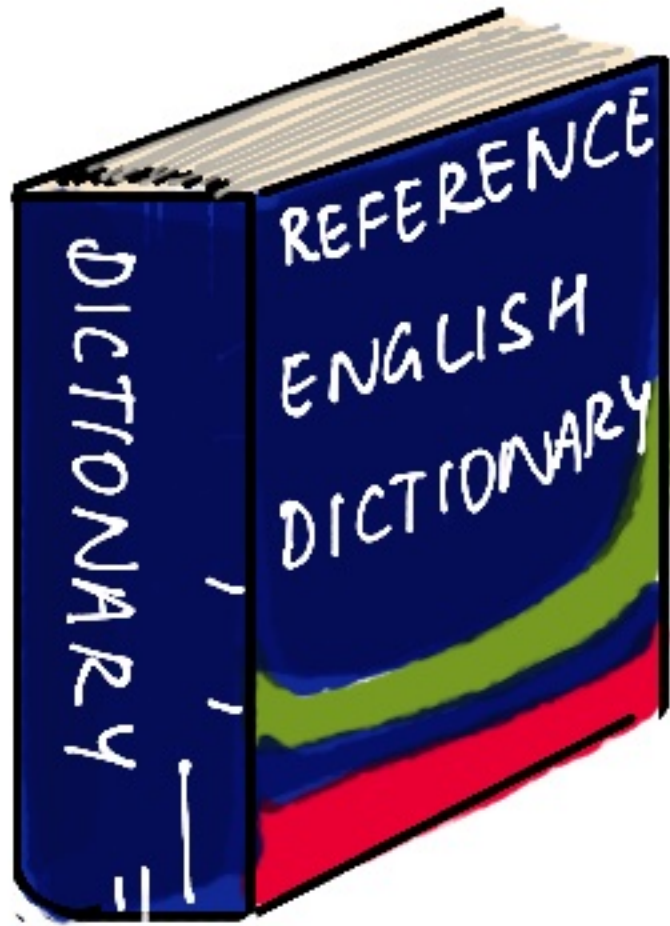
THE ESSENCE

EVERY DISCIPLINE HAS A DIFFERENT NOTION OF COMPLEXITY AND MEASURES IT DIFFERENTLY. HERE WE WILL TRY AND UNDERSTAND WHAT COMPLEXITY IS ALL ABOUT.

COMPLEXITY: DEFINITION

IT IS QUITE A DIFFICULT TASK TO DEFINE COMPLEXITY AS A SCIENCE.
COMPLEXITY TO COMPUTER SCIENTISTS IS NOT WHAT COMPLEXITY IS
TO BIOLOGISTS.

A DICTIONARY DEFINITION OF 'COMPLEXITY'



'the state of having many parts and being difficult to understand or find an answer to'

A PAPER BY SETH LLOYD LISTS THREE QUESTIONS THAT HELP TO
MEASURE COMPLEXITY OF THE SUBJECT

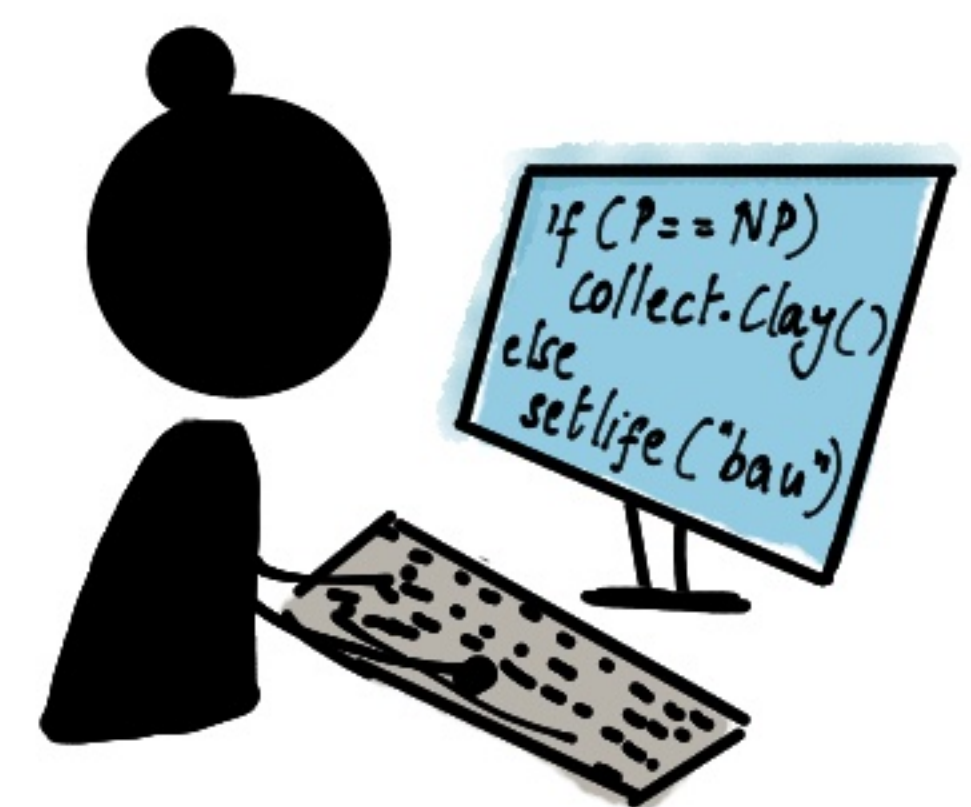
● MEASURES BASED ON HOW HARD TO DESCRIBE

- e.g. ● INFORMATION
- ENTROPY

$S = k \log W$
Boltzmann's
Entropy

● MEASURES BASED ON HOW HARD TO CREATE

- e.g. ● COMPUTATIONAL COMPLEXITY
- COST



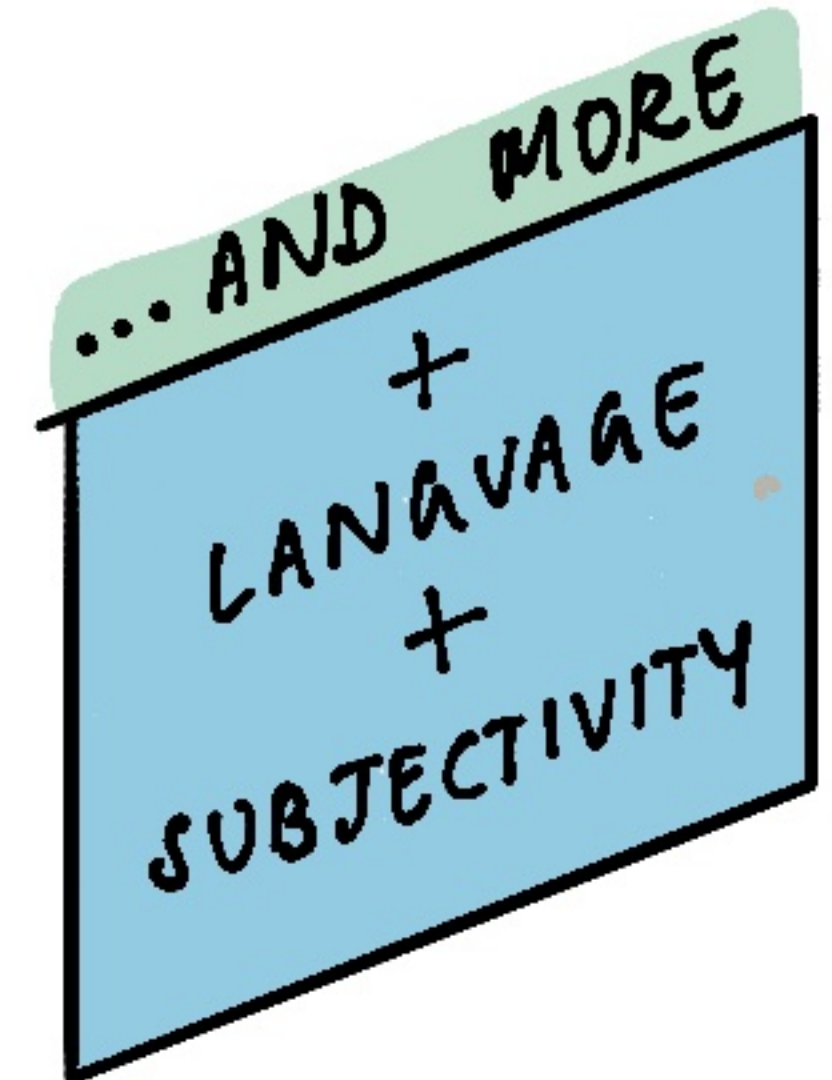
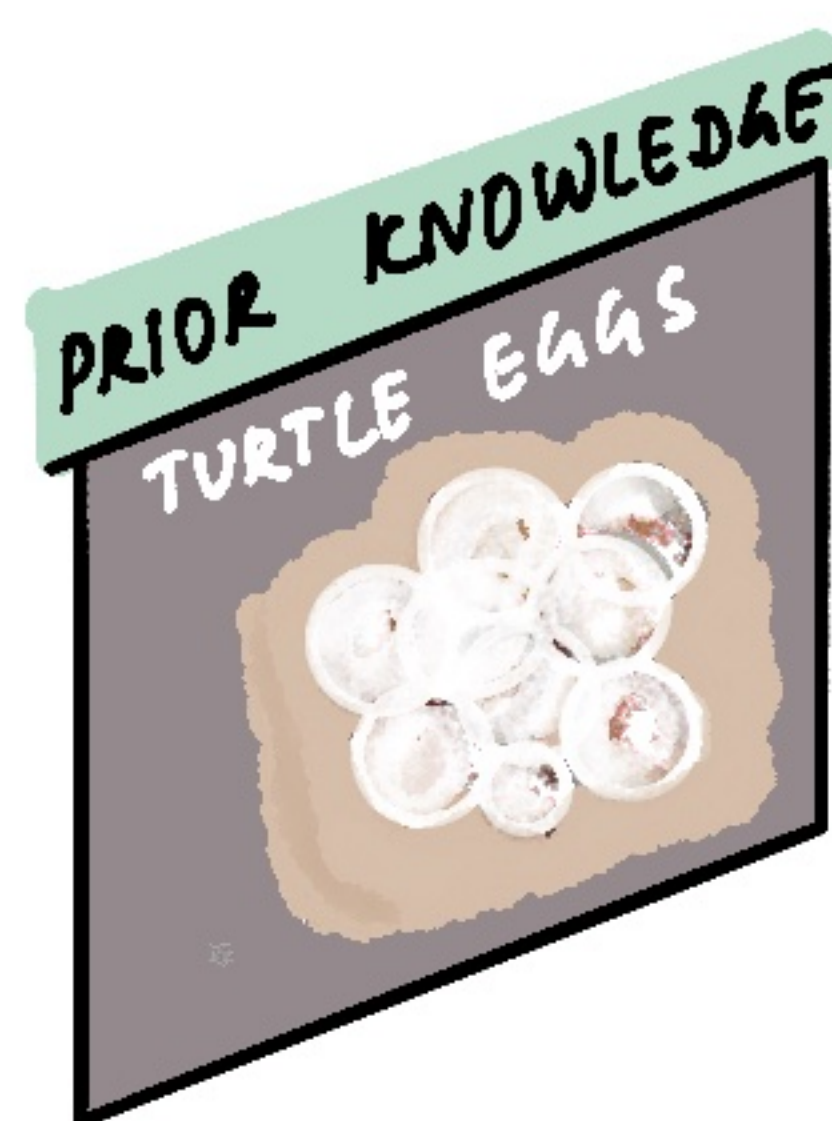
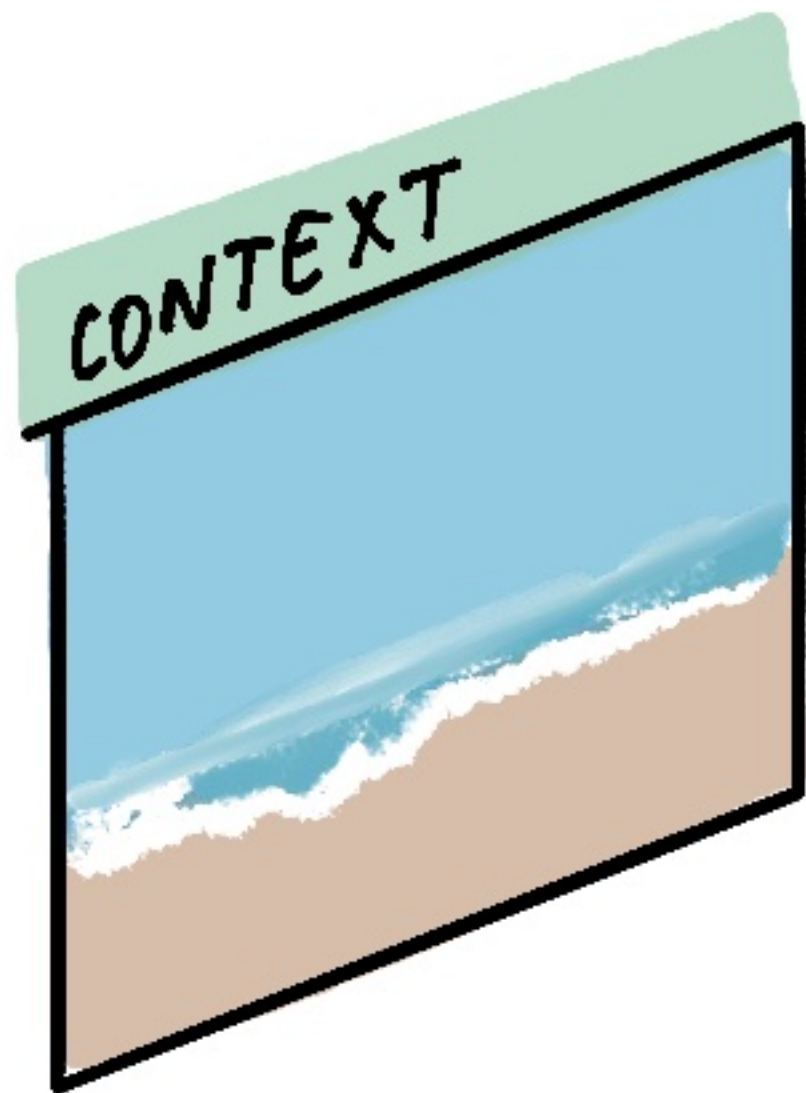
● MEASURES BASED ON DEGREE OF ORGANISATION

- e.g. ● HIERARCHICAL COMPLEXITY
- FRACTAL DIMENSION



COMPLEXITY & ORDER

ALTHOUGH VARIOUS SCIENTIFIC FIELDS MEASURE COMPLEXITY IN DIFFERENT WAYS, UNDERSTANDING THE COMPLEXITY OF THE TOPIC MAY NEED



ANOTHER MEASURE OF COMPLEXITY IS:

the length of
a concise description of
an entity's regularities



MURRAY GELL-MANN

RANDOM
no regularities

5	3	3	3	6	0	5	3	5
6	1	8	3	7	8	1	3	2
6	3	7	4	2	9	7	1	8
0	6	8	1	4	9	6	1	3

UNIFORM
fully regular

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Effective complexity → ZERO

THUS, COMPLEXITY OCCURS BETWEEN
TOTAL ORDER AND TOTAL DISORDER

COMPLEX SYSTEMS

SYSTEMS WHERE A SIZEABLE NUMBER OF FACTORS
ARE INTERRELATED INTO AN ORGANIC WHOLE

-WARREN WEAVER

THE QUESTIONS



WARREN WEAVER

THE PROBLEMS THAT CANNOT BE SOLVED EITHER

● BY MANAGING

THE RELATIONSHIPS BETWEEN
A HANDFUL OF VARIABLES

OR

● BY EMPLOYING

STATISTICAL METHODS TO COPE
WITH MILLIONS OF VARIABLES

...WEAVER DESCRIBES THESE QUESTIONS AS THE SUBJECT OF COMPLEXITY

WHY DOES SALT WATER
FAIL TO SATISFY THIRST?

DO COMPLEX PROTEIN MOLECULES KNOW
HOW TO DUPLICATE THEIR PATTERN?

IS A VIRUS
A LIVING ORGANISM?

ON WHAT DOES THE
PRICE OF WHEAT DEPEND?

WHY IS ONE CHEMICAL SUBSTANCE A POISON
WHILE ANOTHER WITH THE SAME ATOMS
REARRANGED IS COMPLETELY HARMLESS?

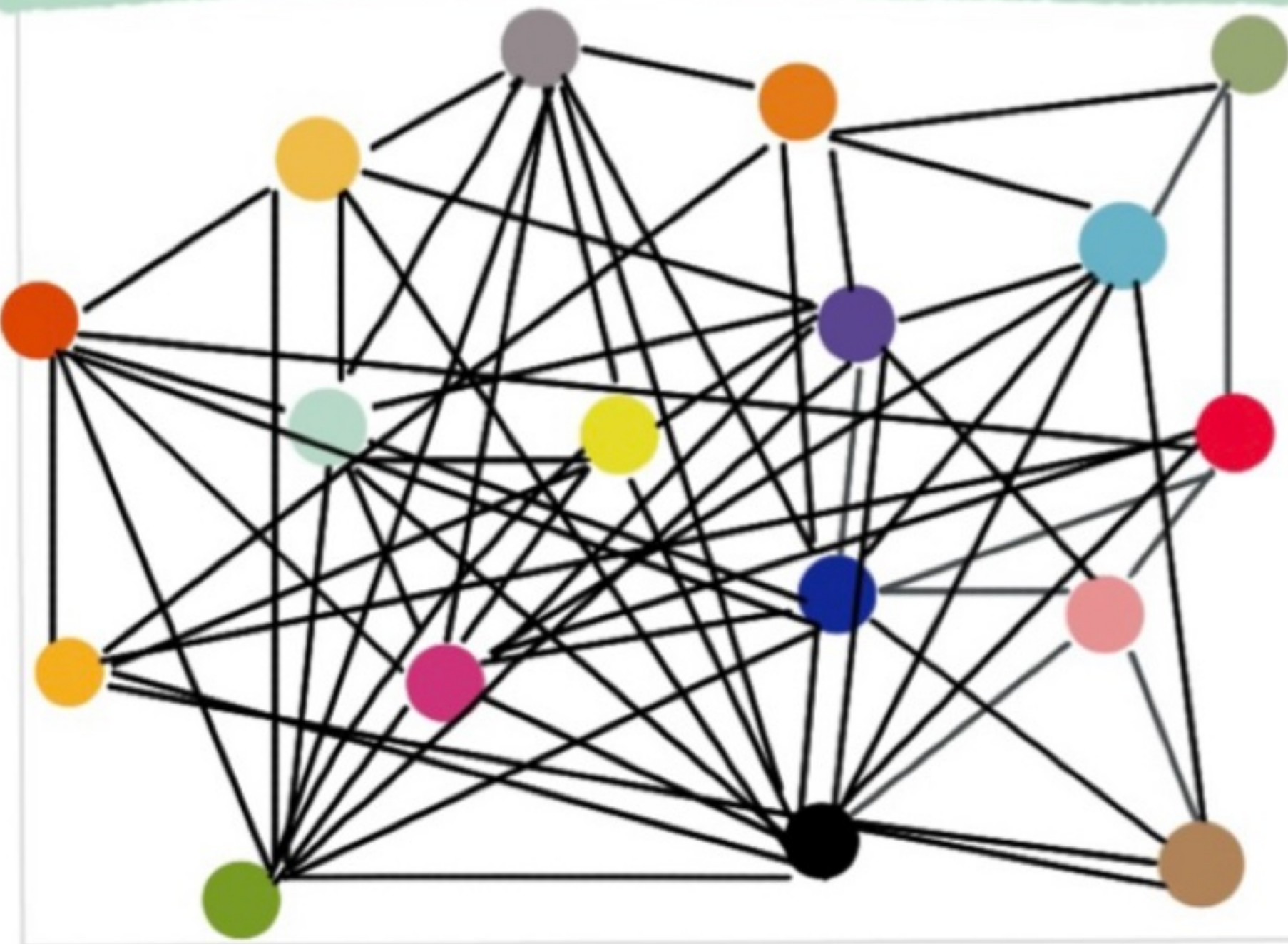
HOW CAN CURRENCY
BE STABILISED?

HOW CAN WE EXPLAIN THE BEHAVIOUR
PATTERNS OF A LABOUR UNION?

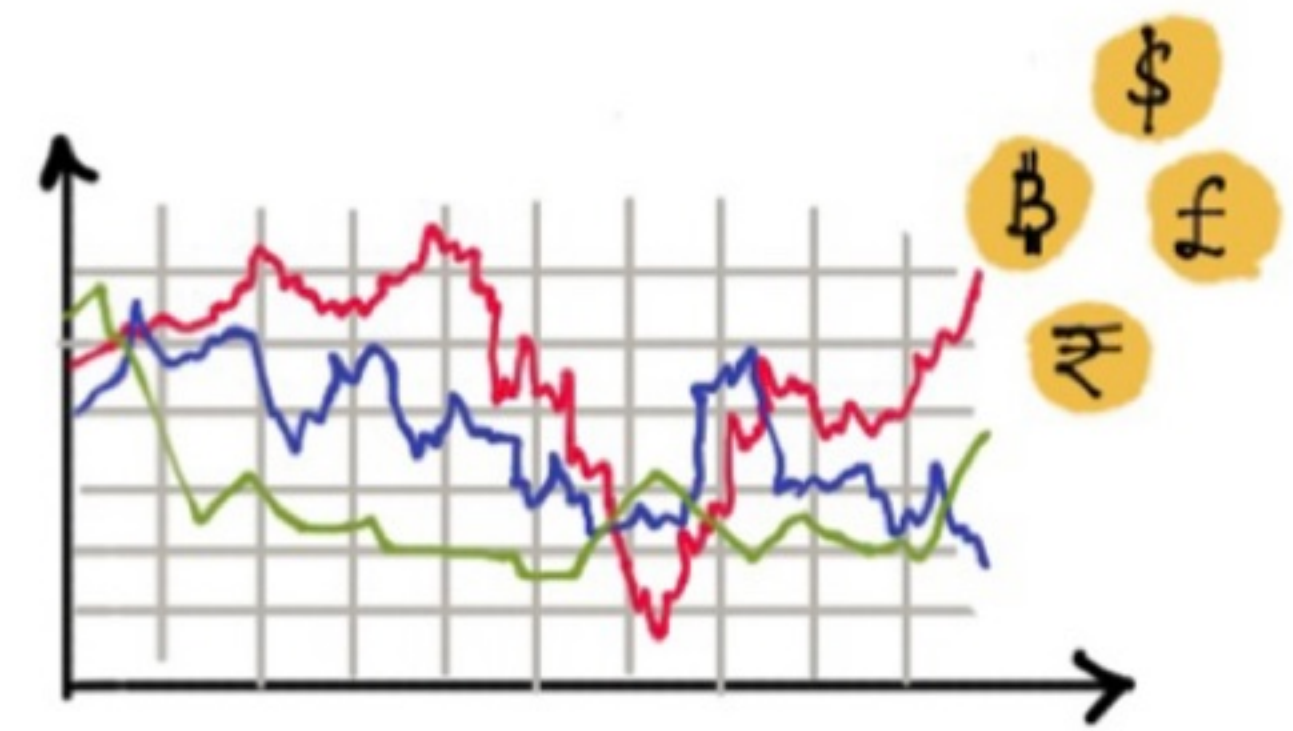
WHAT SACRIFICES OF SELFISH INTEREST
WILL MOST EFFECTIVELY CONTRIBUTE TO
A STABLE, DECENT AND PEACEFUL WORLD?

EXAMPLES OF COMPLEX SYSTEMS

SOCIAL NETWORKS



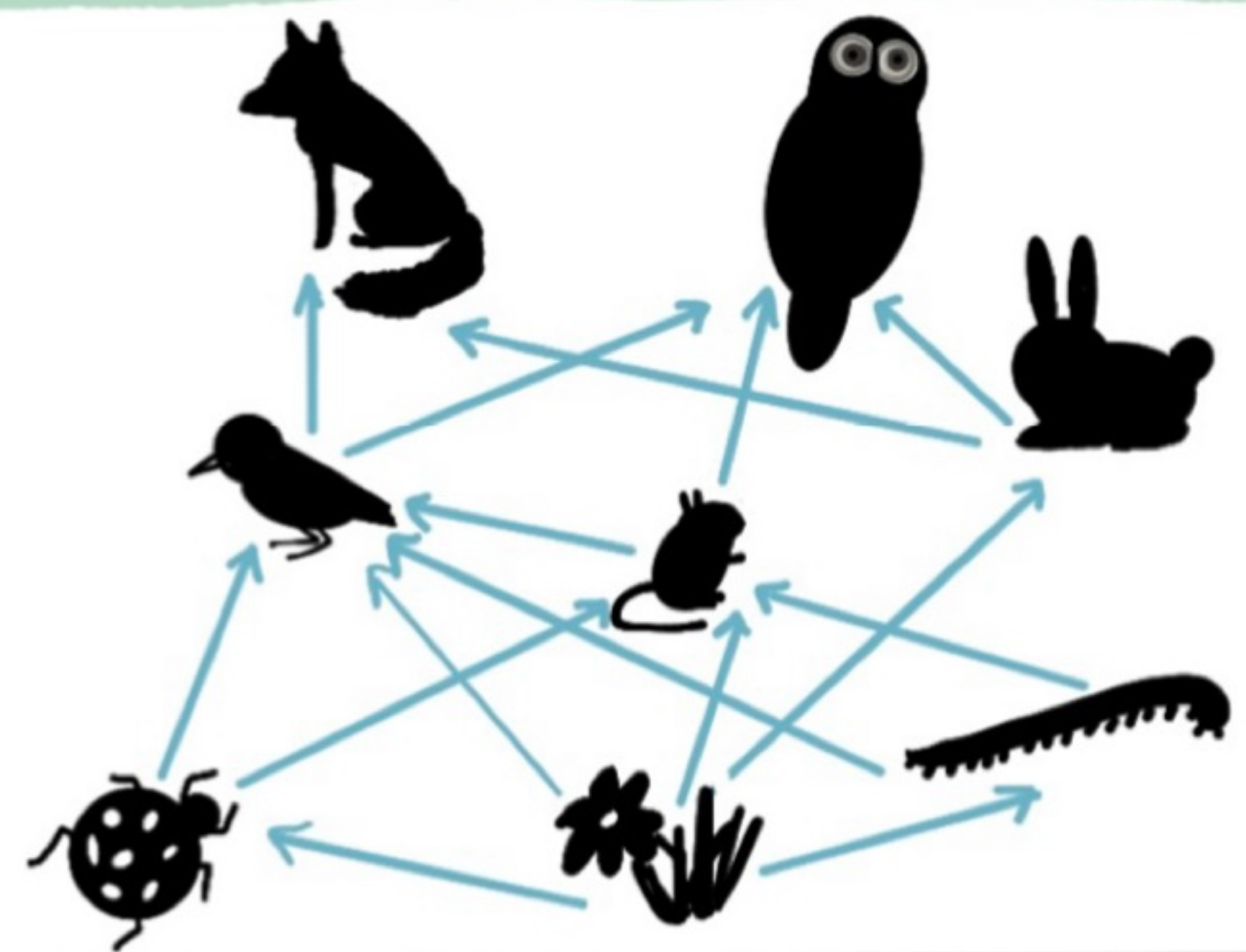
ECONOMIES



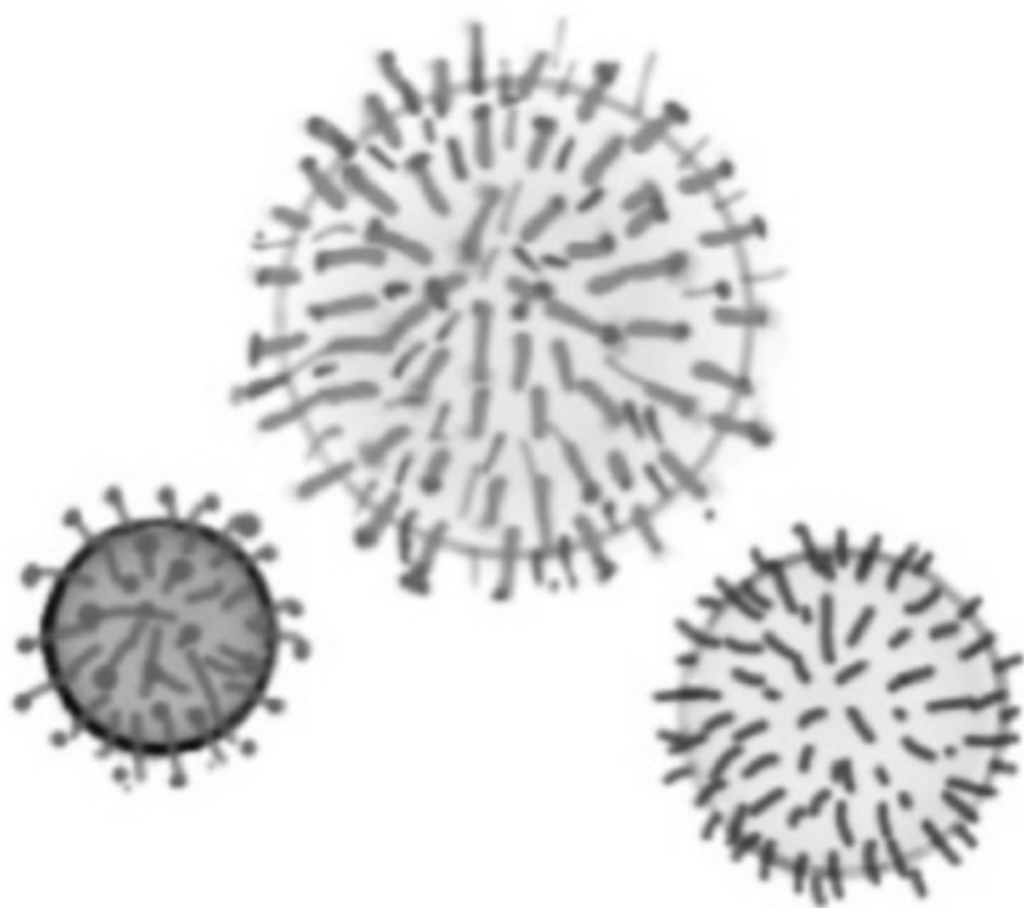
TERMITE COLONIES



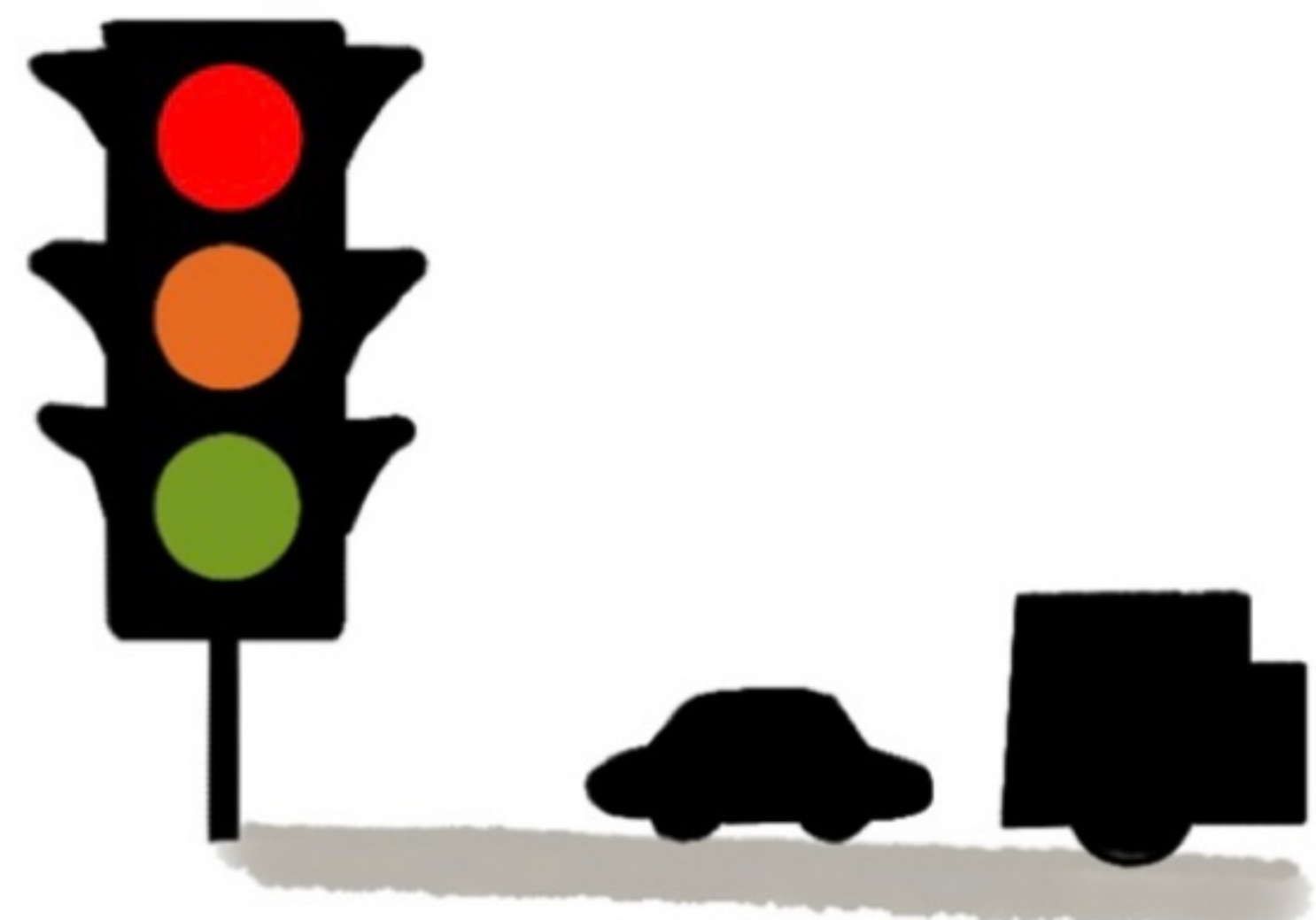
FOOD WEBS



IMMUNE SYSTEM



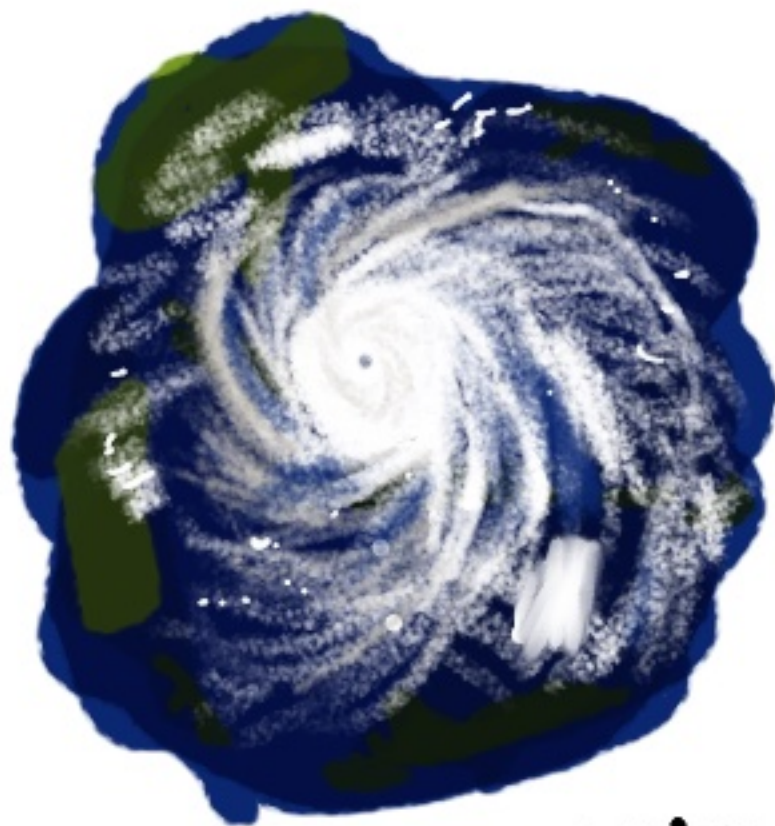
TRAFFIC



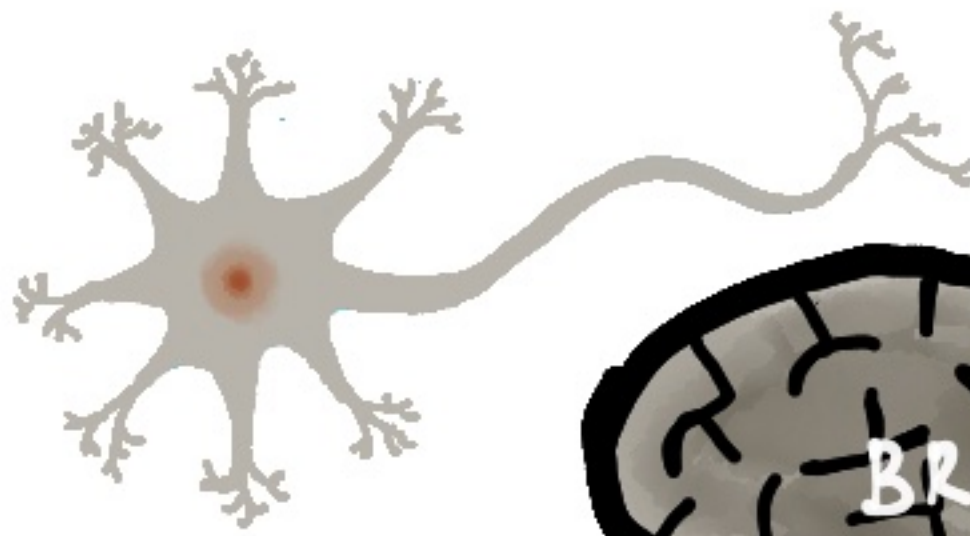
SOME COMMON FEATURES



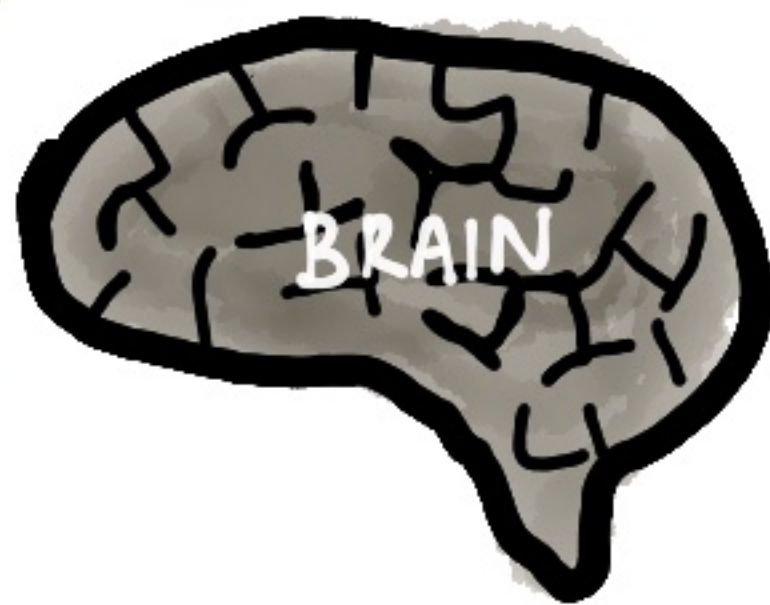
WATER



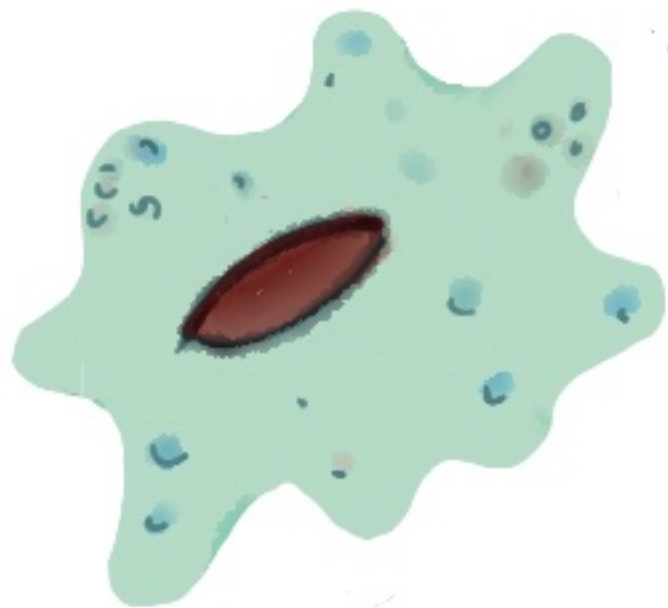
HURRICANE



NEURON



BRAIN



CELL



HIGHER LIFE FORMS



ANT



ANT COLONY

COMPLEX SYSTEMS HAVE SOME COMMON FEATURES. THEY HAVE:

SIMPLE COMPONENTS

- SIMPLER THAN THE

INTERACTIONS

- THE PARTS ARE INTERDEPENDENT AND INTERACT WITH EACH OTHER BASED ON SIMPLE RULES

NO CENTRALISED CONTROL

- THEY ARE SELF ORGANISING

EMERGENT BEHAVIOUR

- THE COLLECTIVE BEHAVIOURS ADAPT AND EVOLVE AND ARE EVEN CHAOTIC AS THE SYSTEM LEARNS FROM ITS ENVIRONMENT

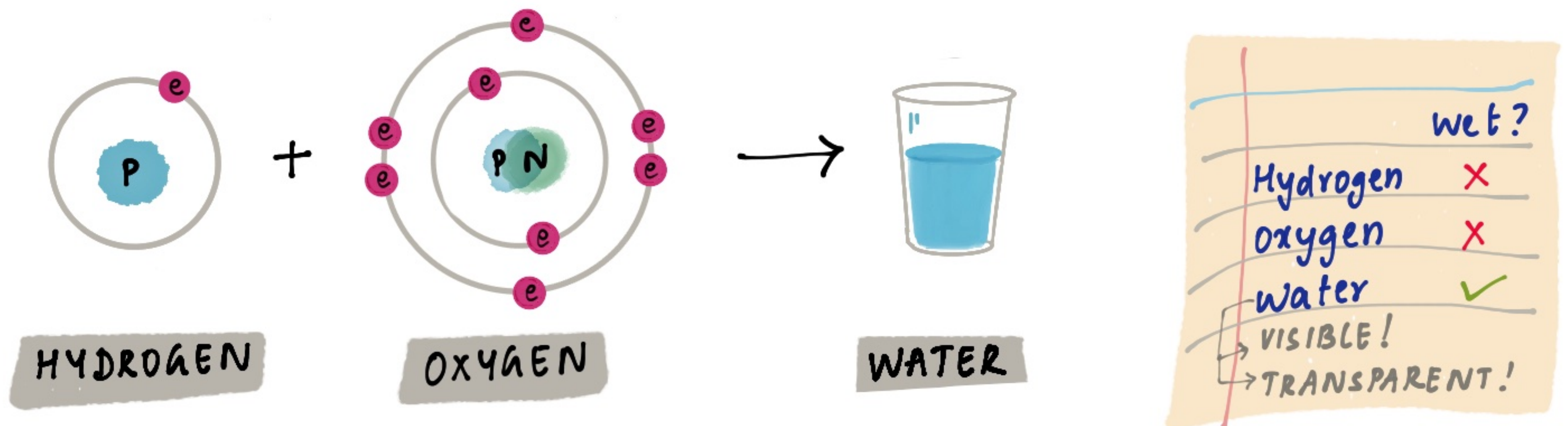
MAKING THE WHOLE GREATER THAN THE PARTS

EMERGENCE

EMERGENT BEHAVIOUR IS AN ESSENTIAL REQUIREMENT
FOR CALLING A SYSTEM COMPLEX

- JOHN HOLLAND

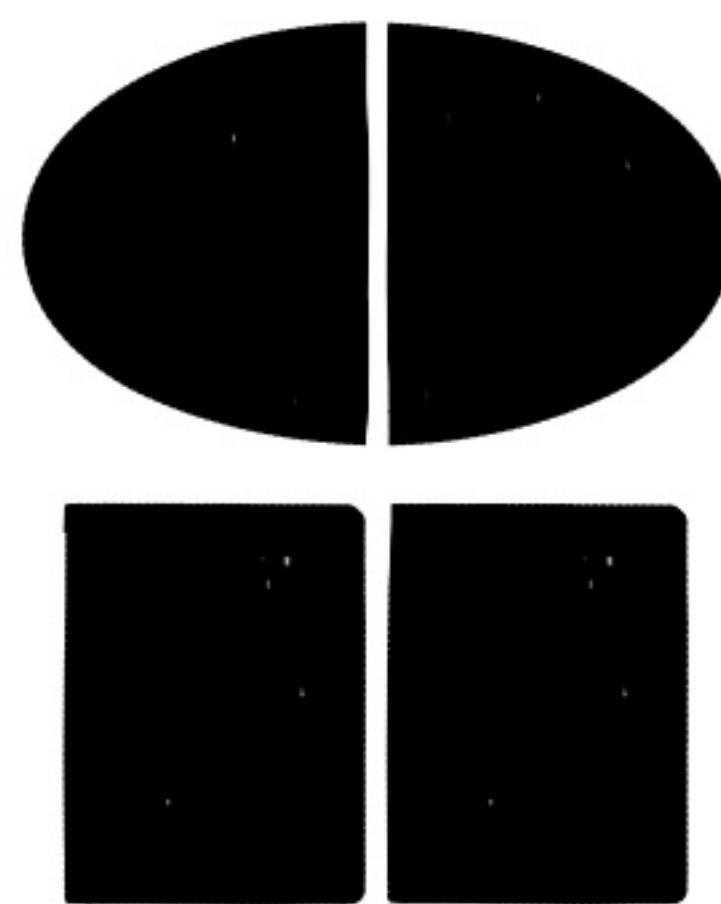
WETNESS IS A PROPERTY OF WATER - NOT ITS CONSTITUENTS
THIS EMERGENT PROPERTY SHOWS UP AT THE 'HIGHER' LEVEL.
THUS EMERGENCE AND HIERARCHY ARE CLOSELY LINKED.



EACH LEVEL HAS ITS OWN INTERESTING BEHAVIOURS, BUT IS
DRIVEN BY THE RULES OF THE PREVIOUS LEVEL.

EMERGENCE IS ALSO NOT EASILY DEFINED

Where the whole
is greater than
the parts!



EXPERTS

Not possible to
bring it down to
interaction of parts!

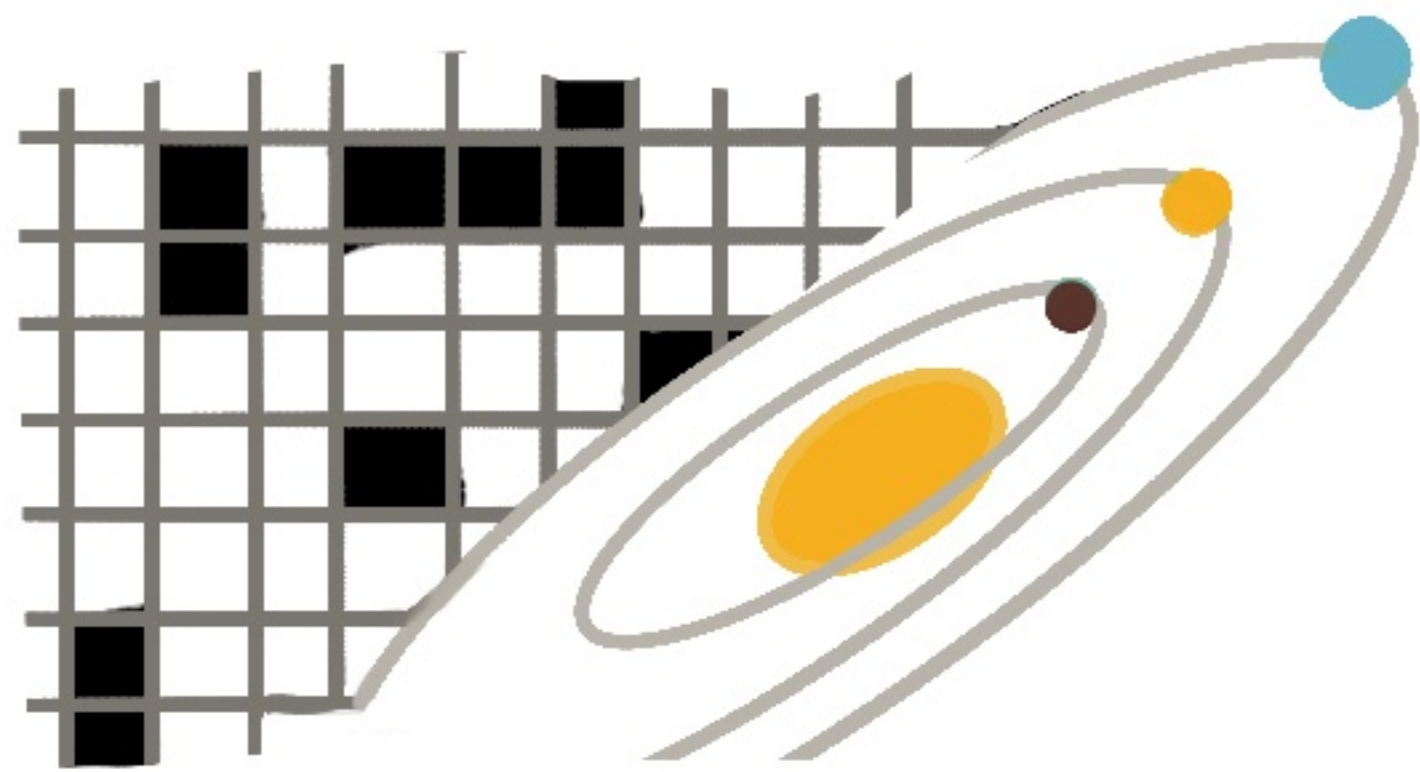
TECHNIQUES TO STUDY EMERGENT BEHAVIOURS COME FROM MANY
DISCIPLINES. HOWEVER, THE CHALLENGE REMAINS THAT THE RULES/PATTERNS
OBSERVED NEED TO BE CONSISTENT ACROSS MANY COMPLEX SYSTEMS.

TWO PATHS

THERE ARE TWO DIFFERENT KINDS OF EMERGENCE STUDIED -
THROUGH EXAMINING:

COMPLEX
PHYSICAL SYSTEMS
CPS

GRID LIKE STRUCTURES
OR INANIMATE OBJECTS



COMPLEX
ADAPTIVE SYSTEMS
CAS

BIOLOGICAL, SOCIO-CULTURAL
OR ECONOMIC SYSTEMS



GOVERNED BY PHYSICAL LAWS
SPELT OUT BY RULES/EQUATIONS

BEHAVIOUR DEPENDS ON
OTHER ELEMENTS

THE PARTS STAY THE SAME

THE PARTS - CALLED AGENTS -
LEARN AND ADAPT

MOST INTERACTIONS ARE BETWEEN
NEAREST NEIGHBOURS

AGENTS INTERACT WITH EACH
OTHER FORMING NETWORKS
AND FEEDBACK LOOPS.

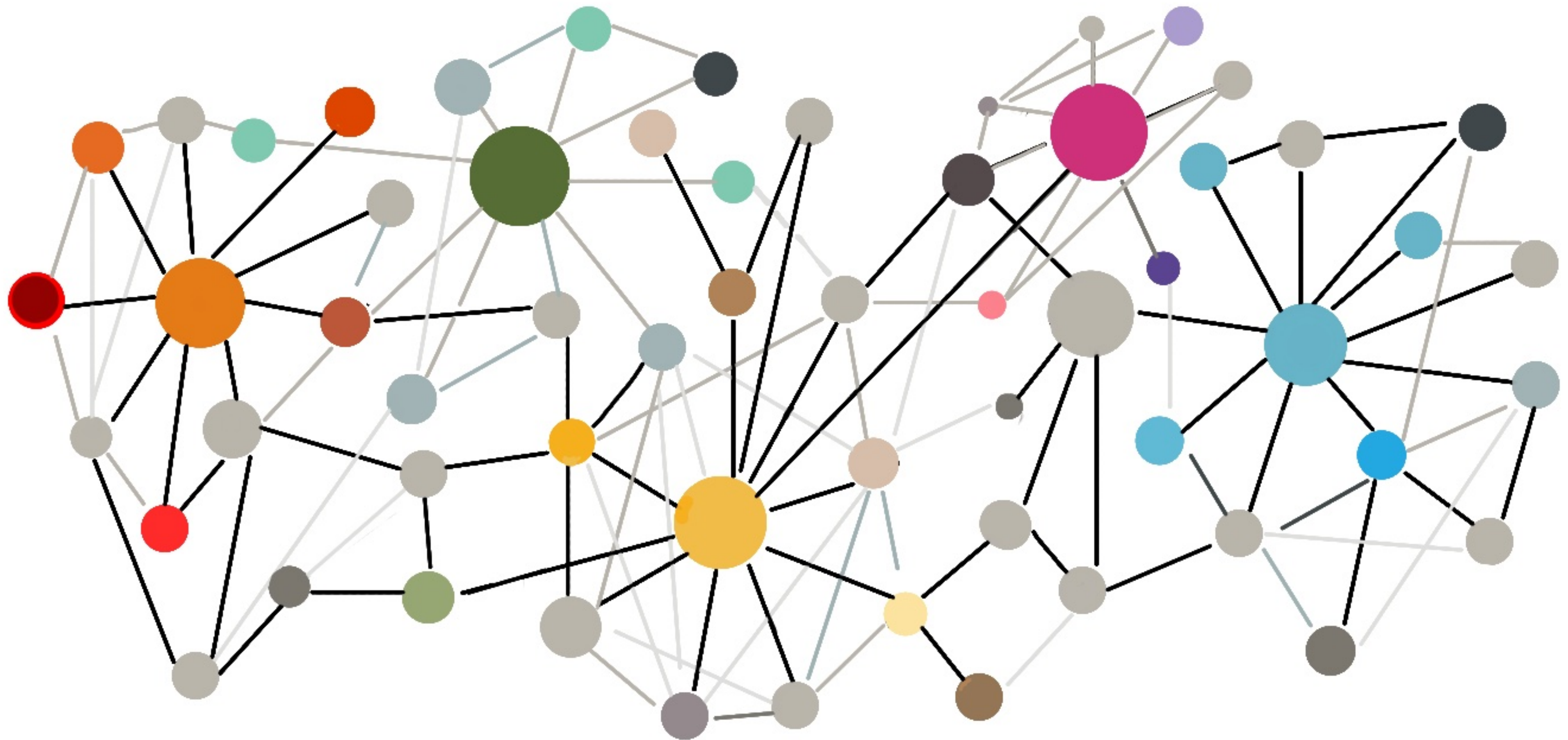
THE POSITION/STATE CHANGES

THE ADAPTATION OVER TIME
RESULTS IN DIVERSITY

THE NON-ADDITIVITY OF EMERGENCE PRESENTS A MATHEMATICAL DIFFICULTY
AND THERE IS NOT YET AN OVERARCHING THEORY OF COMPLEX SYSTEMS

NETWORKS - 1

NETWORK SCIENCE HAS GROWN AS A FIELD OF ITS OWN. IT STUDIES THE PROPERTIES OF A NETWORK & RELATIONSHIPS BETWEEN THE NODES. THE INTENT IS TO USE A COMMON LANGUAGE TO DESCRIBE DIFFERENT NETWORKS AND SHARE LEARNINGS

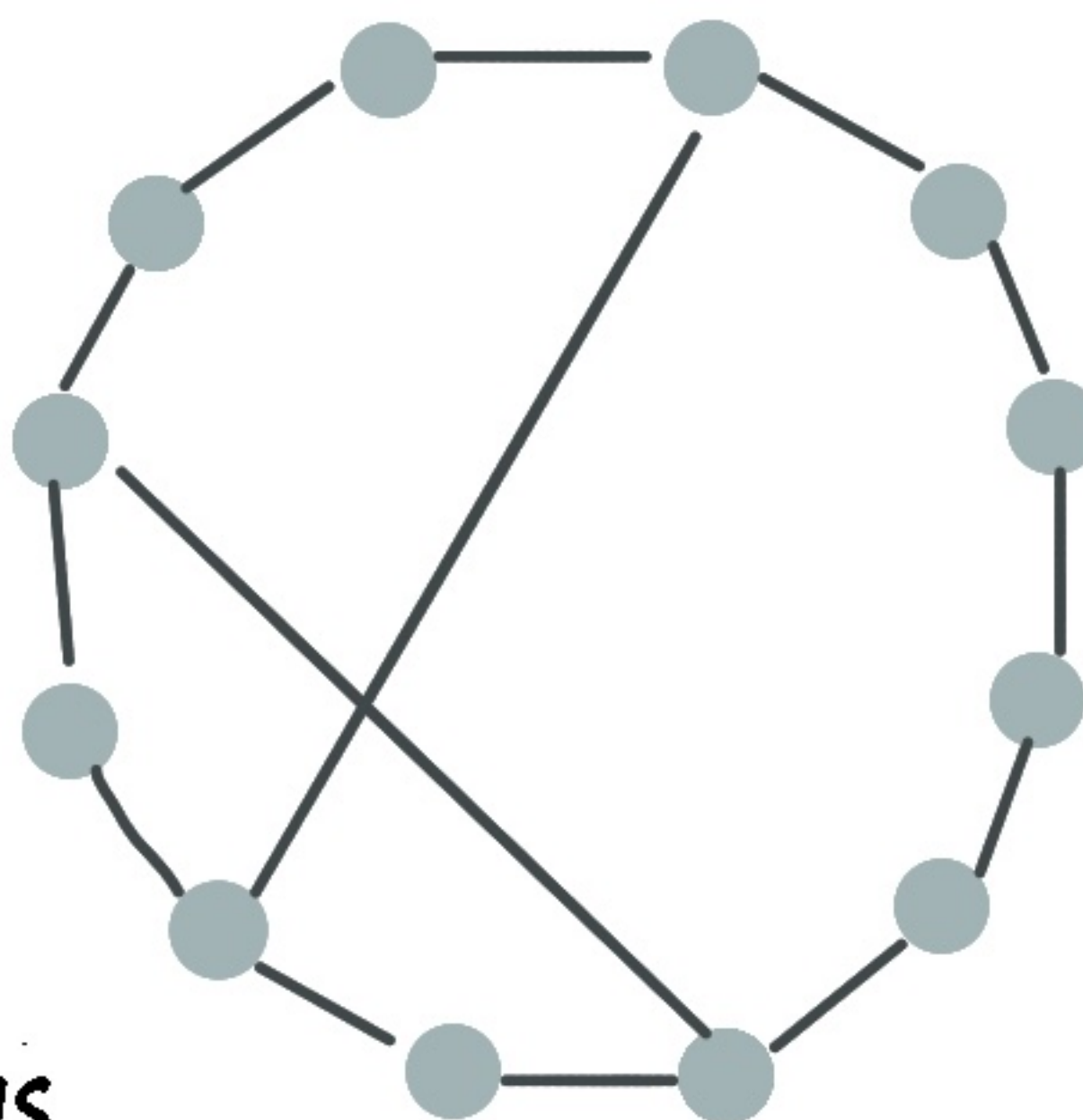


DEGREE/FANOUT

THE NUMBER OF CONNECTIONS OF A NODE

HUB

A NODE WITH A HIGH DEGREE



PATH LENGTH

NUMBER OF CONNECTIONS IN THE SHORTEST PATH BETWEEN TWO NODES

CLUSTER

A MOSTLY SEPARATE INTERCONNECTED SET OF NODES

NETWORKS - 2

SMALL WORLD NETWORK

A SMALL NUMBER OF
HIGH DEGREE NODES AND
HIGH CLUSTERING

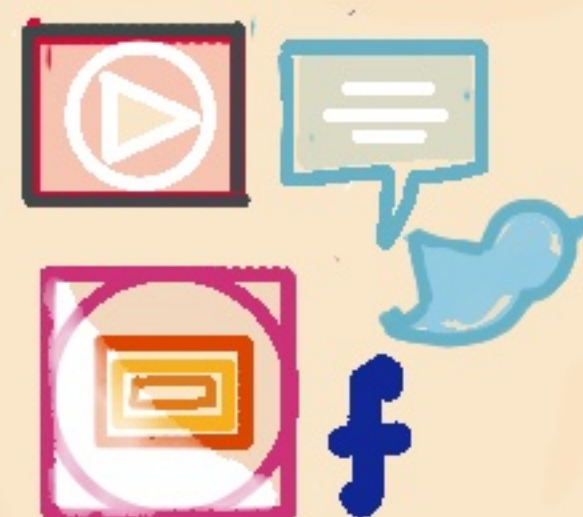
A WORM'S
BRAIN



A POWER GRID



INFLUENCERS



THIS ENSURES A SHORT(ISH) AVERAGE PATH LENGTH AND ENABLES
INFORMATION TO TRAVEL QUICKER AND CHEAPER.

SCALE FREE NETWORK

A TYPE OF SMALL WORLD NETWORK
FOR EXAMPLE, THE WORLD WIDE WEB.



STRUCTURE

- SMALL # OF
HIGH DEGREE NODES
- NODES WITH A
WIDE RANGE OF DEGREES
- SELF SIMILAR



FEATURE

REMOVING A NODE (COMPUTER/PAGE)
DOESN'T AFFECT ITS OPERATION



FAILURE

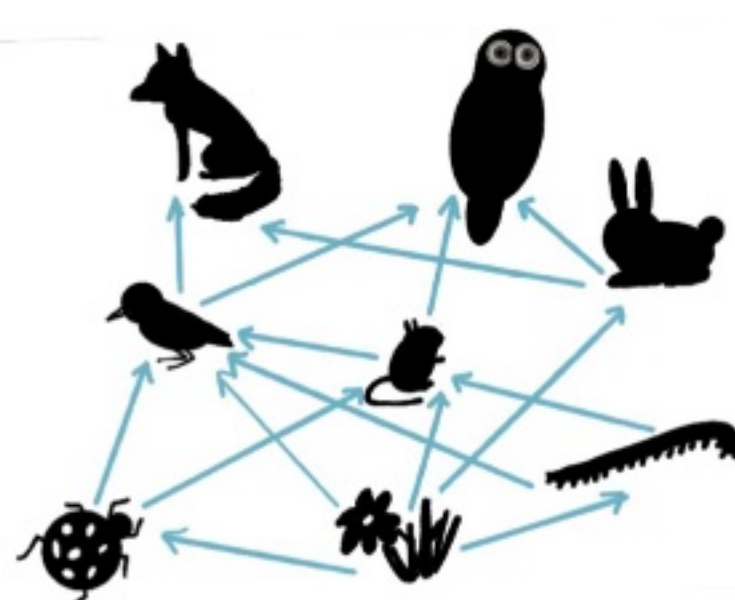
REMOVING ONE OR MORE HUBS
WILL HAVE BIG CONSEQUENCES

EVERYDAY EXAMPLES OF NETWORKS

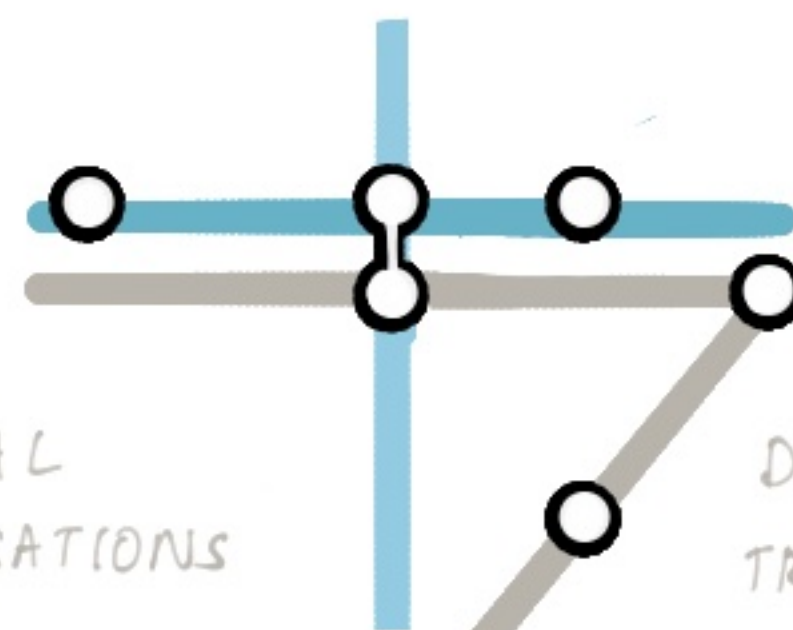
IMMUNE
SYSTEM



ARTIFICIAL
NEURAL
NETWORKS



CRIMINAL
ORGANISATIONS



DISEASE
TRANSMISSION

NEURAL NETWORKS

FOOD WEBS

TRANSPORT NETWORKS

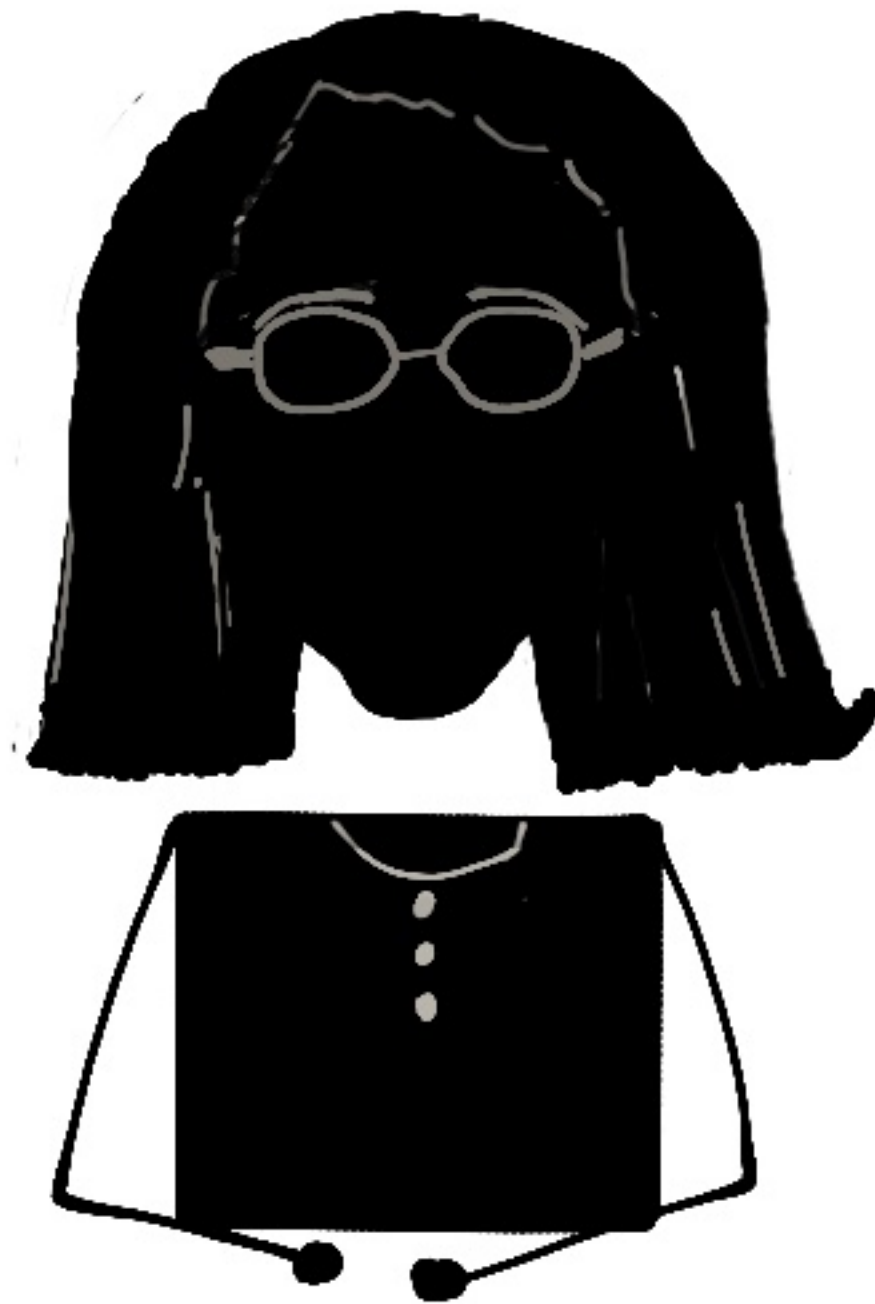
THIS STUDY WILL HELP US BETTER UNDERSTAND THE STRENGTHS &
VULNERABILITIES OF OUR OWN NATURAL AND ORGANISED NETWORKS

BUILDING THE SCIENCE

LET US TAKE A LOOK AT THE SCIENCES THAT COME TOGETHER
IN THE QUEST FOR A UNIFIED THEORY OF COMPLEXITY.

GOALS

COMPLEXITY SCIENCES STUDY BOTH COMPLEX PHYSICAL SYSTEMS AND COMPLEX ADAPTIVE SYSTEMS. THE INTENTION IS TO USE LEARNINGS FROM ONE TO BETTER UNDERSTAND THE OTHER.



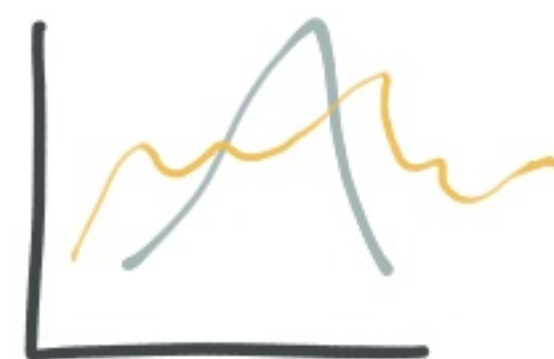
MELANIE MITCHELL

ACCORDING TO MELANIE MITCHELL,
AT SANTA FE INSTITUTE
THE TWO GOALS OF COMPLEXITY ARE:

- CROSS DISCIPLINARY INSIGHTS FROM DEVELOPING MATHEMATICAL AND COMPUTATIONAL TOOLS



MATHEMATICS



STATISTICS



COMPUTATION

APPLY THESE TO A COMPLEX PHYSICAL/ADAPTIVE SYSTEM TO

- GET INSIGHTS
- COMPARE WITH ANOTHER COMPLEX SYSTEM

- A GENERAL THEORY OF COMPLEXITY

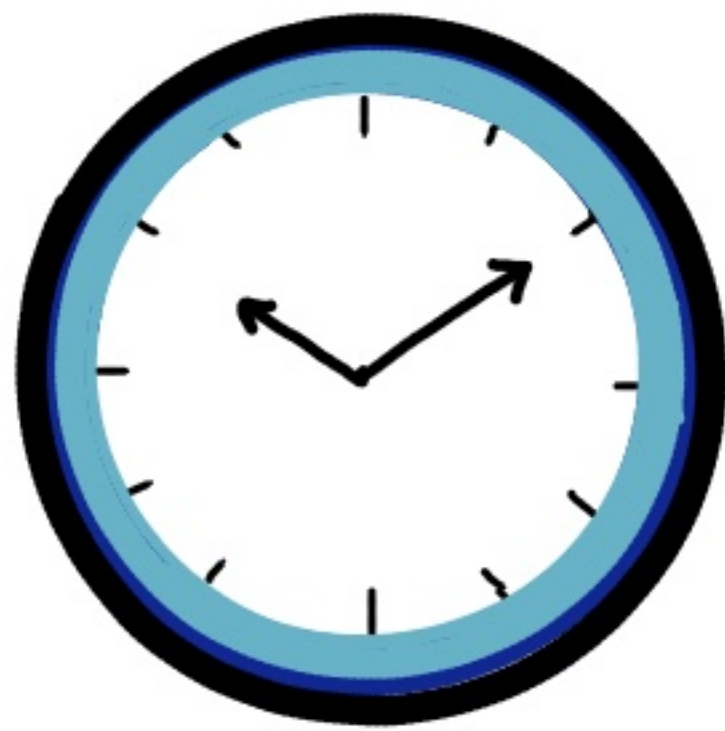
TO UNIFY THE SCIENCES THAT MAKE UP COMPLEXITY

(THE HOLY GRAIL + CONTROVERSIAL GOAL)

CORE DISCIPLINES

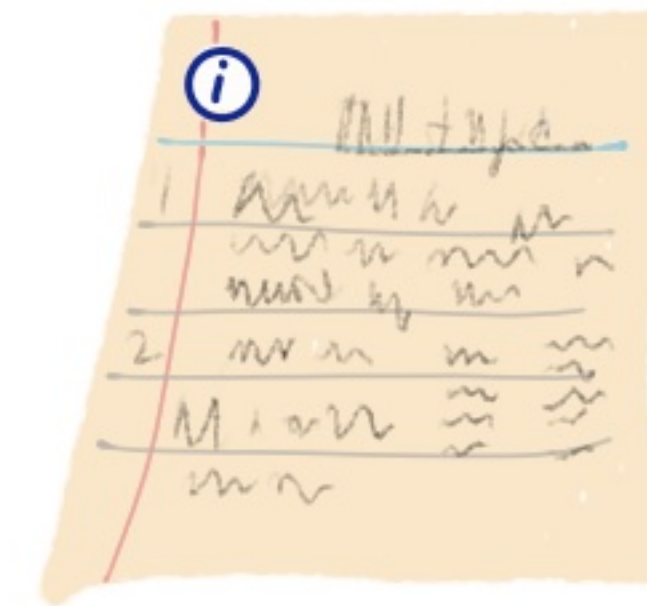
COMPLEXITY BRINGS TOGETHER ASPECTS OF OTHER SCIENCES

DYNAMICS



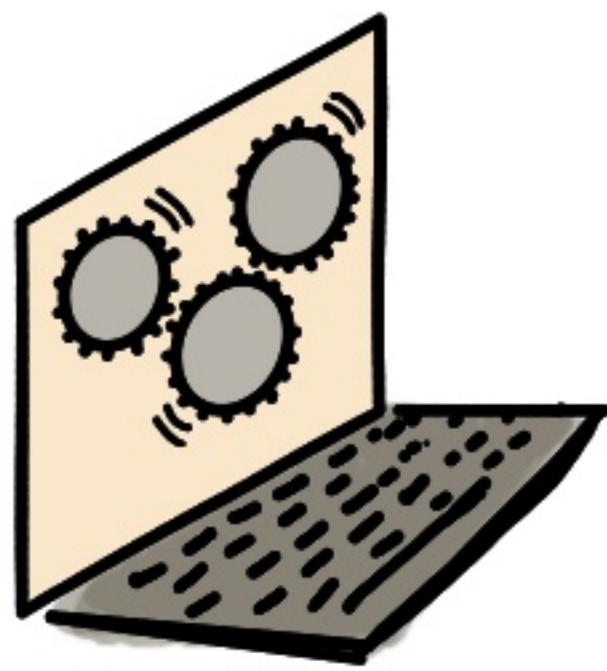
HOW AND WHY THINGS
CHANGE OVER TIME

INFORMATION



SIGNALS EXCHANGED
WITHIN THE SYSTEM

COMPUTATION



HOW THE INFORMATION
IS PROCESSED/INTERPRETED

EVOLUTION



HOW SYSTEMS ADAPT AND LEARN
FROM THE CHANGING ENVIRONMENT

DYNAMICS

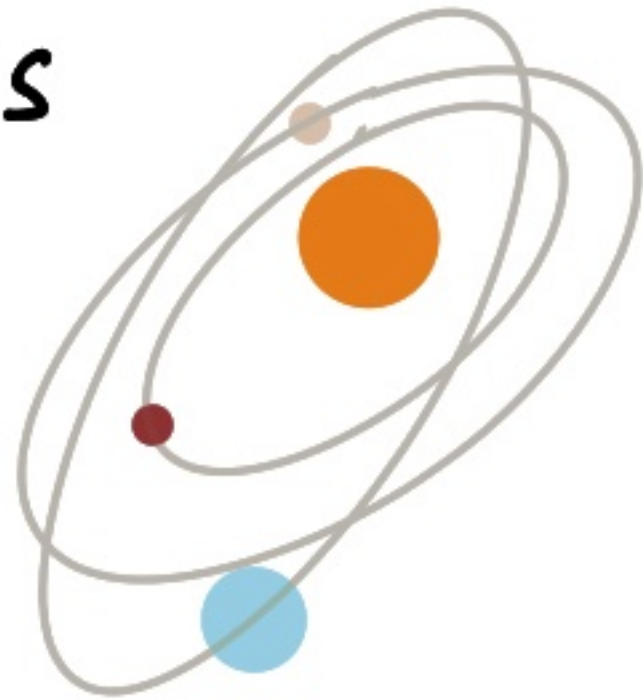
HELPS TO DESCRIBE THE NATURE OF
CHANGE IN A COMPLEX SYSTEM

ALL ABOUT DYNAMICS

DYNAMICS IS ABOUT HOW THINGS CHANGE OVER TIME

THERE ARE MANY
KINDS OF DYNAMICS
UNDER STUDY

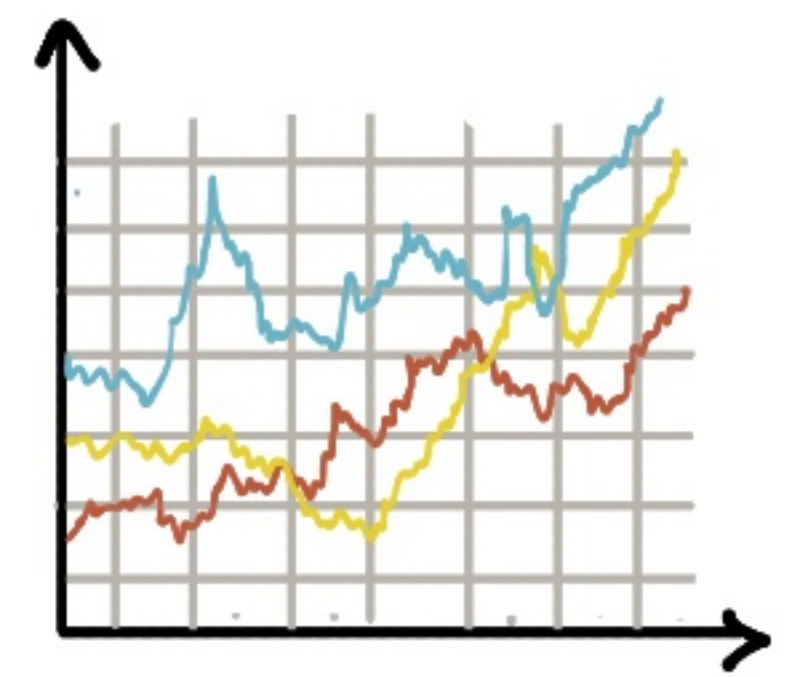
ORBITS



GROUPS



STOCK PRICES



WHILE THERE ARE MATHEMATICAL TOOLS
TO STUDY CHANGE AND MAKE PREDICTIONS,
NOT ALL DYNAMICAL SYSTEMS ARE EASY TO PREDICT.

... Calculus Algebra Topology Differential Equations ...

COMPLEX BEHAVIOURS IN DYNAMICAL SYSTEMS COULD BE THE RESULT OF

ITERATION



REPEATING THE
SAME BEHAVIOURS
OVER AND OVER

NON-LINEARITY



WHERE THE WHOLE
IS NOT THE SUM
OF THE PARTS

CHAOS



SENSITIVE
DEPENDENCE ON
INITIAL CONDITIONS

WE WILL NOW LOOK AT EACH OF THESE COMPLEX BEHAVIOURS

ITERATION

REPEATING THE SAME BEHAVIOURS PRODUCES COMPLEX PATTERNS.

HERE IS A LINE



REMOVE THE MIDDLE
ONE THIRD SEGMENT

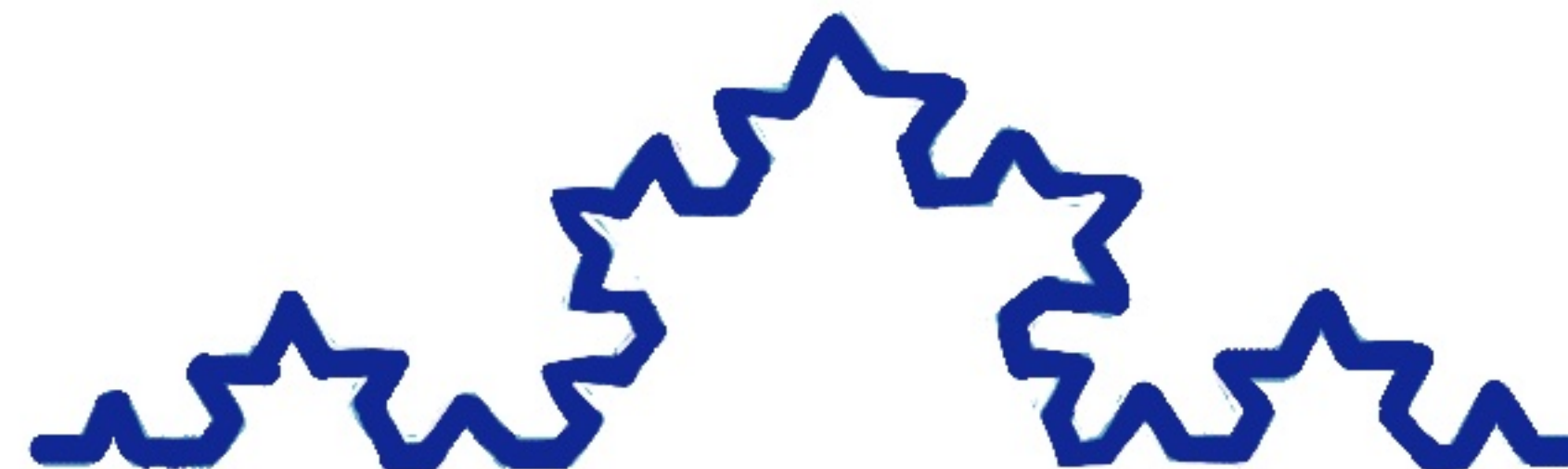
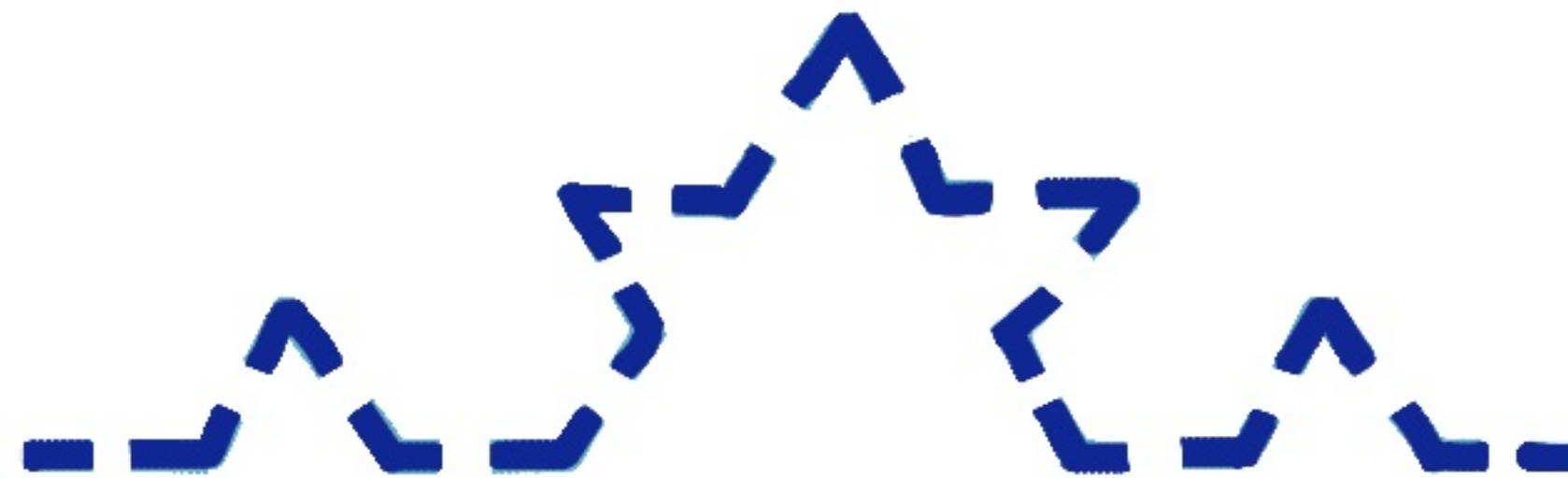
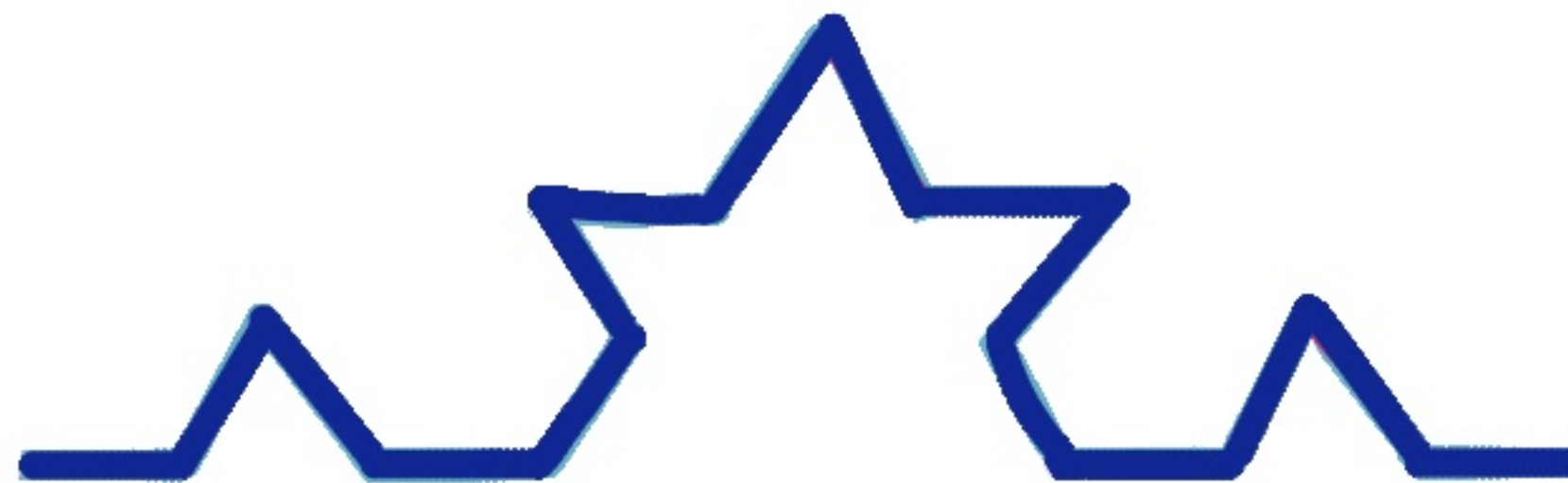
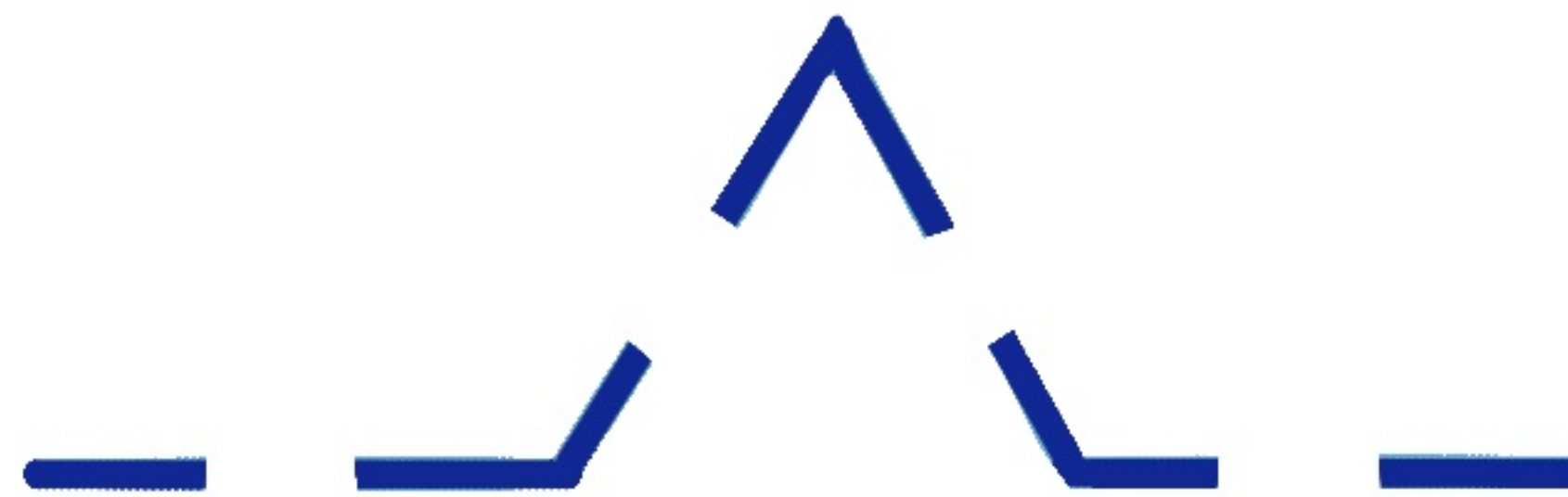


FILL THE GAP WITH
TWO LINES SO EACH..



..IS THE LENGTH OF
THE REMOVED SEGMENT

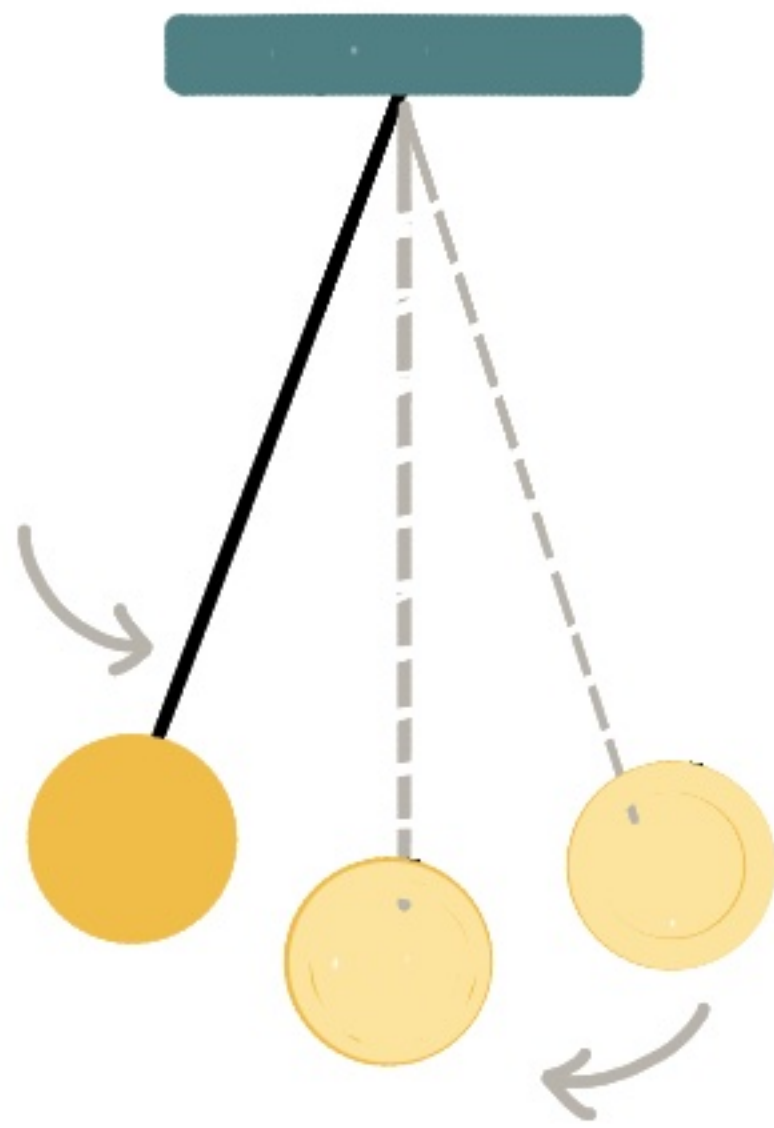
REPEAT FOR EACH SEGMENT



THIS IS A KOCH CURVE, A SELF SIMILAR PATTERN - A FRACTAL

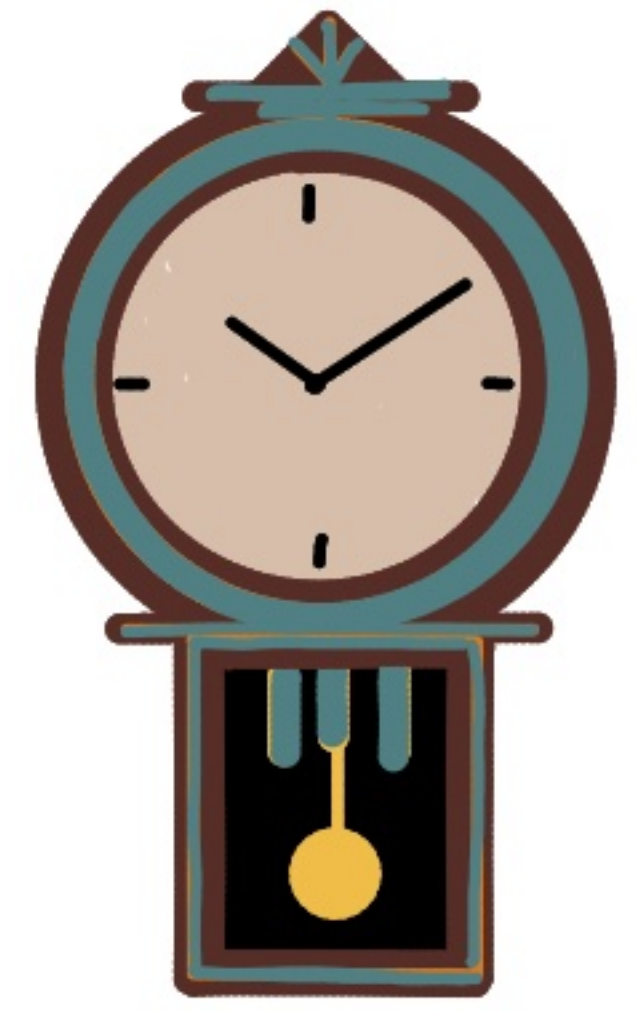
NON LINEARITY

A SIMPLE PENDULUM



A SYSTEM WITH
A STRING FIXED ON ONE END AND
A WEIGHT ATTACHED TO THE OTHER.

THE MOTION IS PREDICTABLE
EVERY RUN.

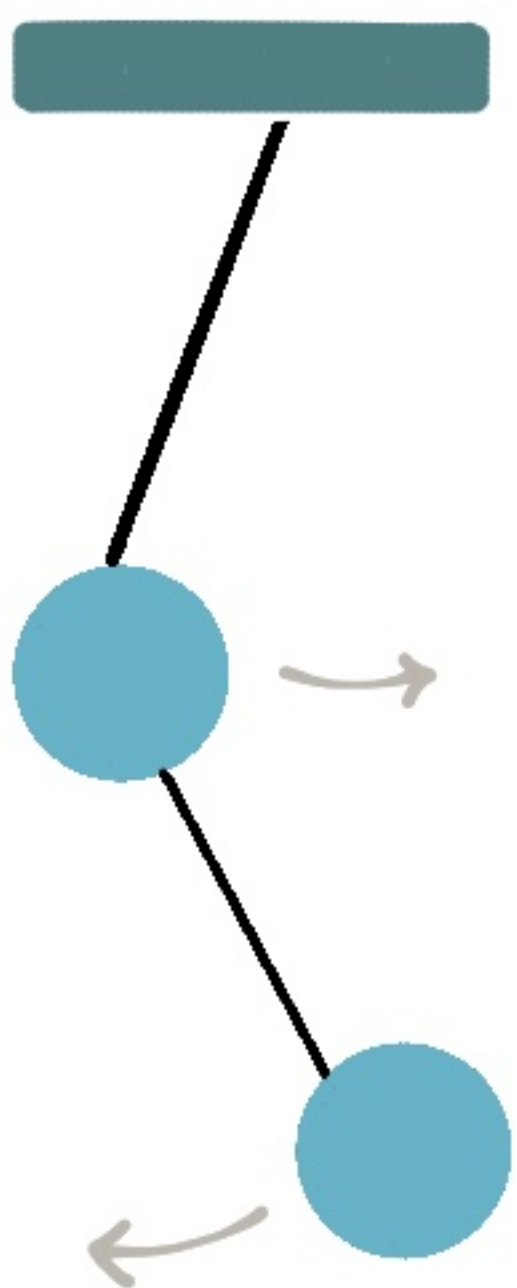


THE EQUATIONS
TO CALCULATE
THE FREQUENCY ...

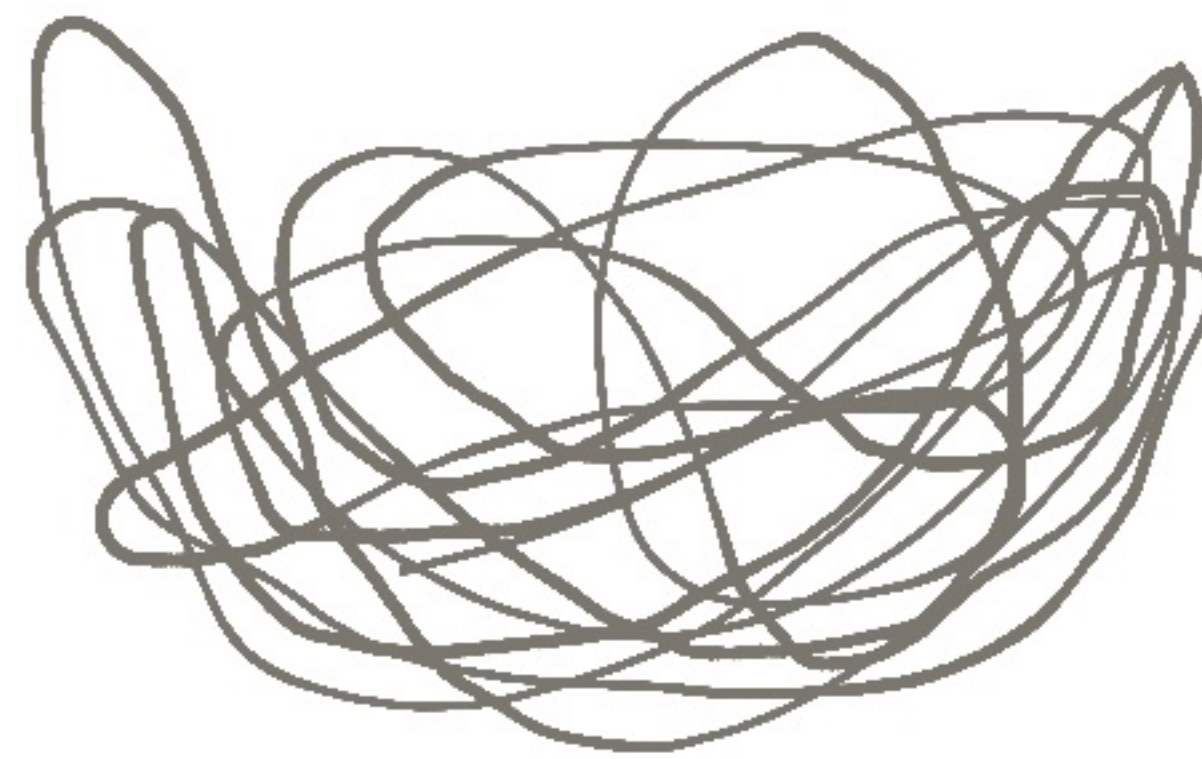
$$\text{Period } T = 2\pi\sqrt{\frac{L}{g}}$$
$$\text{Frequency } f = \frac{1}{2\pi}\sqrt{\frac{g}{L}}$$

...AND PERIOD OF
ITS MOTION ARE
SOLVABLE BY HAND

A DOUBLE PENDULUM IS CHAOTIC



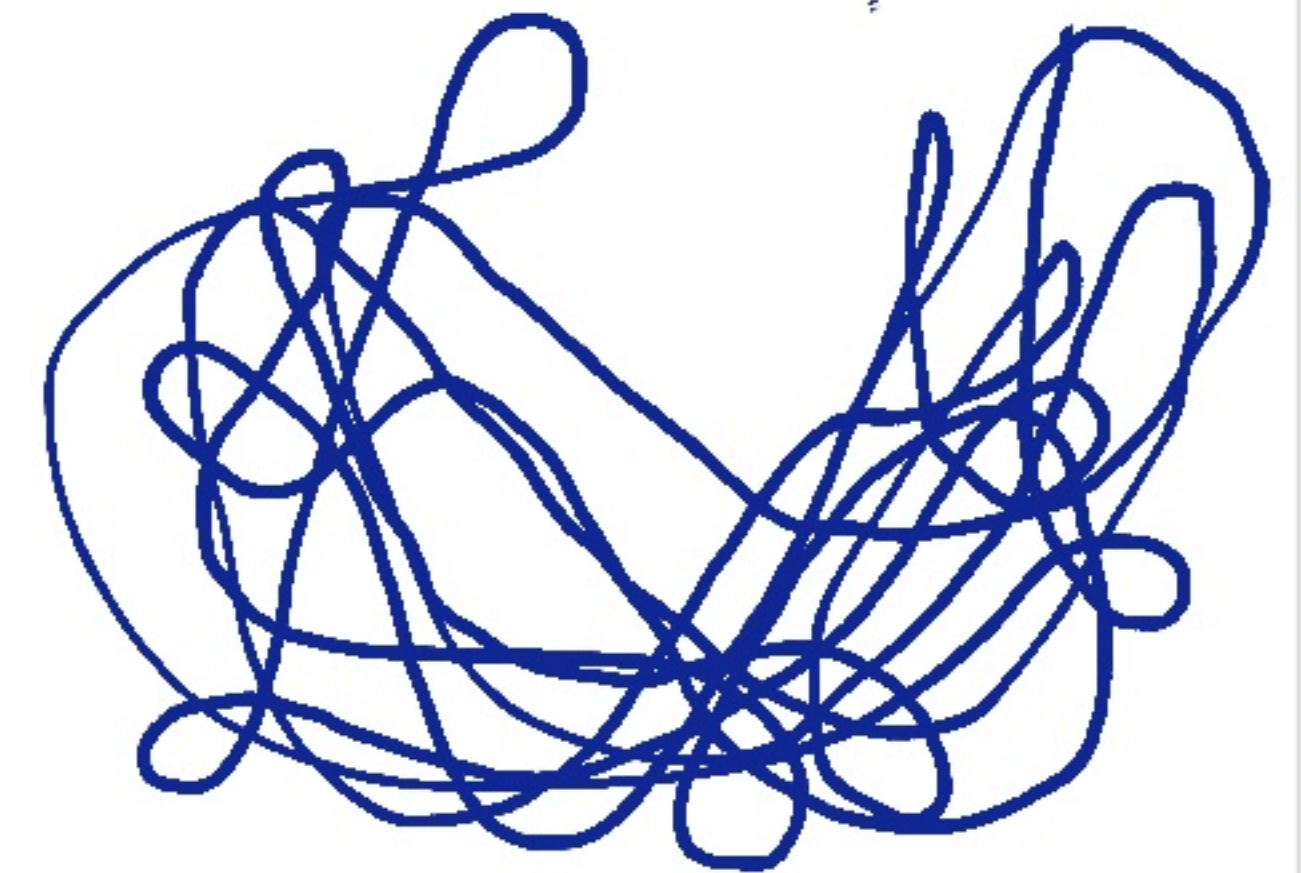
A PENDULUM
WITH A PENDULUM
ATTACHED TO IT.



PATH-1

THE PATH TRACED
LOOKS RANDOM
AND UNPREDICTABLE

NEEDS A COMPUTER
TO SOLVE EQUATIONS



PATH-2

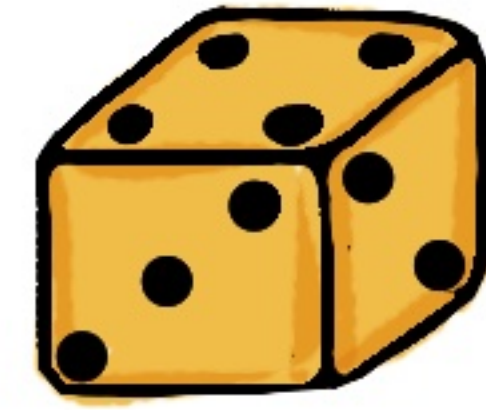
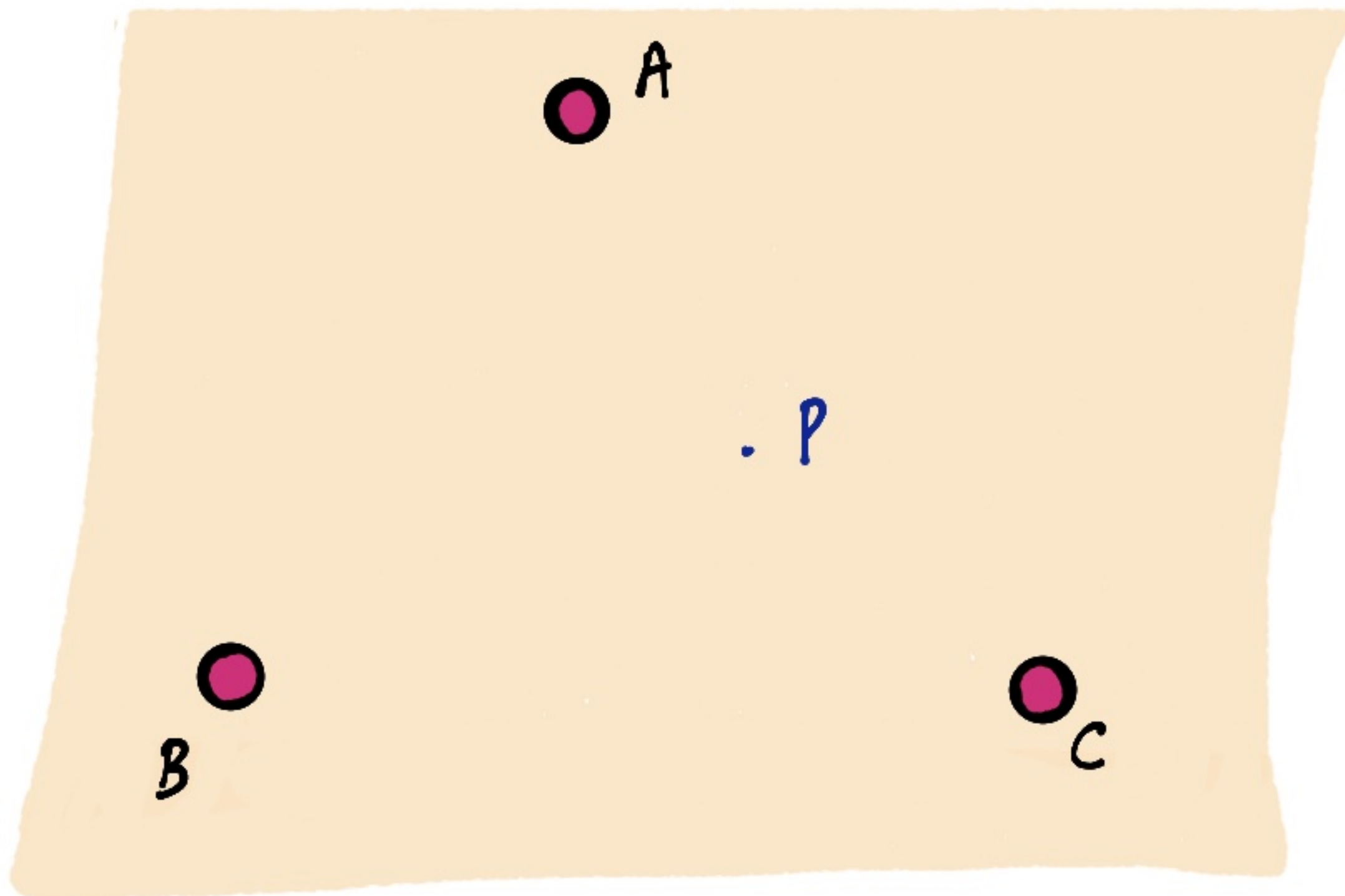
A SECOND RUN
TRACES OUT A
VERY DIFFERENT PATH

SMALL DIFFERENCE IN
INITIAL CONDITIONS

THE NON LINEARITY OF DYNAMIC SYSTEMS CAN BE THOUGHT OF AS:
MOTION OF 2 SIMPLE PENDULUMS \neq MOTION OF 1 DOUBLE PENDULUM

CHAOTIC OR FRACTAL?

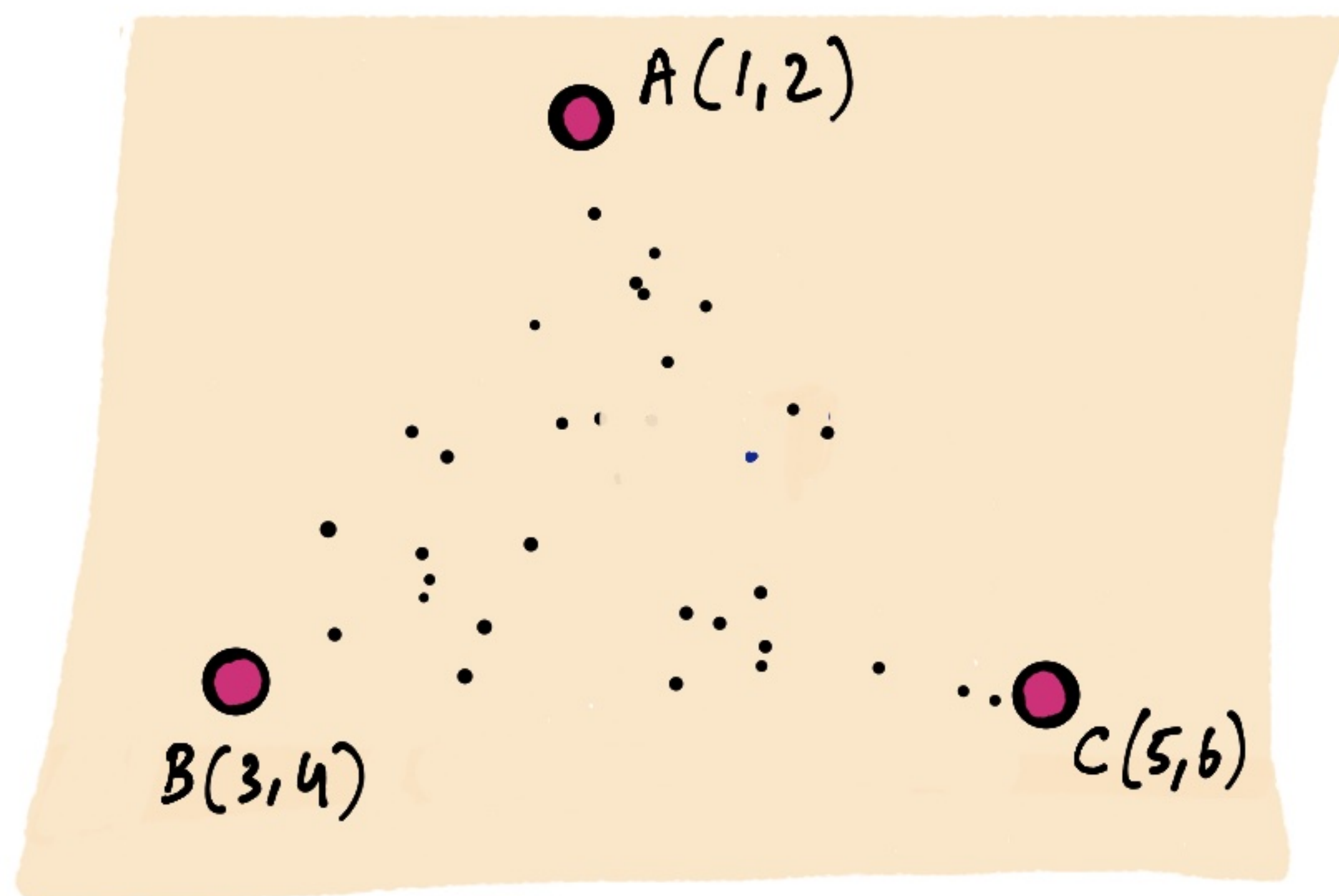
DRAW THREE DOTS A, B AND C. MARK A RANDOM POINT P FROM WHERE TO START. USE A DIE TO PLOT OTHER POINTS



(1,2) → MOVE HALFWAY TO A

(3,4) → MOVE HALFWAY TO B

(5,6) → MOVE HALFWAY TO C



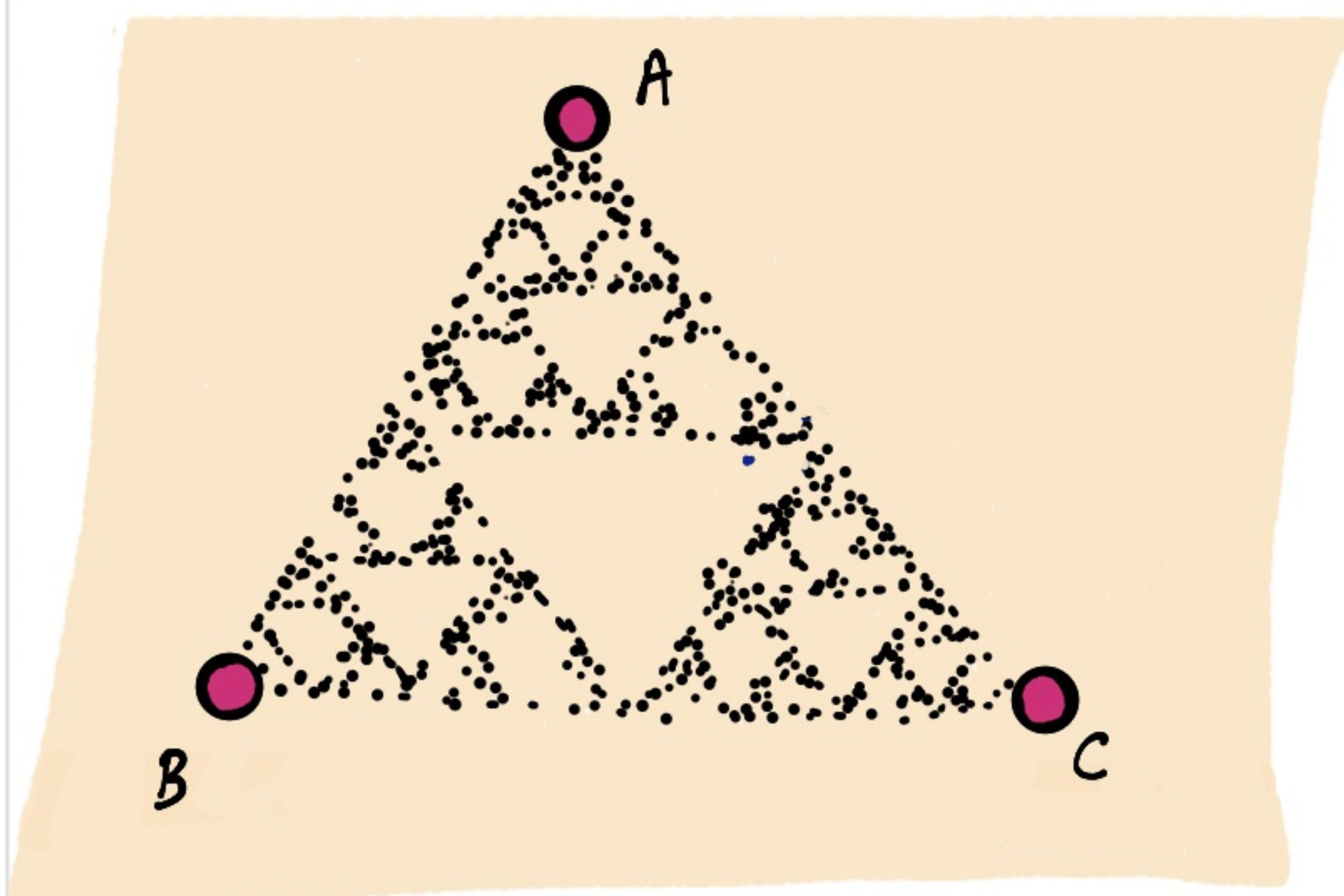
WHAT STARTS OFF AS

RANDOM DOTS BEGINS TO

LOOK MORE STRUCTURED

WITHIN A FEW HUNDRED

ITERATIONS



THIS SET OF RULES TENDS
TOWARDS A PATTERN CALLED

AN ATTRACTOR. THE PATTERN

IS A FAMOUS FRACTAL:

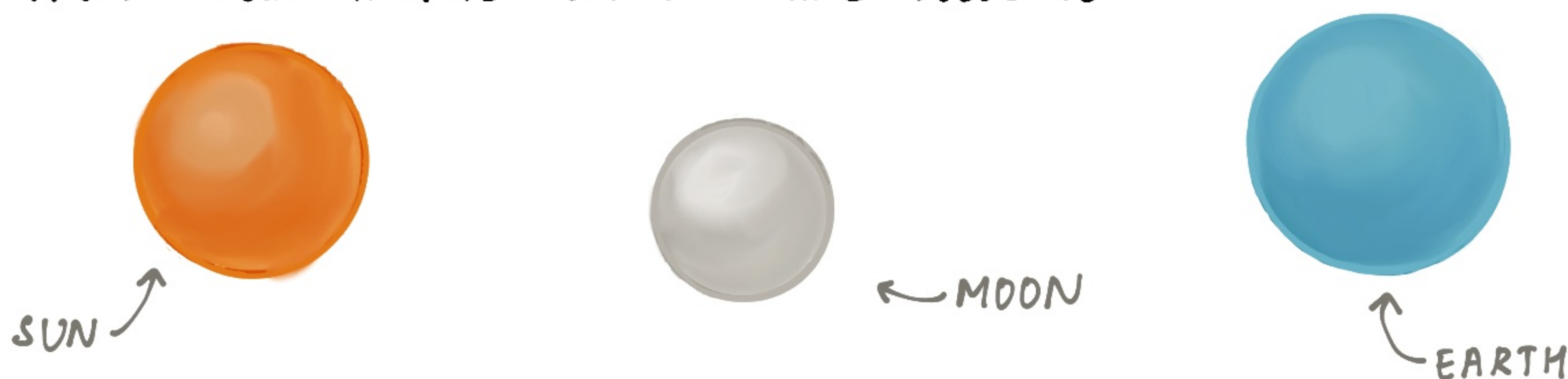
THE SIERPINSKI TRIANGLE

CHAOS & POINCARÉ

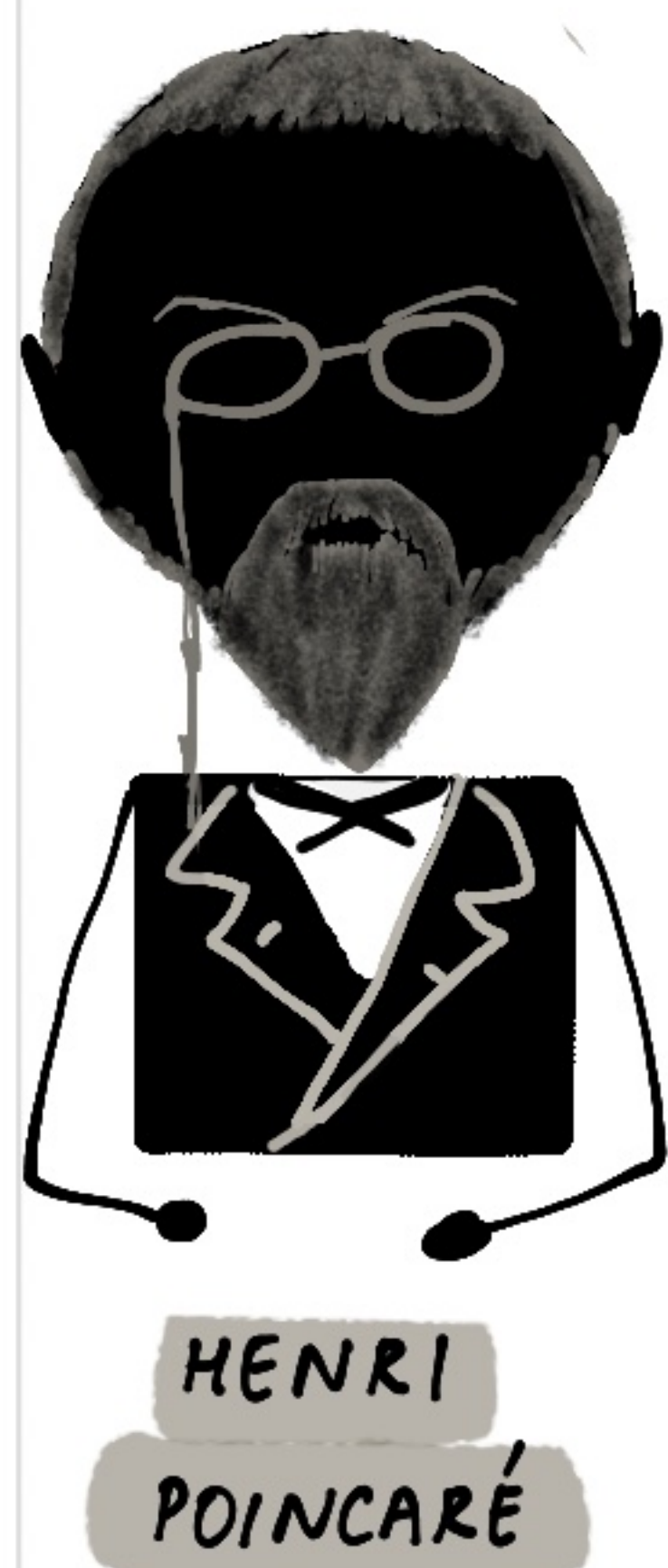
NEWTON'S EQUATIONS DESCRIBE THE MOTION OF PLANETS ACCURATELY ONLY IN THE CASE WHERE THERE ARE EXACTLY TWO BODIES.

IN THE LATE 1800s:

MATHEMATICIAN HENRI POINCARÉ ATTEMPTED TO DESCRIBE THE MOTION OF 3 BODIES USING NEWTON'S LAWS OF MOTION AND GRAVITATION FROM THEIR INITIAL POSITIONS AND VELOCITIES



POINCARÉ DIDN'T SUCCEED



My work had a serious error

I had to withdraw my paper...

...paying a huge amount of money

BUT HE CAME TO THE REALISATION THAT

WE CAN KNOW THE INITIAL CONDITIONS OF ANY EVENT ONLY APPROXIMATELY

SMALL DIFFERENCES IN THE INITIAL CONDITIONS PRODUCE VERY GREAT ONES IN THE FINAL PHENOMENA

POINCARÉ'S WORK LAID THE FOUNDATION OF CHAOS THEORY

UNPREDICTABLE AS WEATHER

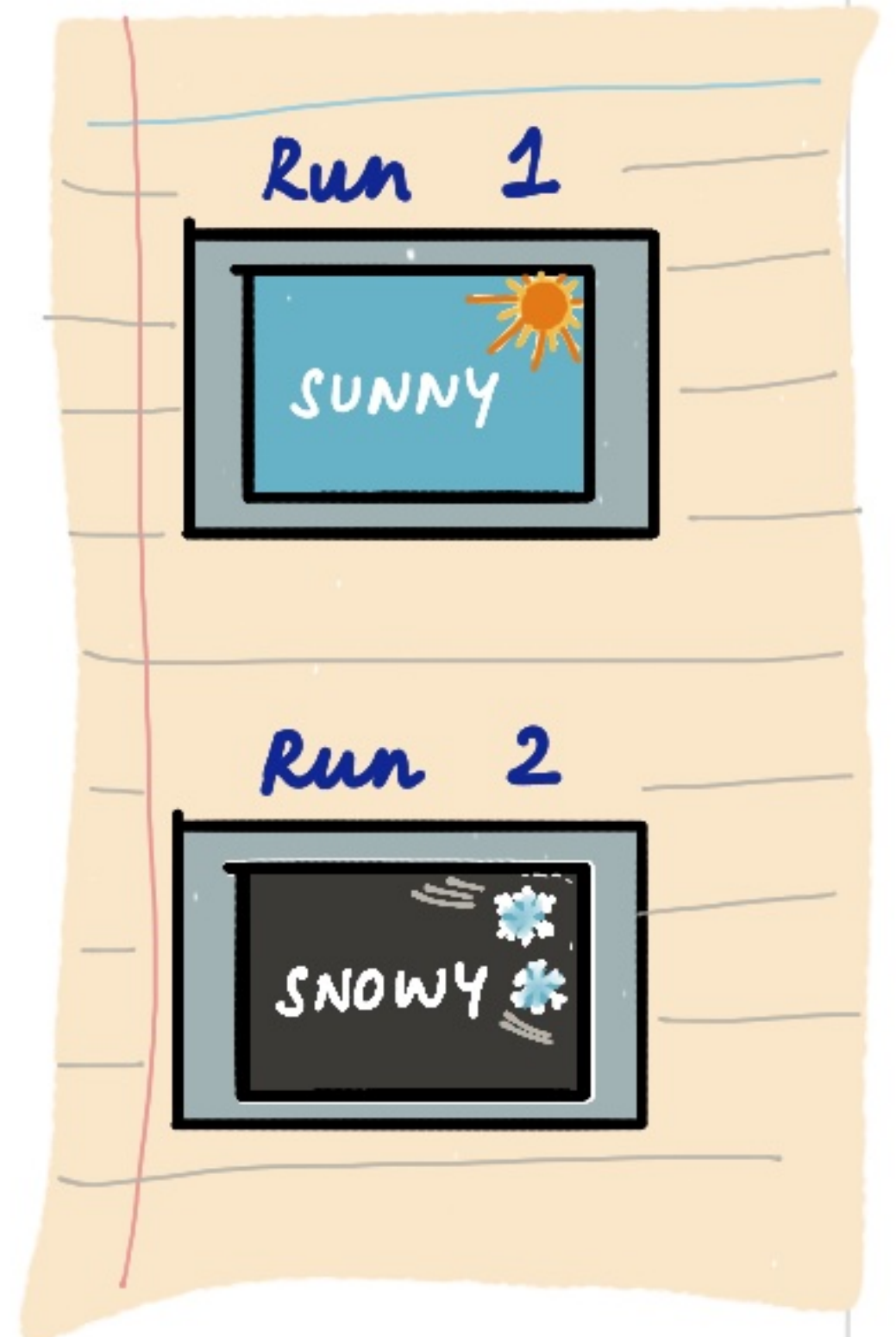


EDWARD
LORENZ

METEOROLOGIST EDWARD LORENZ
WAS SIMULATING ON HIS COMPUTER,
A SIMPLE MODEL OF THE ATMOSPHERE

in only twelve equations!

ON THE SECOND RUN, HE FOUND THAT
THE RESULTS WERE VERY DIFFERENT



THE SECOND RUN HAD A DIFFERENT INPUT VALUE IN ONE OF THE
DECIMAL PLACES DUE TO ROUNDING.

Temperature : 27.084271°

Temperature : 27.084°

SMALL CHANGES AMPLIFIED IN THIS DETERMINISTIC SYSTEM RESULTING
IN 'CHAOTIC' BEHAVIOUR

1963

Deterministic
Non periodic flow

By
Edward Lorenz



ELLEN
FETTER



MARGARET
HAMILTON

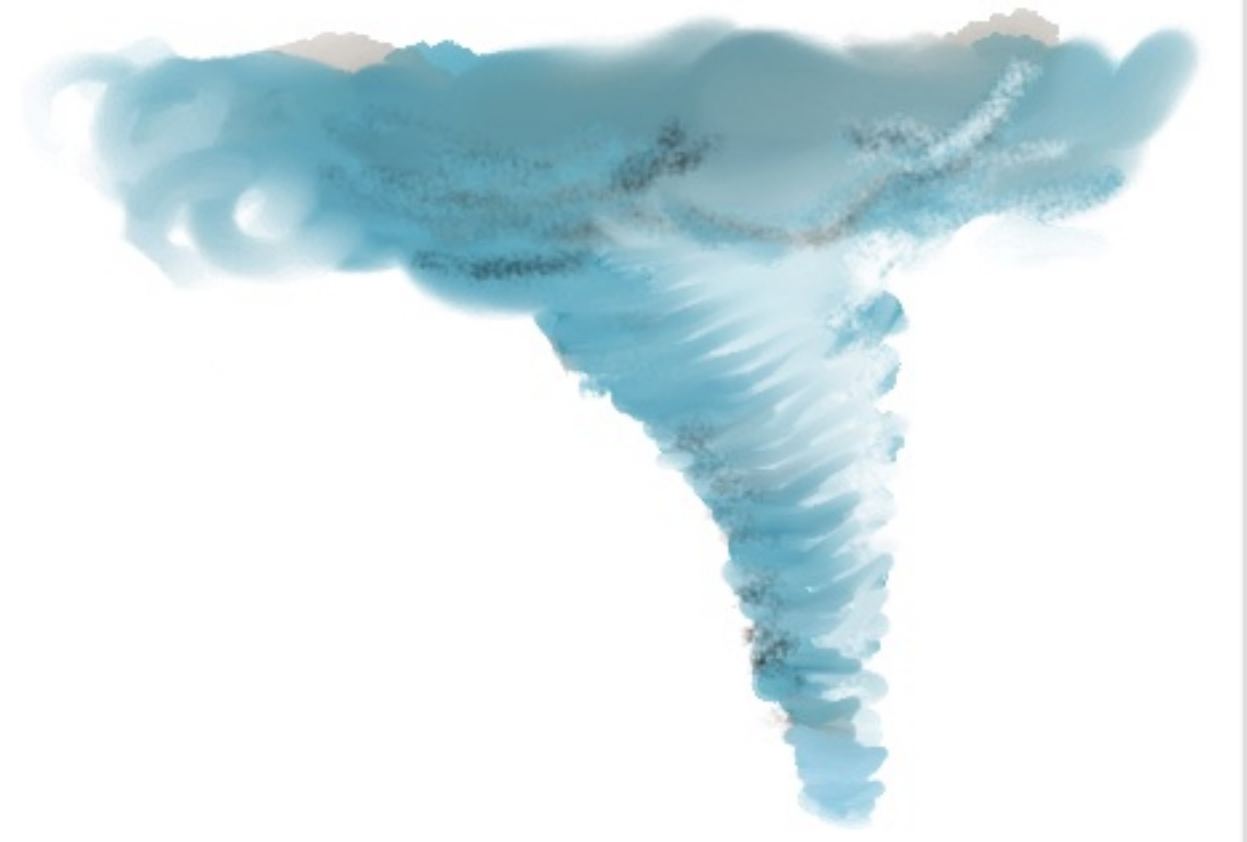
LORENZ PURSUED THIS RESEARCH WITH HELP FROM HAMILTON AND FETTER
AND PUBLISHED HIS OBSERVATIONS IN A PAPER

THE BUTTERFLY EFFECT

CHAOS IS THE SENSITIVE DEPENDENCE ON INITIAL CONDITIONS

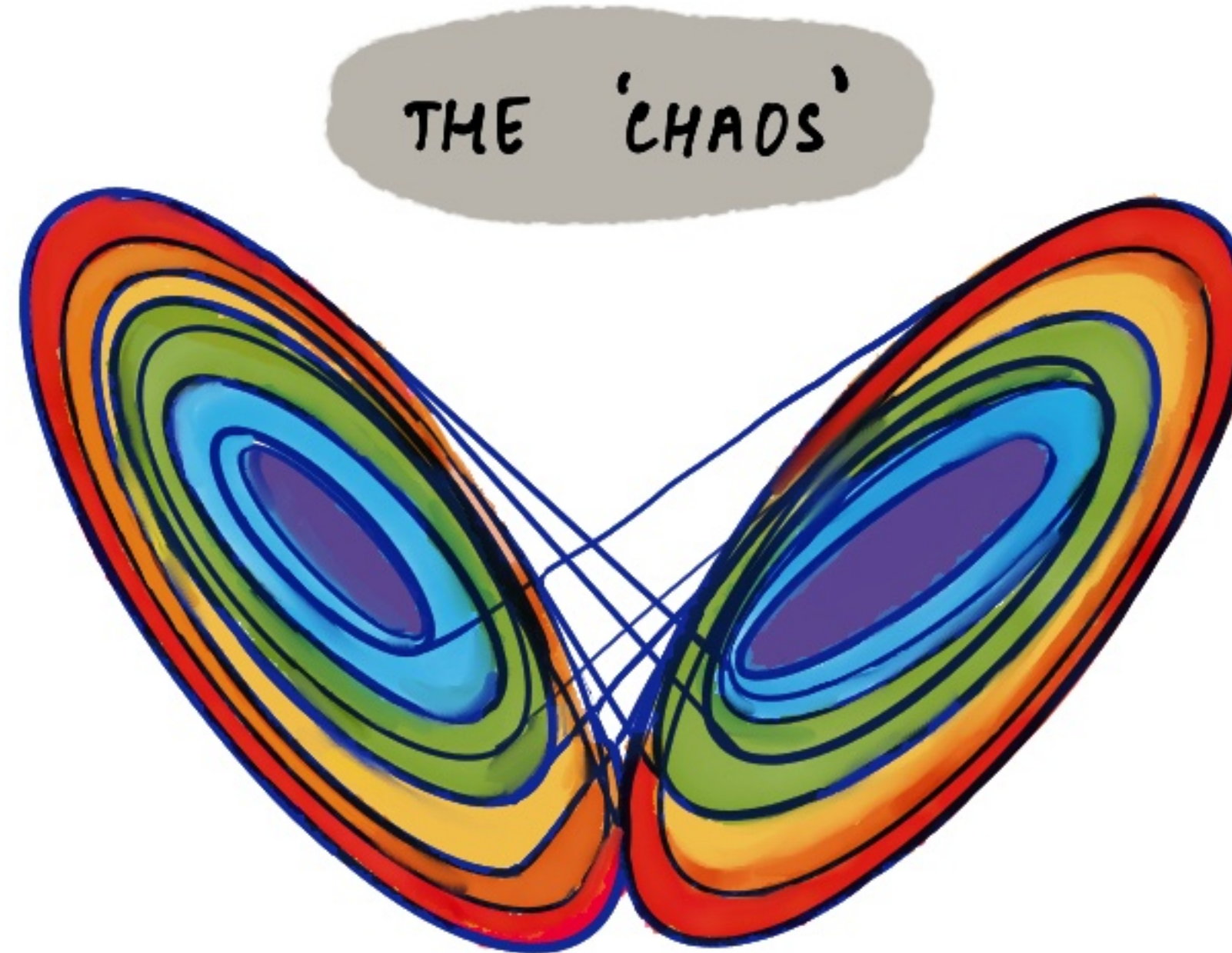


APPARENTLY CAPABLE OF SETTING OFF
A TORNADO IN TEXAS
BY THE FLAPPING OF
A BUTTERFLY'S WINGS IN BRASIL



THIS PHENOMENON THAT LORENZ WROTE ABOUT CAME TO BE
POPULAR AS THE BUTTERFLY EFFECT.

LORENZ NOTICED THAT THE SOLUTIONS TO A SET OF 3 OF THOSE EQUATIONS
TAKE THE SHAPE OF CURVED LINES LOOPING AROUND TWO "CENTRES".



THE 'CHAOS'

NEVER RETRACES
THE SAME PATH

CALLED THE
LORENZ ATTRACTOR

LOOKS LIKE THE
WINGS OF A BUTTERFLY

FORMS AN
ORDERLY PATTERN

TWO PATHS STARTING NEAR EACH OTHER CAN DIVERGE, ONE SEPARATING
OFF TO THE RIGHT HALF AND THE OTHER TO THE LEFT, CAUSING THE
UNPREDICTABILITY BETWEEN THE TWO RUNS

DETERMINISTIC CHAOS - 1

$$x_{n+1} = \lambda x_n (1 - x_n)$$

x = POPULATION

$n+1$ = NEXT YEAR

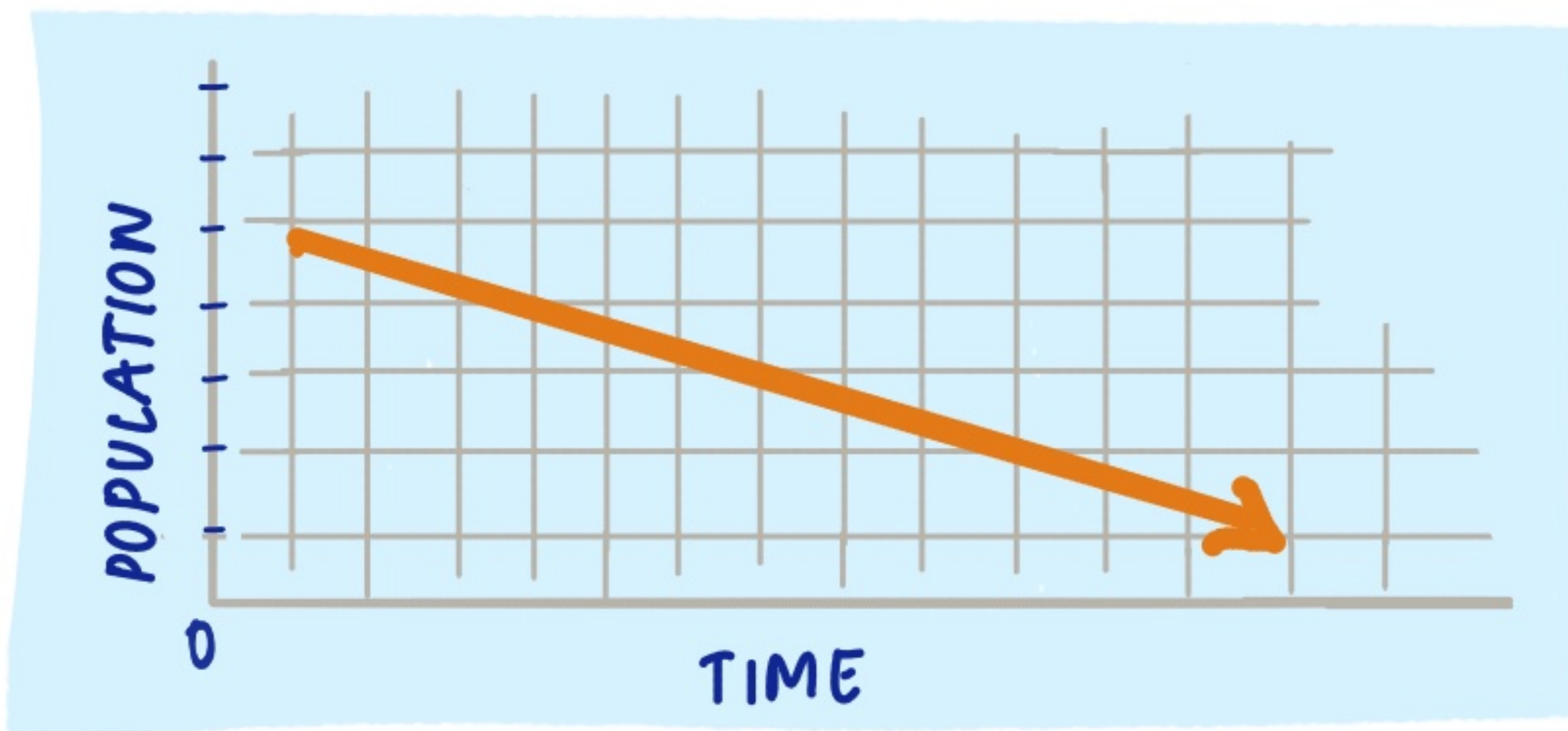
λ = GROWTH RATE

n = THIS YEAR

→ from a paper
by Robert May

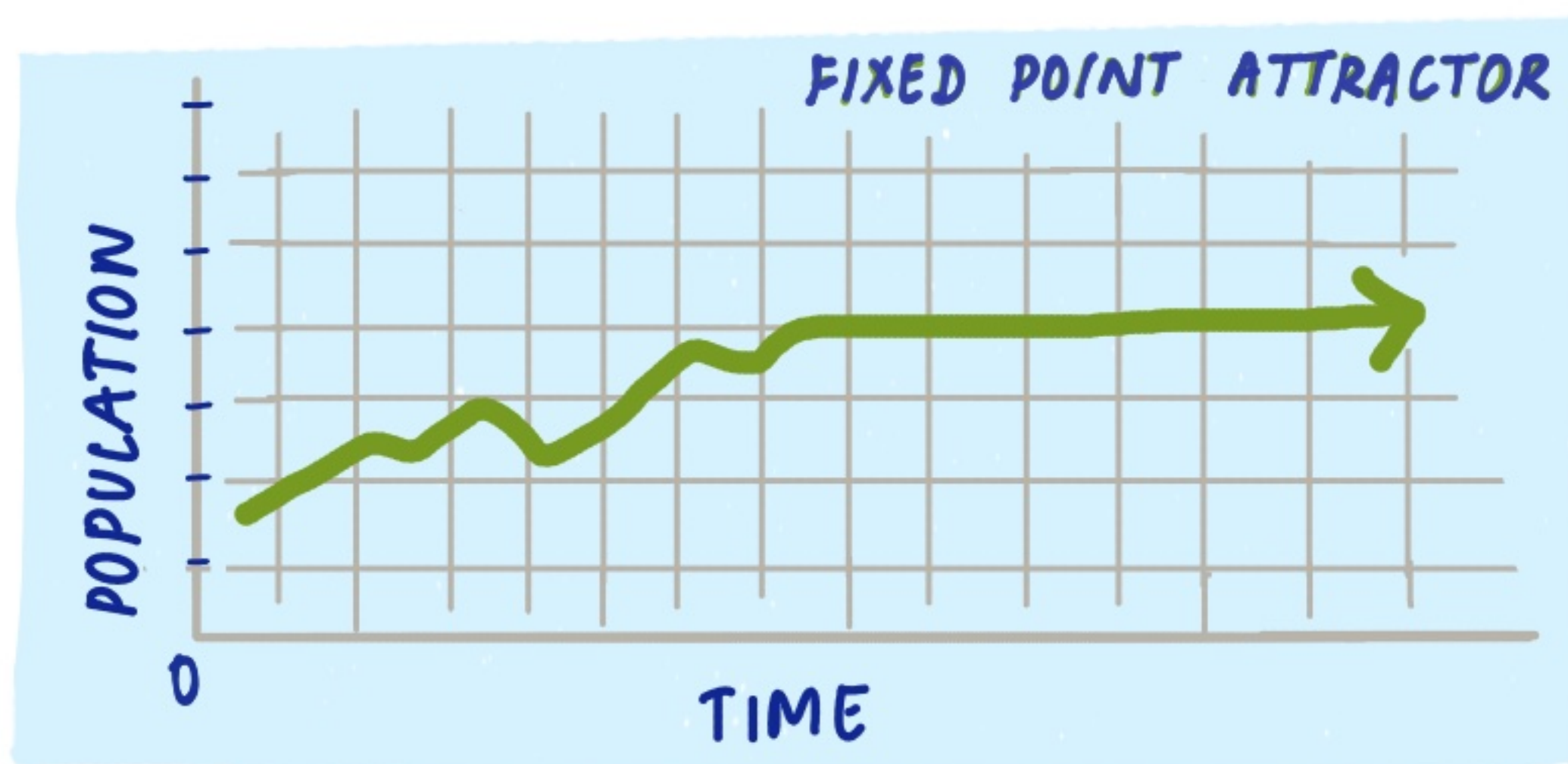
THIS IS AN EQUATION THAT MODELS POPULATION GROWTH

IF THE GROWTH RATE IS BETWEEN 0-1



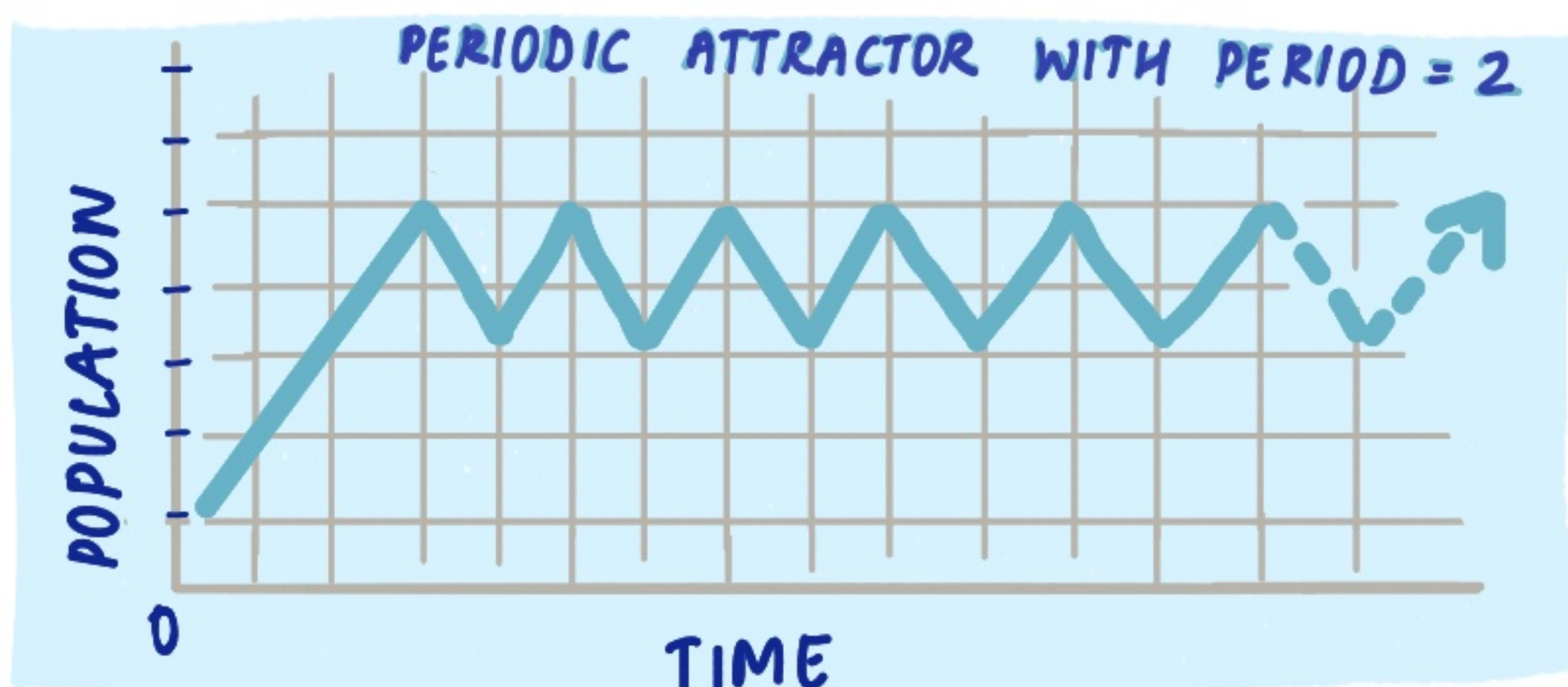
THE POPULATION
DIES OUT OVER A
FEW GENERATIONS

FOR SOME GROWTH RATES ABOVE 1



THE POPULATION
STABILISES OVER A
FEW GENERATIONS

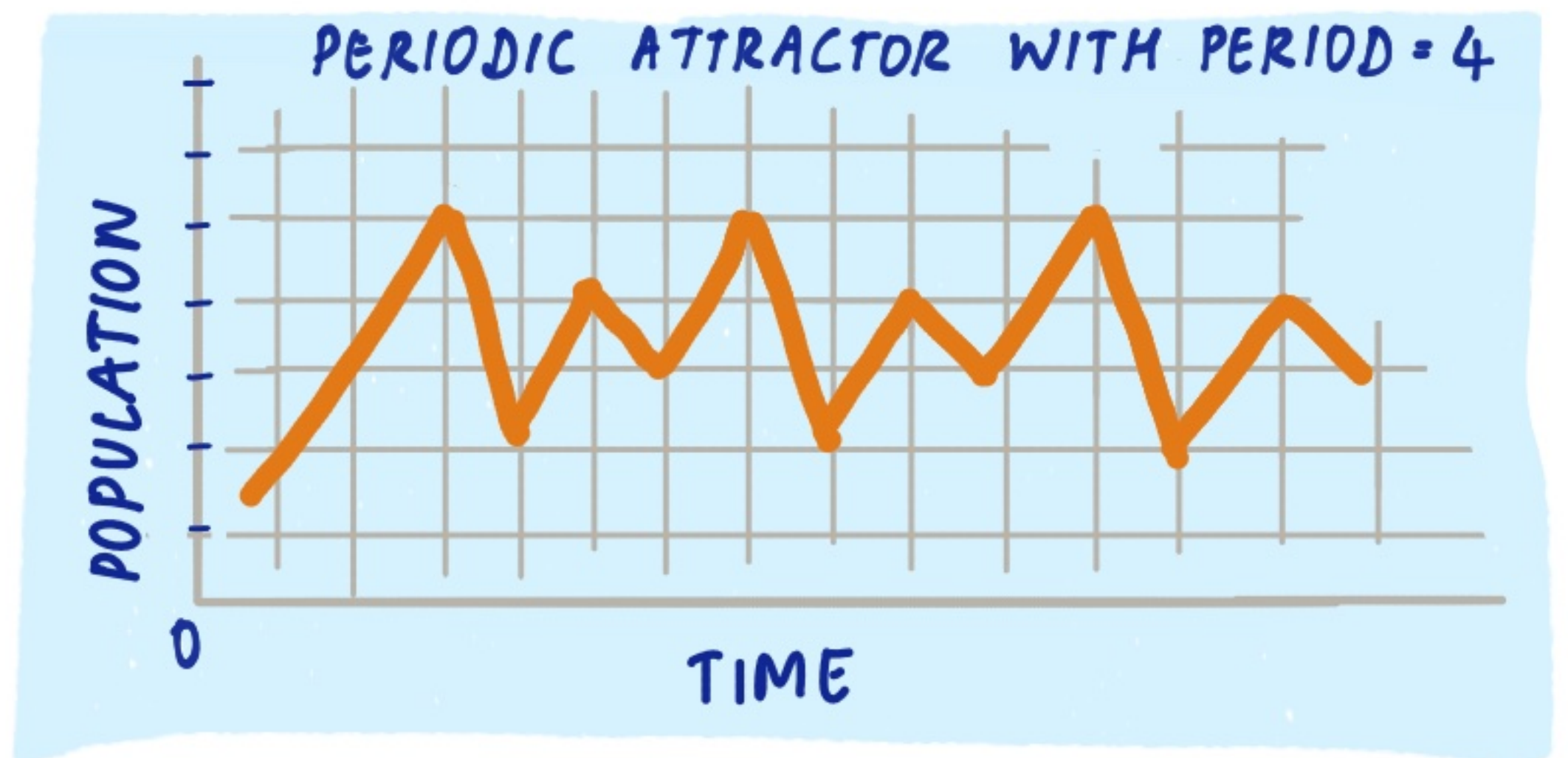
FOR HIGHER GROWTH RATES AROUND 3.2



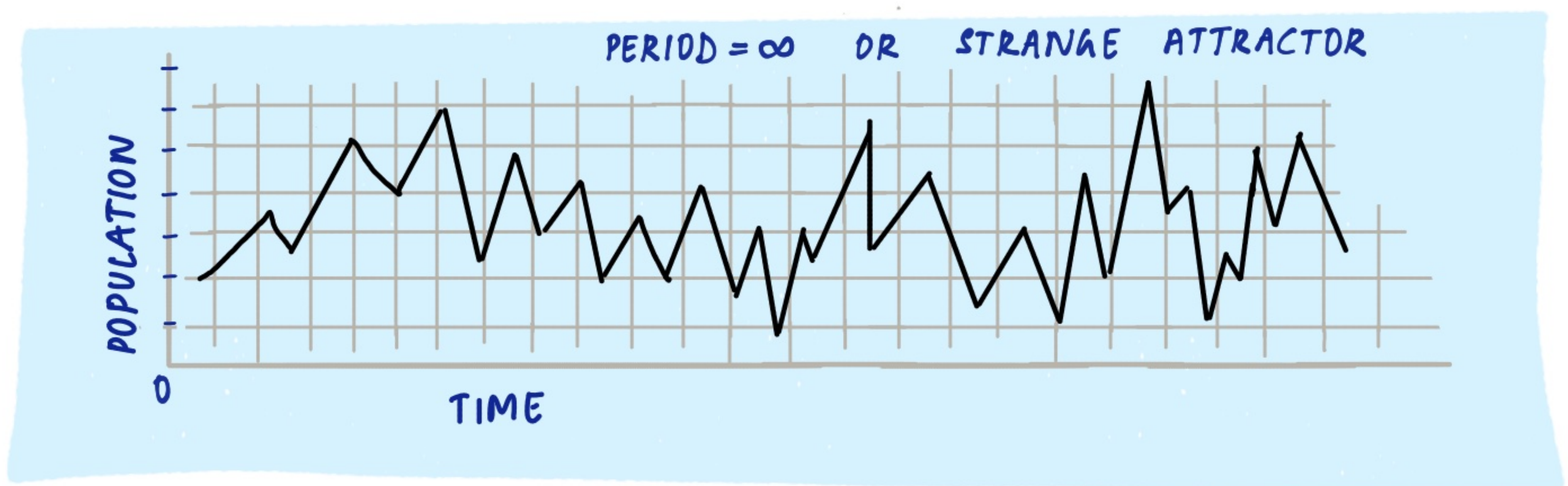
THE POPULATION OSCILLATES
BETWEEN 2 STABLE VALUES
EVERY ALTERNATE GENERATION

DETERMINISTIC CHAOS - 2

AS λ INCREASES BY FURTHER SMALL AMOUNTS, THE PERIOD GOES TO 4, 8, 16, 32 ETC.



FINALLY, AT A CERTAIN VALUE OF GROWTH RATE, CLOSE TO 4, THE POPULATION DOES NOT SEEM TO BE CYCLING THROUGH ANY PREDICTABLE SET OF VALUES AT ALL.



A RERUN OF THE POPULATION MODEL NOW WOULD VARY SIGNIFICANTLY

AN EQUATION WHICH USED TO MAKE ACCURATE PREDICTIONS IS NOW IMPOSSIBLE TO PREDICT. THIS IS CALLED DETERMINISTIC CHAOS.

UNIVERSALITY IN CHAOS

① ROUTE TO CHAOS

This period doubling route to chaos is also seen in other chaotic systems

② RATE OF PERIOD DOUBLING

The period doubles 4.669201... times faster than last time

This is the Feigenbaum Constant

INFORMATION

HELPS US BETTER UNDERSTAND SELF ORGANISATION
IN A COMPLEX SYSTEM

A HISTORY

INFORMATION THEORY HAS ITS ORIGINS IN THERMODYNAMICS, A BRANCH OF PHYSICS DEALING WITH HEAT, WORK AND MOTION

THERE ARE SOME FUNDAMENTAL LAWS OF THERMODYNAMICS

LAW 1 ENERGY IN THE UNIVERSE IS FIXED

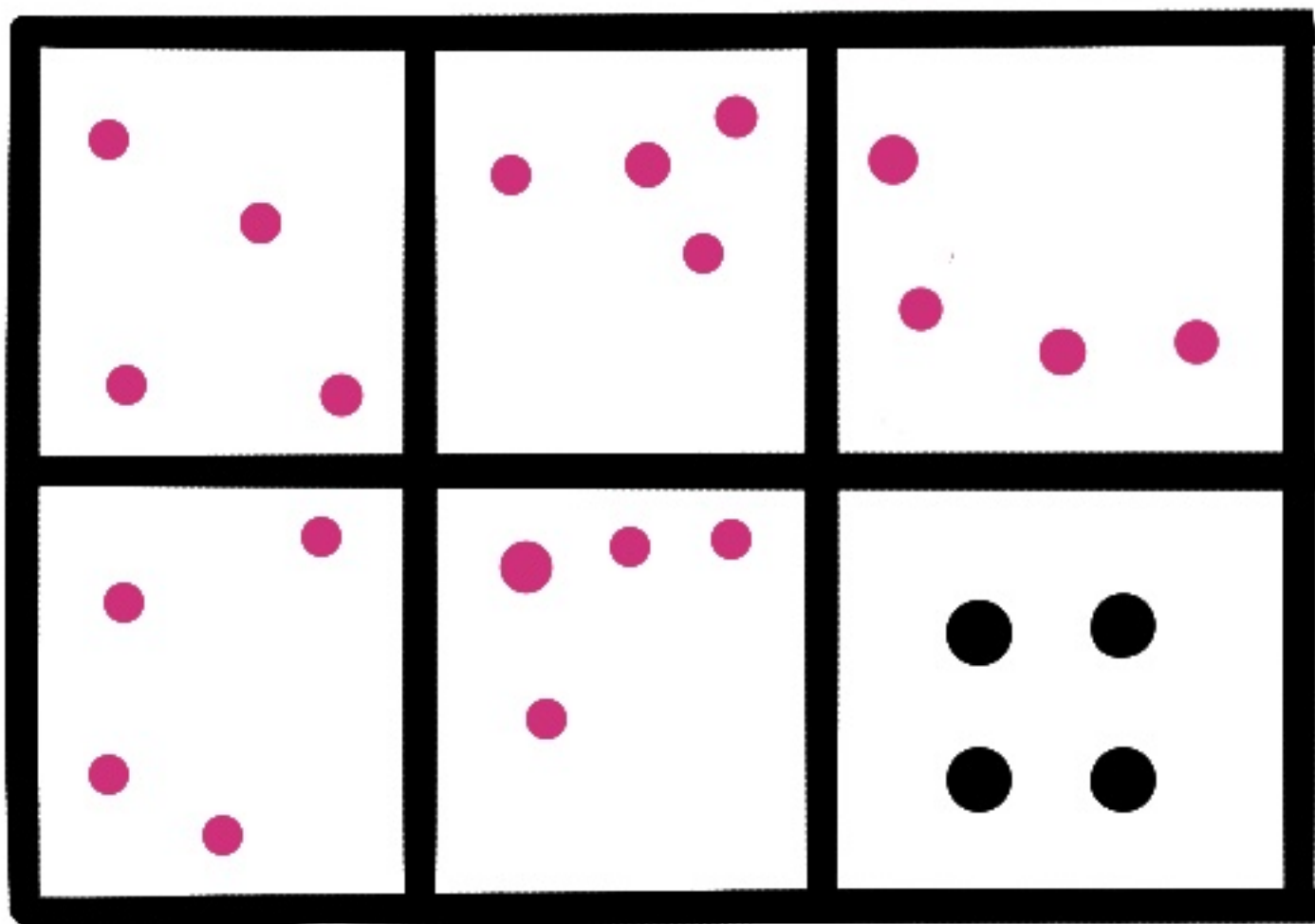
Energy cannot be created or destroyed

LAW 2 ANY UNUSABLE ENERGY INCREASES THE DISORDER OR ENTROPY OF THE UNIVERSE

Order turns to disorder unless work is done

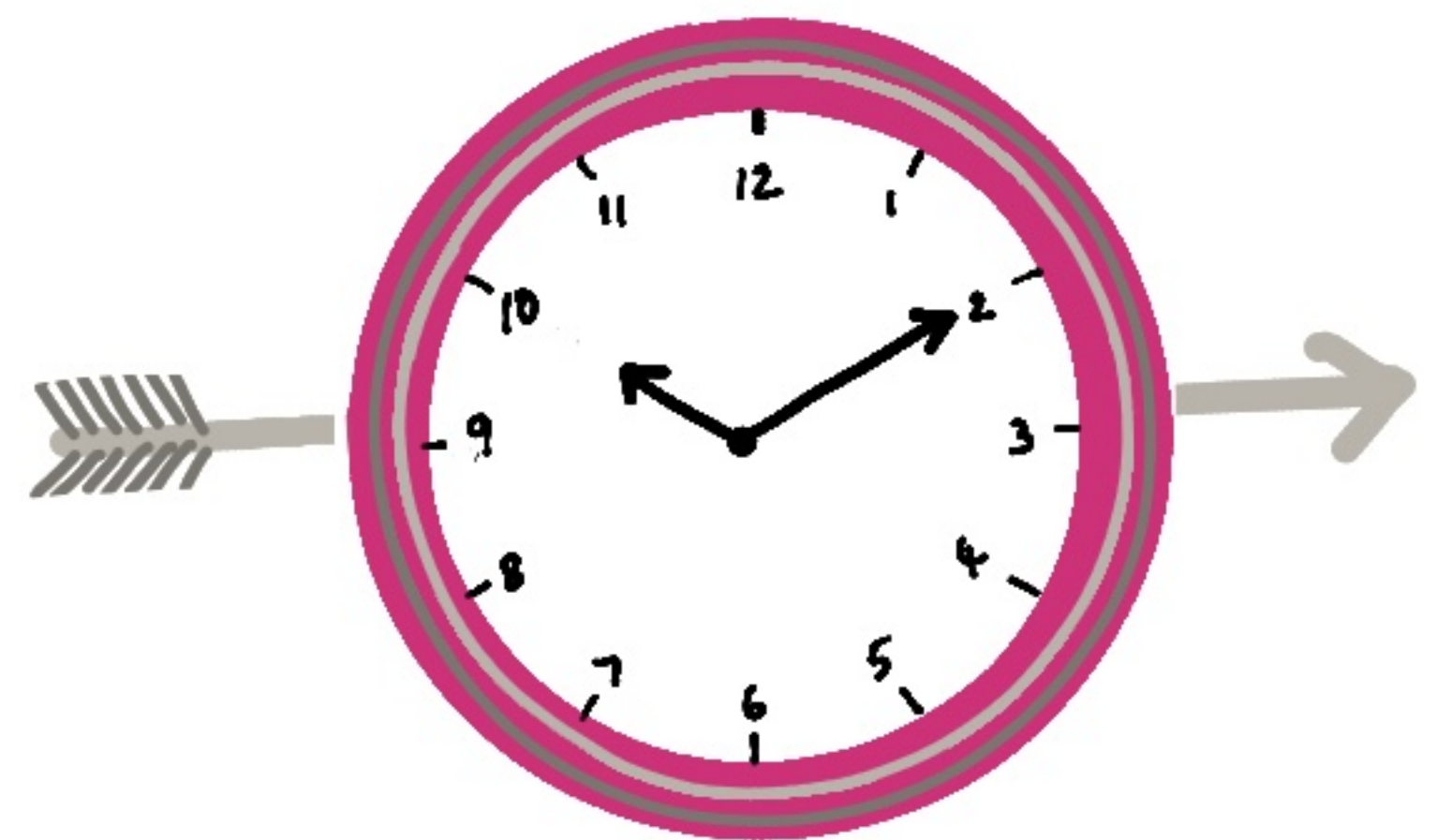
OUR FOCUS IS THE SECOND LAW WHICH IS INVIOCLABLE

ENTROPY IS CONNECTED TO PROBABILITY



THERE ARE MORE WAYS TO ACHIEVE DISORDER THAN THERE ARE TO ACHIEVE ORDER

ENTROPY TELLS US THAT TIME HAS A DIRECTION



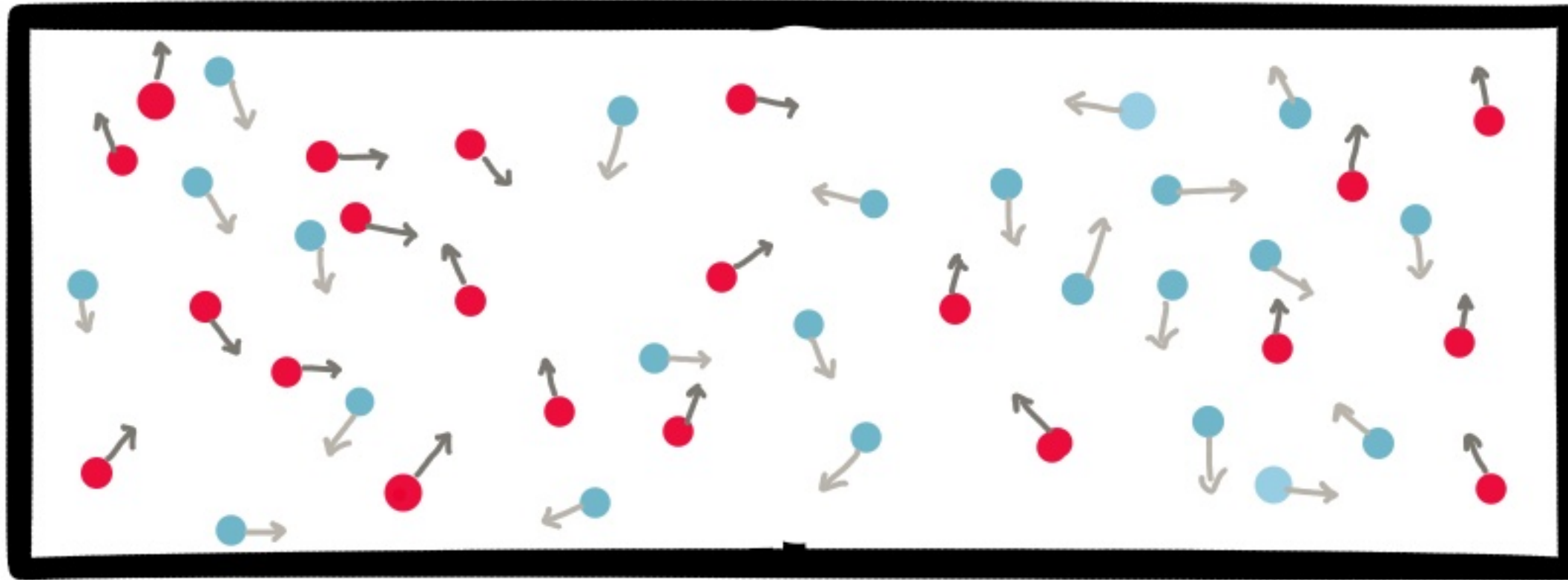
IN THE DIRECTION OF INCREASING ENTROPY

JAMES CLERK MAXWELL WONDERED IN A FAMOUS THOUGHT EXPERIMENT IN 1867 INVOLVING A DEMON, IF THE SECOND LAW COULD BE VIOLATED

MAXWELL'S DEMON

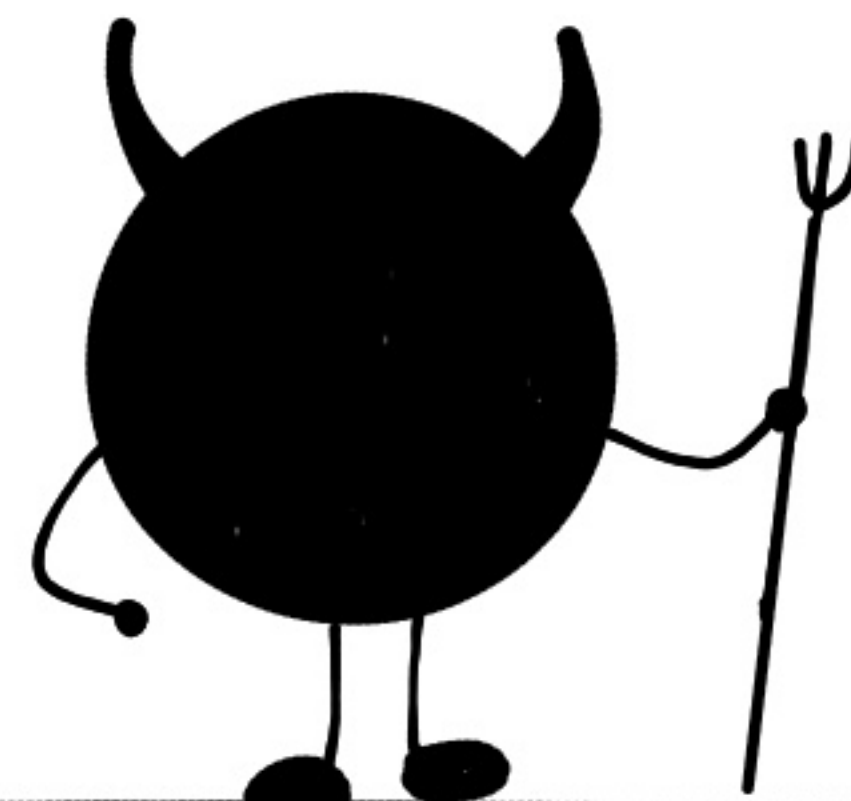
MAXWELL KNEW THAT HEAT WAS THE MOTION OF MOLECULES.

HOTTER MOLECULES MOVED FASTER AND COOLER ONES MOVED SLOWER.

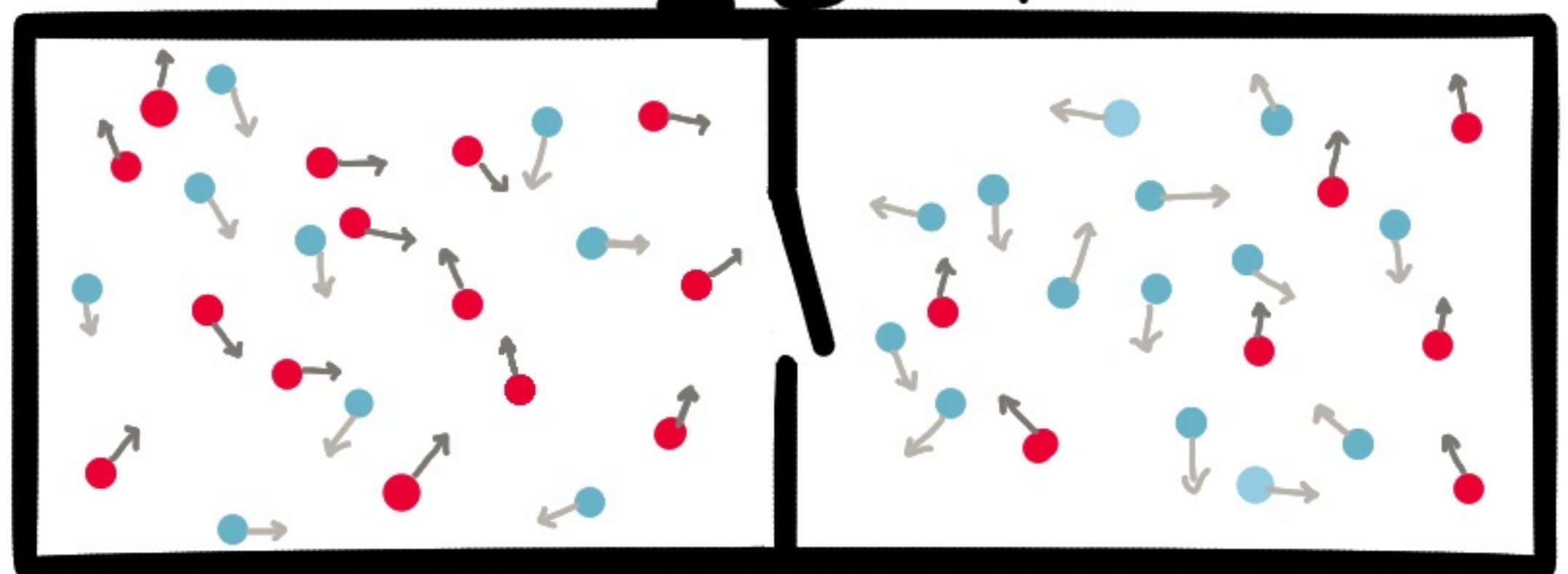


MAXWELL IMAGINED THAT IT MIGHT BE POSSIBLE TO SEPARATE THE COOL AND HOT AIR JUST WITH INFORMATION ABOUT IT

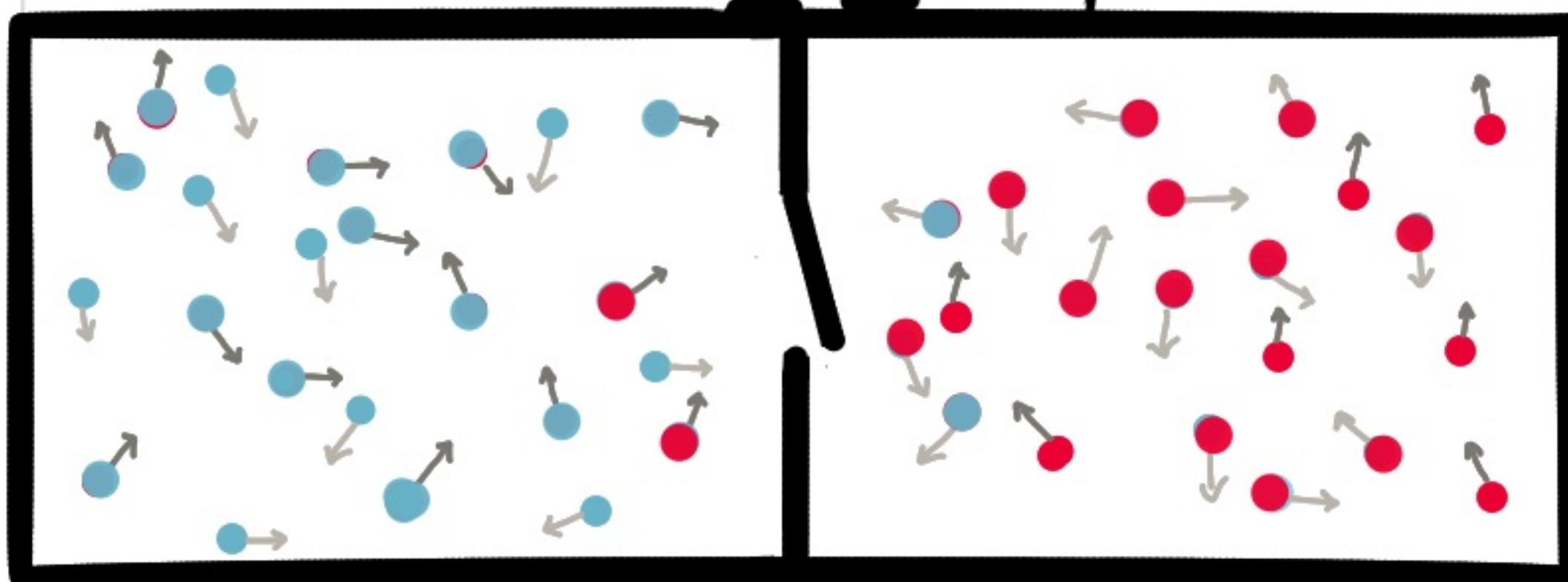
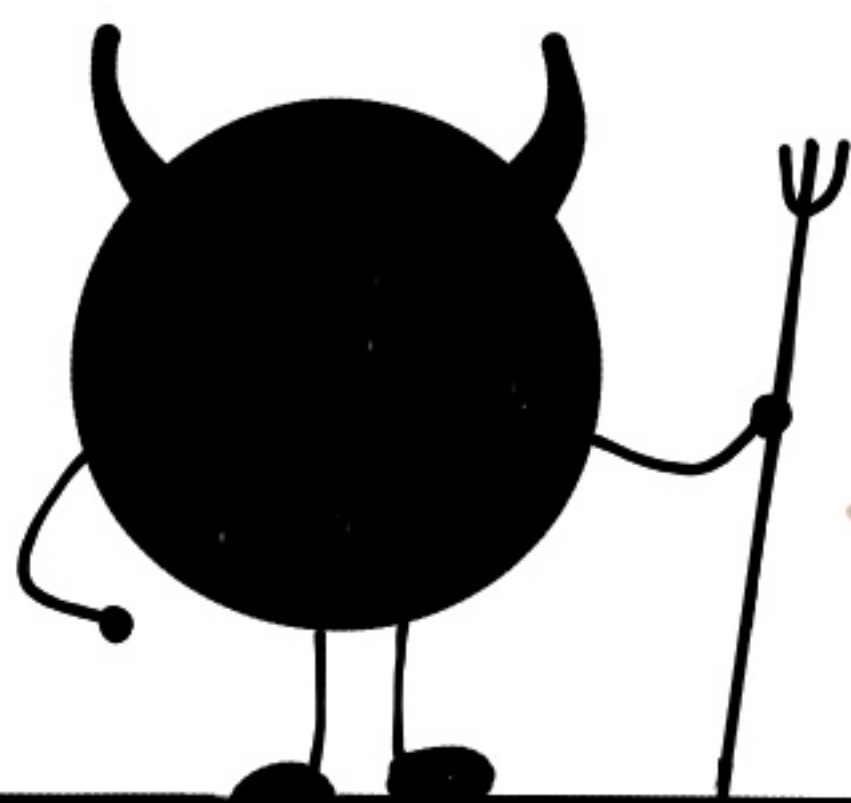
Just a friendly demon who can open a partition with negligible effort...



A DEMON IN CHARGE OF A PARTITION WOULD OBSERVE AND REMEMBER THE SPEEDS OF ALL MOLECULES



from left to right and fast may pass from right to left and slow may go



ORDER WOULD BE CREATED WITH JUST INFORMATION AND NO WORK DONE

WHAT IS INFORMATION AND DOES IT VIOLATE THE SECOND LAW?

WHAT IS INFORMATION?

AN ABSTRACT MASS- NOUN USED TO DENOTE ANY AMOUNT OF DATA, CODE OR TEXT THAT IS STORED, SENT, RECEIVED OR MANIPULATED IN ANY MEDIUM

— PLATO. STANFORD.EDU

THE RESOLUTION OF UNCERTAINTY

— WIKIPEDIA

ASIDE FROM THE SPOKEN WORD, HUMANS HAVE INVENTED MANY WAYS TO EXCHANGE INFORMATION



CLAY TABLET



PUNCH CARDS



PRINTED WORDS



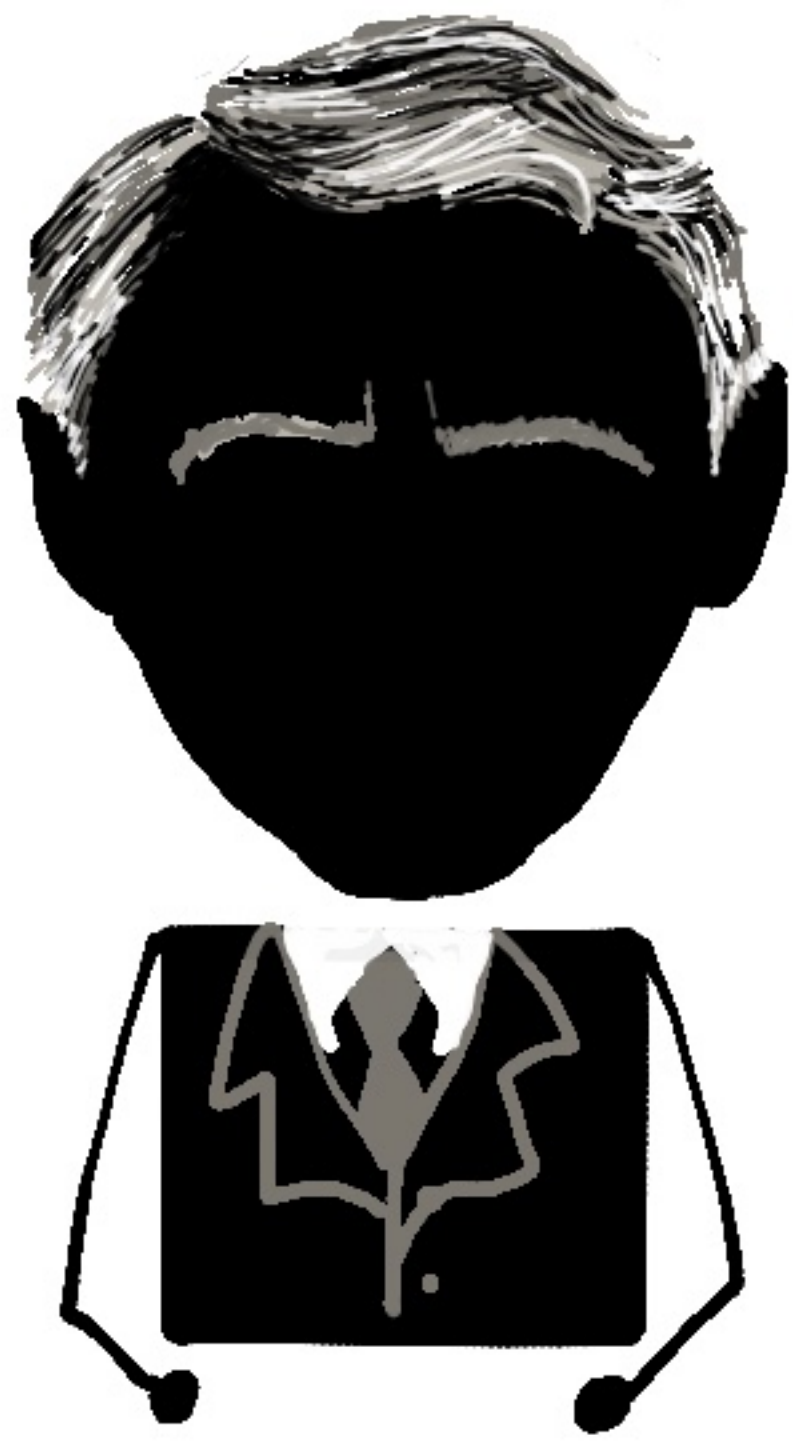
TELEGRAPH



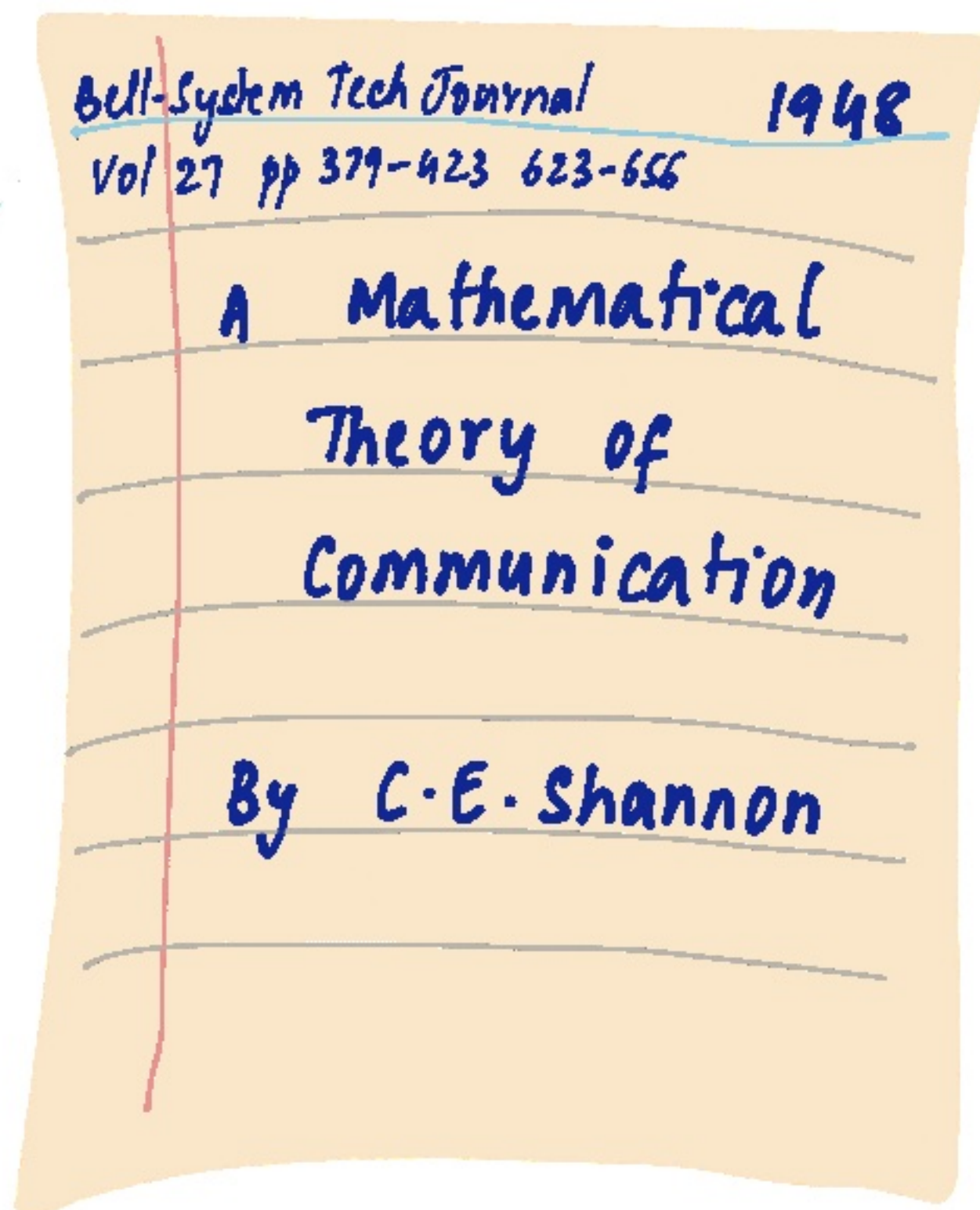
COMPUTERS

MEASURING INFORMATION

CLAUDE SHANNON, MATHEMATICIAN, WAS INTERESTED IN THE EFFICIENT TRANSFER OF SIGNALS THROUGH TELEPHONE WIRES.



CLAUDE SHANNON
BELL LABS



THROUGH THE PAPER HE WROTE, SHANNON:

INTRODUCED
THE SMALLEST UNIT
OF INFORMATION

A BIT -
SHORT FOR BINARY DIGIT

0

1

THE BIT UNDERPINS
MODERN COMPUTATION

QUANTIFIED
HOW WE CAN
MEASURE INFORMATION

SAY FOR A COIN TOSS

PROBABILITY OF $\begin{cases} \text{HEADS} = P(H) = 1/2 \\ \text{TAILS} = P(T) = 1/2 \end{cases}$

INFORMATION CONTENT:

$$= -[P(H)\log_2 P(H) + P(T)\log_2 P(T)]$$

$$= -\left[\frac{1}{2}\log_2 \frac{1}{2} + \frac{1}{2}\log_2 \frac{1}{2}\right]$$

$$= 1 \text{ bit}$$

ON INFORMATION CONTENT

INFORMATION CONTENT
IN A MESSAGE

frequency
THE ✂ **AND**
✉ **E** @ **!**

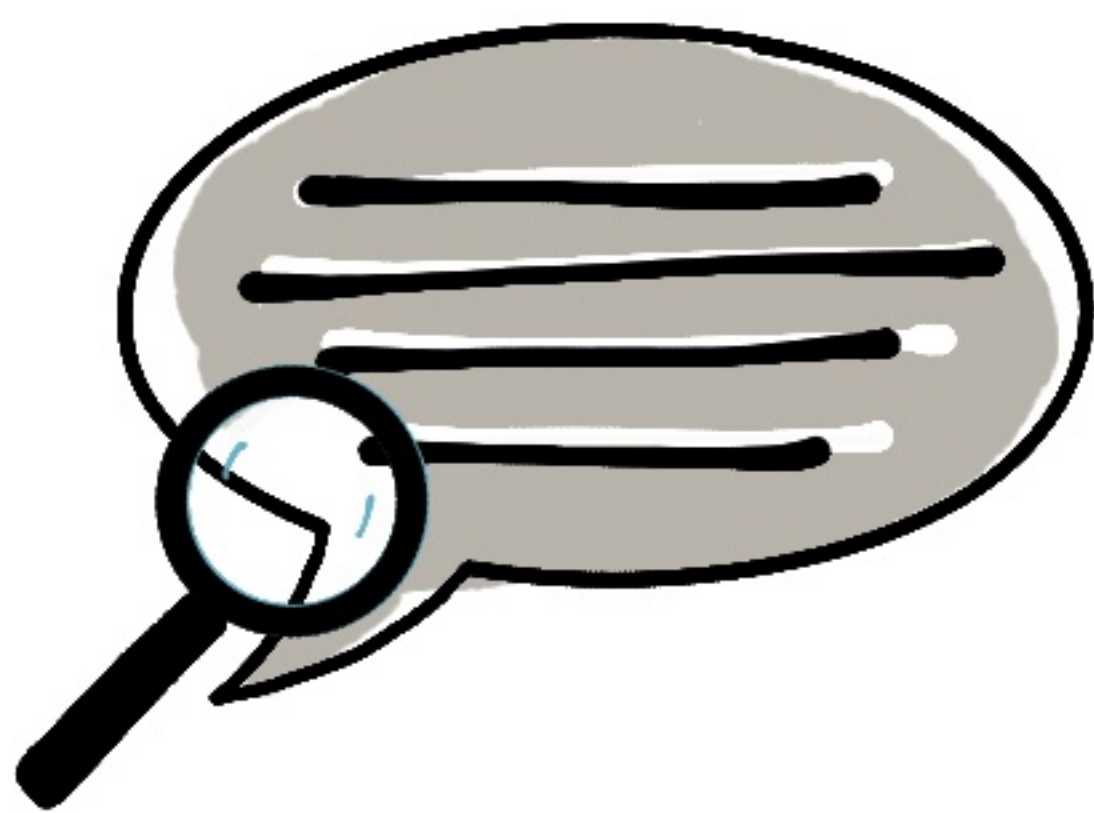
IS RELATED TO THE
PROBABILITIES OF ITS
SYMBOLS OR OUTCOMES

A MESSAGE WITH
HIGHER INFORMATION CONTENT

INFORMATION CONTENT
IS THE
OPTIMAL BITS
NEEDED TO ENCODE

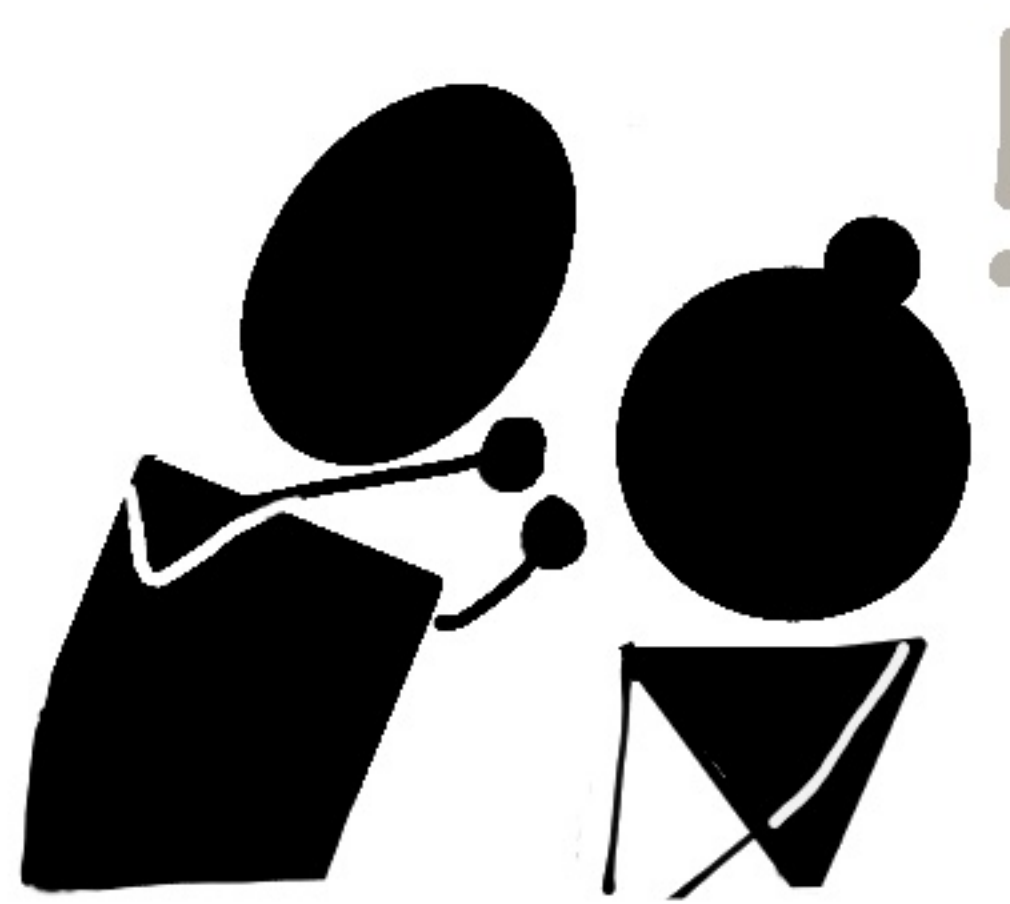
IS LESS COMPRESSIBLE

THE MEANING



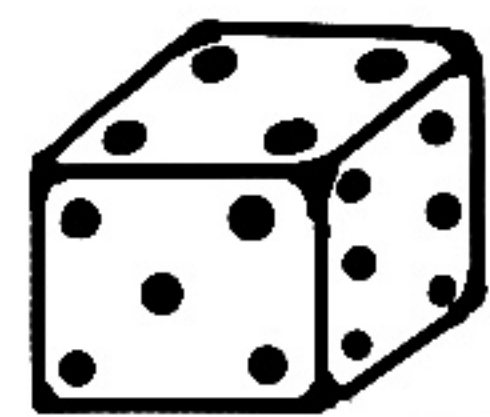
IS IRRELEVANT

THE QUANTITY
OF INFORMATION



IS ABOUT HOW
UNEXPECTED IT IS

THUS THE ROLL
OF A DIE



shannon
entropy



HAS MORE SURPRISE
THAN A COIN TOSS

WITH THIS, SHANNON HAD LAID THE FOUNDATIONS FOR A NEW BRANCH
OF STUDY CALLED INFORMATION THEORY

WHAT OF THE DEMON?

MAXWELL'S DEMON HAD TROUBLED SCIENTISTS FOR NEARLY A CENTURY

THERE NOW SEEMED TO BE A
VALID EXPLANATION THAT MAXWELL'S
DEMON DID NOT VIOLATE THE SECOND
LAW OF THERMODYNAMICS

LEO SZILARD

LÉON BRILLOUIN

ROLF LANDAUER

CHARLES BENNETT

IN THEORY:

THERE IS A METHOD TO	AND NOT CHANGE ENTROPY
DETECT MOLECULE VELOCITIES	✓
OPEN PARTITIONS	✓
STORE INFORMATION	✗
ERASE INFORMATION	✗

THE DEMON LEARNS ABOUT THE
HOT AND COOL AIR MOLECULES

THE KNOWLEDGE ALTERS THE
STATE OF ITS MEMORY

THE DEMON REDUCES
DISORDER IN THE BOX

ITS OWN MEMORY HAS
NOW INCREASED ENTROPY

ERASING OR RESETTNG
MEMORY RELEASES ENTROPY

All information needs
to be carried by a
physical 'thing'...

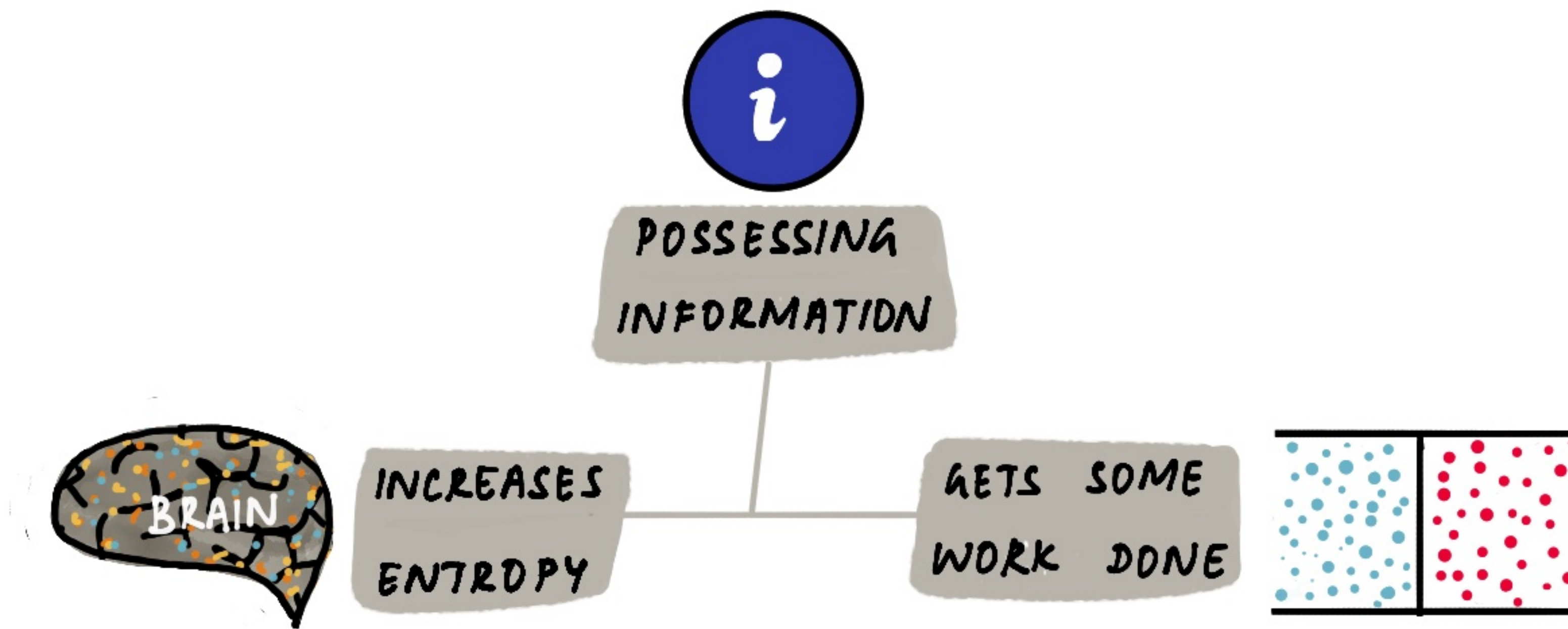


...A thought, a book,
sounds or pictures..



INFORMATION & COMPLEXITY

THE EXPLANATION TO MAXWELL'S THOUGHT EXPERIMENT SHOWS US
THE PROFOUND LINK BETWEEN ENTROPY AND INFORMATION



INFORMATION IS PART OF THE PHYSICAL
WORLD AND IT OBEYS THE LAWS OF PHYSICS
JUST LIKE EVERYTHING ELSE

— JIM AL-KHALILI

INFORMATION IS AS KEY TO COMPLEXITY
AS ENERGY IS TO PHYSICS

— JIM CRUTCHFIELD

THE NEW AREAS OF RESEARCH

- BUILD ON SHANNON INFORMATION
- INVESTIGATE OTHER KINDS OF INFORMATION
- INFORMATION PROCESSING IN NATURAL SYSTEMS

COMPUTATION

THE IDEA THAT COMPLEX SYSTEMS CAN
FIND AND CONSUME INFORMATION

WHAT IS COMPUTATION?

A COMPUTATION IS A PROCESS THAT OBEYS
FINITELY DESCRIBABLE RULES

- RUDY RUCKER

COMPUTATION IS WHAT A COMPLEX SYSTEM DOES WITH
INFORMATION TO SUCCEED/ADAPT IN ITS ENVIRONMENT

- MELANIE MITCHELL

ALL PHYSICAL SYSTEMS CAN BE THOUGHT OF AS
REGISTERING AND PROCESSING INFORMATION.

HOW ONE WISHES TO DEFINE COMPUTATION WILL DETERMINE
YOUR VIEW OF WHAT COMPUTATION CONSISTS OF

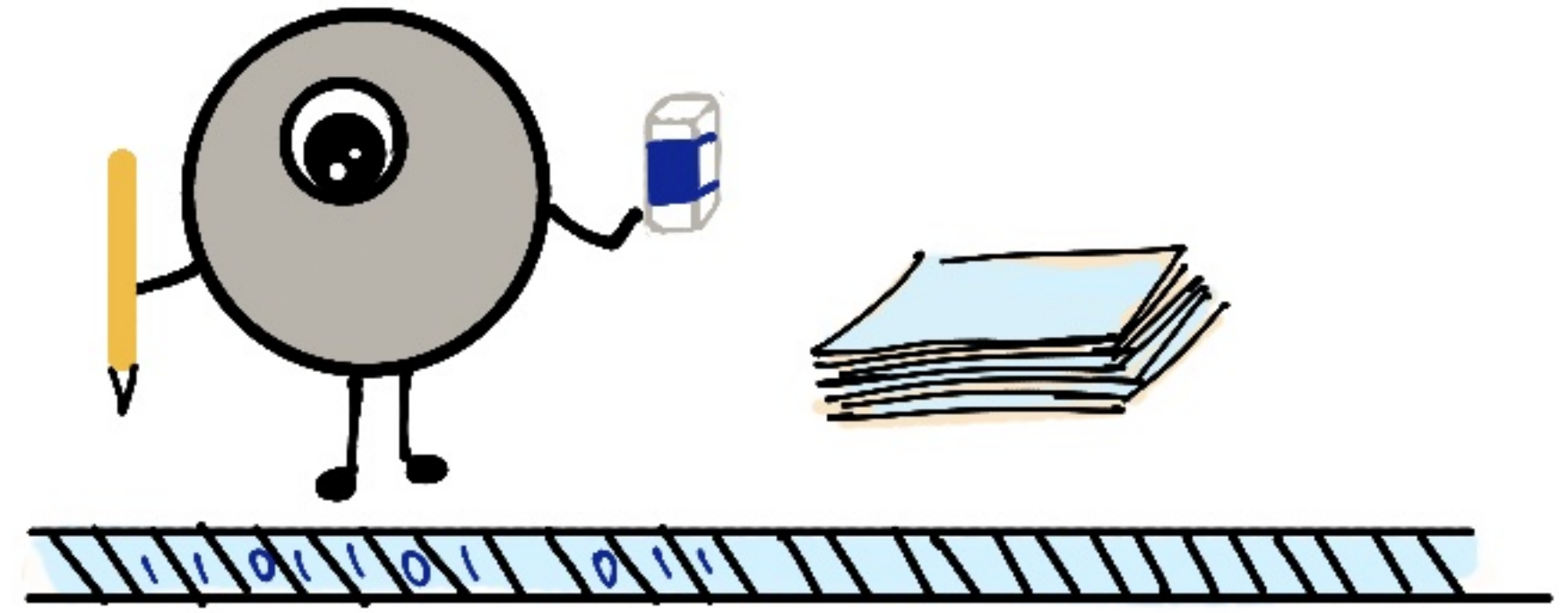
- SETH LLOYD

THE PURPOSE OF COMPUTATION IS INSIGHT,
NOT NUMBERS

- RICHARD HAMMING

IDEAS IN COMPUTATION

WE ARE FAMILIAR WITH
THE IDEA THAT COMPUTATION
IS THE STEPS CARRIED OUT
BY A TURING MACHINE.



FROM THIS MODEL OF COMPUTATION STEMMED THE IDEA OF
COMPUTATIONAL COMPLEXITY - THE RESOURCES NEEDED TO RUN A PROGRAM

Read 'The Story of Quantum Computing' from thoughtworks.com for more detail

ANOTHER POIGNANT IDEA THAT CAME ABOUT WAS THE CONCLUSION
OF THE DECIDABILITY PROBLEM

IS THERE A TURING MACHINE
TO DECIDE IF A TURING MACHINE
WOULD HALT OR RUN FOREVER?

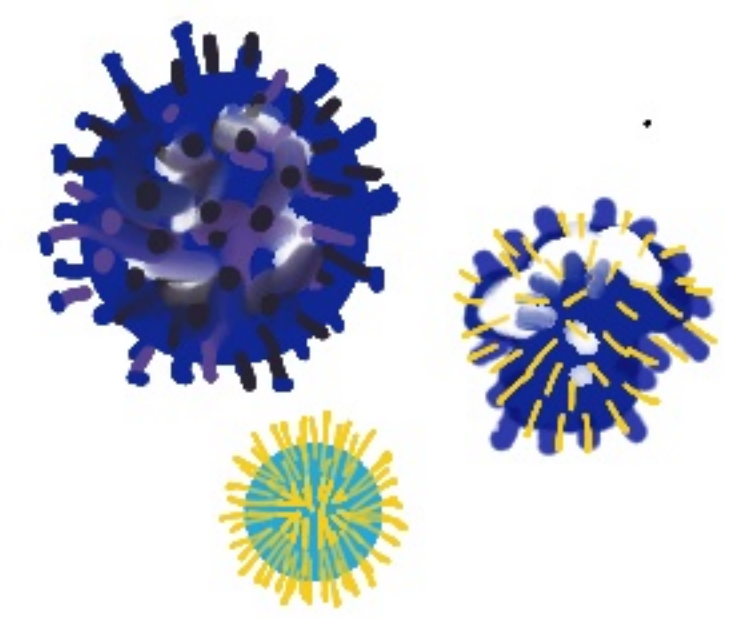
IN SHORT, THE ANSWER TO THE DECIDABILITY PROBLEM IS NO, LEAVING US
TO CONCLUDE THAT THERE ARE SOME ANSWERS WE CAN NEVER COMPUTE

Read 'A Tribute to Turing' from thoughtworks.com for more detail

PROCESSES IN NATURE
CAN ALSO BE THOUGHT
OF AS COMPUTATION



NUTRIENTS TRANSPORT
SYSTEM IN PLANTS

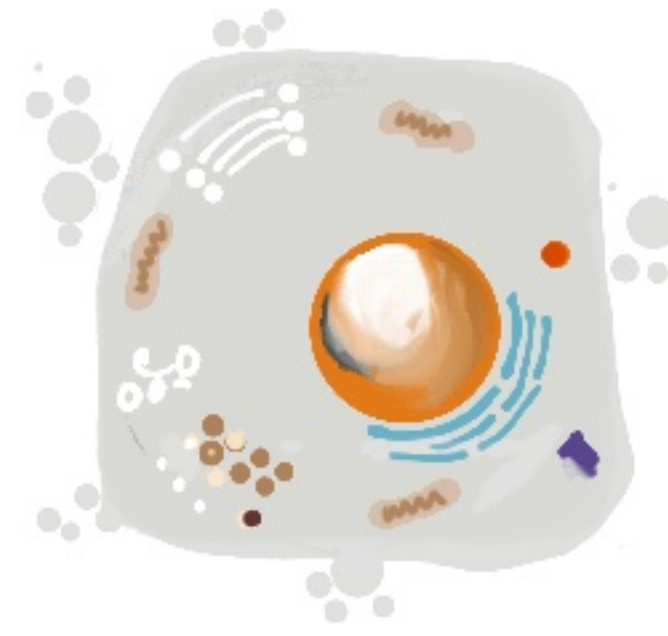


HUMAN
IMMUNE SYSTEM

WHAT DOES NATURE COMPUTE?

CELLS HAVE THE ABILITY TO STORE AND PROCESS INFORMATION AND IN THIS RESPECT, CELLS AND COMPUTERS ARE OFTEN COMPARED.

THE LIVING BEING, BE IT A CELL OR ANT, HAS RECEPTORS

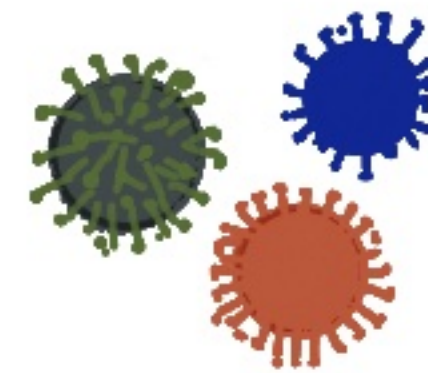


CELL



ANT

IT CAN SENSE THE ENVIRONMENT WITH THIS



PATHOGENS



FOOD

WHEN THE RECEPTOR ENCOUNTERS AN INTERESTING OBJECT, IT EMITS A SIGNAL



CYTOKINES



PEROMONES

THE OTHER LIVING BEINGS IN THE VICINITY SENSE THE SIGNAL AND REACT TO IT

PRODUCTION OF
MORE CELLS TO
FIHT
INTRUDERS

SCENT TRAIL
GATHERS A
LARGE GROUP
OF ANTS

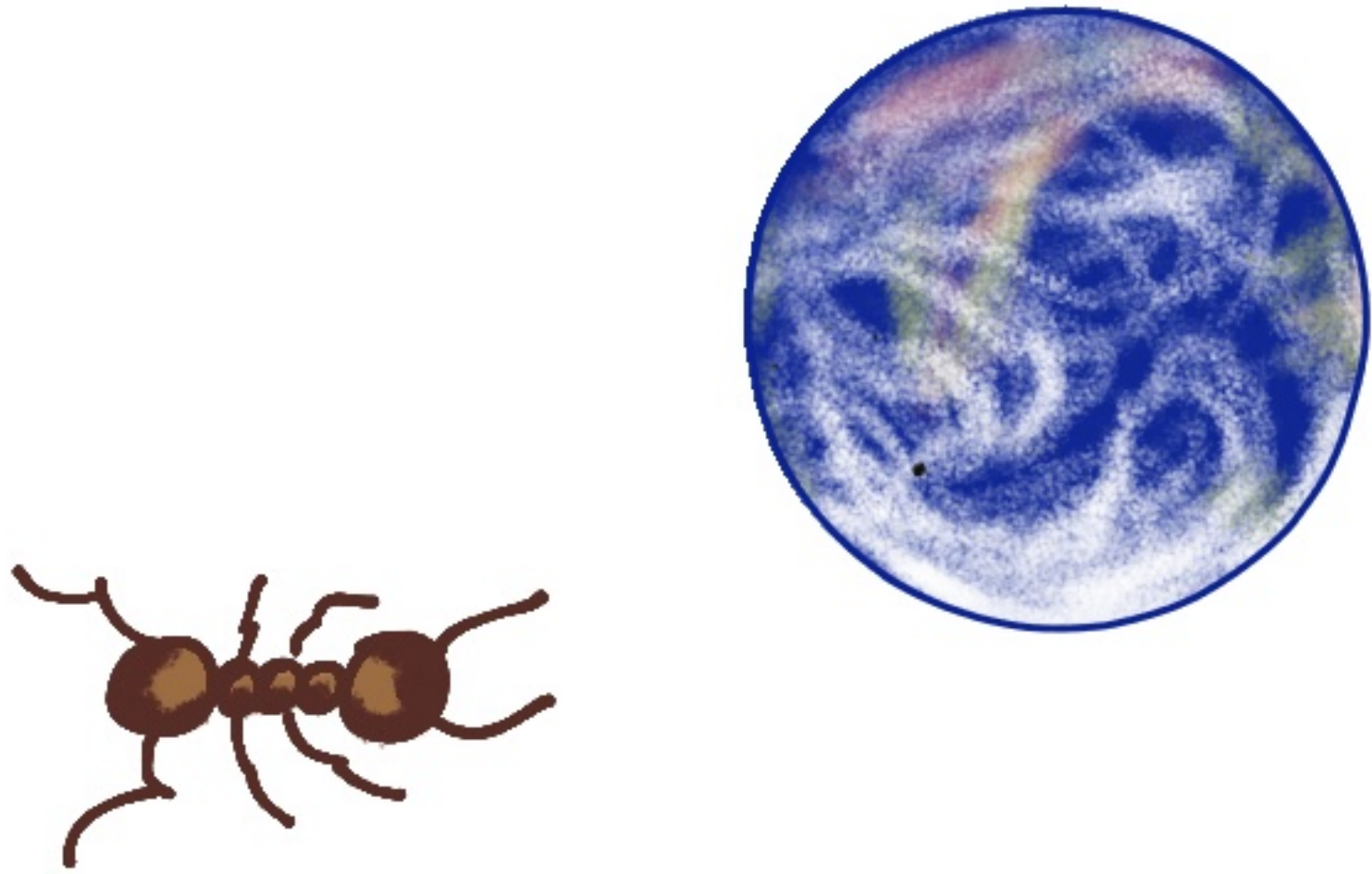
THE INFORMATION IS THE DISTRIBUTION OR CONCENTRATION OF

WHITE BLOOD
CELLS

ANTS IN
THE TRAIL

PROCESSING INFORMATION

THE INDIVIDUAL IS TOO SMALL TO UNDERSTAND THE WHOLE SYSTEM



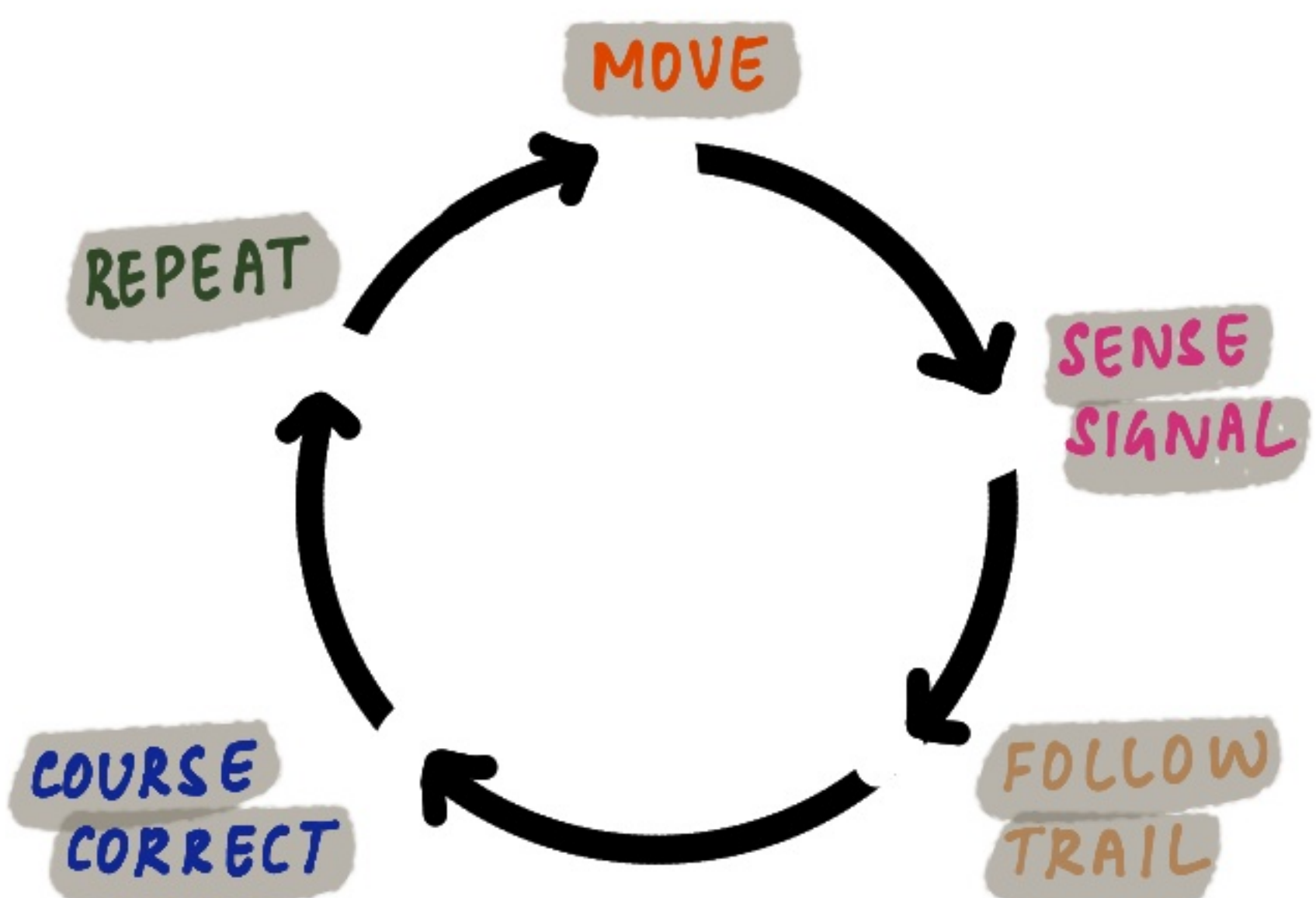
SO IT TAKES IN RANDOM SAMPLES



SAMPLING BECOMES LESS RANDOM AS SIGNALS GET MORE FREQUENT



THE INFORMATION CAN BE THOUGHT OF AS FEEDBACK LOOPS



FEEDBACK LOOPS ACT LIKE A THERMOSTAT

NEGATIVE FEEDBACK

POSITIVE FEEDBACK



FEEDBACK LOOPS RECIRCULATE SIGNALS & RESOURCES



MEANING OF INFORMATION

EXPLORING THE NOTION OF

THE MEANING OF INFORMATION

IS ALSO AN EXPLORATION

OF CONSCIOUSNESS

OR THE SELF

TO WHO INFORMATION

MUST MAKE SENSE

THIS TOPIC IS BEYOND THE SCOPE OF THIS BOOK.



EVOLUTION

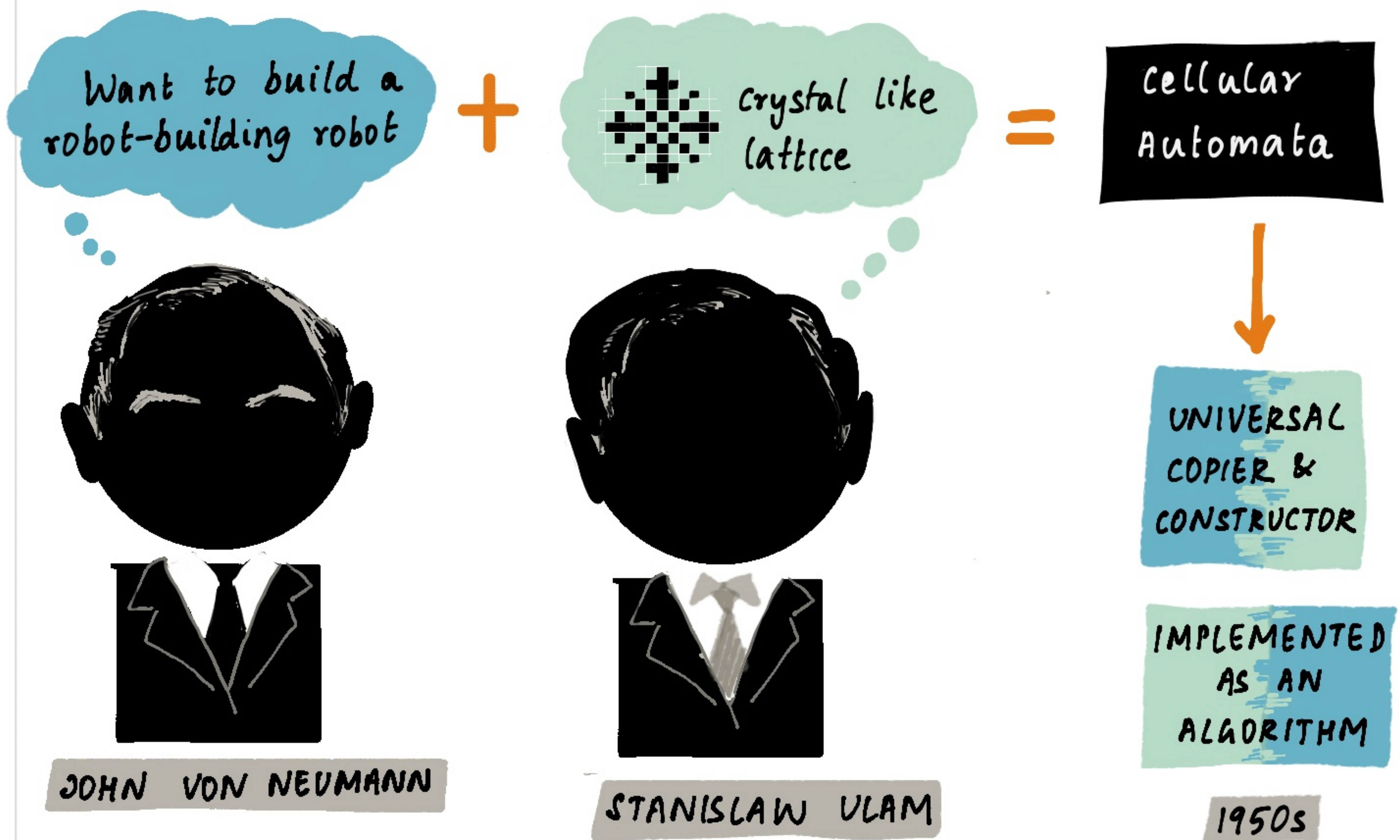
THE ABILITY OF A SYSTEM TO LEARN, GROW,
ADAPT AND THRIVE IN A CHANGING ENVIRONMENT

A NEW CAPABILITY

IN THE 1950s, STARTING FROM ALAN TURING, MANY PEOPLE WONDERED ABOUT THE CONNECTION BETWEEN MIND AND MACHINE

CAN BIOLOGICAL PROCESSES BE TRANSLATED INTO A MECHANISTIC ONE?

THE AIM, AS IT HAS BEEN FOR CENTURIES ACROSS MANY CIVILISATIONS, WAS TO CREATE A SELF OPERATING MACHINE – OR AUTOMATON.



whether self-reproduction is enough to call a machine or program alive or conscious is a topic for a whole other book

THE NEXT QUESTION: CAN THE PROGRAM LEARN AND EVOLVE IN AN ENVIRONMENT?

EVOLUTION

EVOLUTION IS THE CHANGE IN CHARACTERISTICS OF A POPULATION OVER TIME. THE CHARACTERISTICS THAT GIVE AN INDIVIDUAL SOME ADVANTAGE ARE PASSED ON THROUGH THE PROCESS OF NATURAL SELECTION TO THE NEXT GENERATIONS

NATURAL EVOLUTION: A REMINDER

Charles Darwin's theory of evolution by natural selection:

- Individuals have large variations for a characteristic
- Those most suited to the environment are more likely to survive and breed
- The characteristics that helped survival will be passed on to the next generation

← Variation

← Survival of the fittest

← Heredity + random mutations

THE BEST BEAK FOR THE JOB IS:



EVOLUTIONARY COMPUTATION

EVOLUTION IN COMPUTATION DRAWS IDEAS FROM EVOLUTION IN NATURE

IT USES SIMILAR CONCEPTS SUCH AS SELECTION, REPRODUCTION, Crossover AND MUTATION TO EVOLVE NEW 'GENERATIONS' FROM RANDOMLY CHOSEN POSSIBLE SOLUTIONS.

PIONEERS IN THE FIELD

DAVID FOGEL

JOHN H HOLLAND *came up with*

INGO RECHENBERG

HANS-PAUL SCHWEFEL

TECHNIQUES

EVOLUTIONARY ALGORITHMS

GENETIC ALGORITHMS

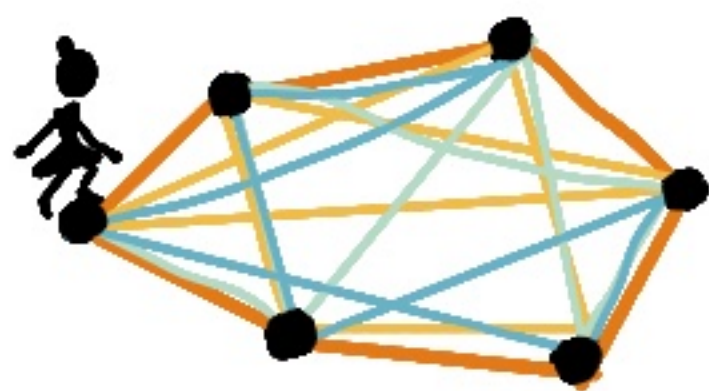
GENETIC PROGRAMMING

GRAMMATICAL EVOLUTION

SUITABLE TO

- EXPLORE A LARGE SEARCH SPACE
- SOLVE OPTIMISATION PROBLEMS

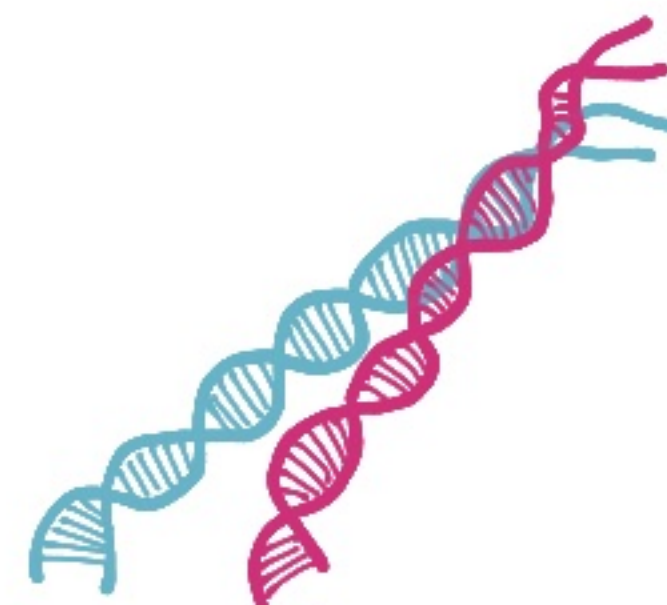
SOME APPLICATIONS



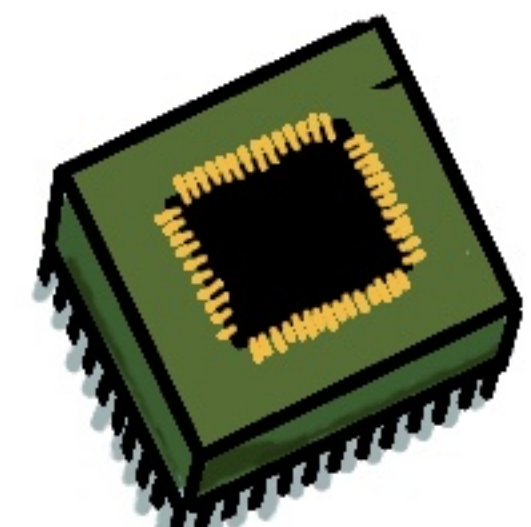
TRAVELLING
SALESPERSON
PROBLEMS



GAME
PLAYING



DNA/GENE
ANALYSIS



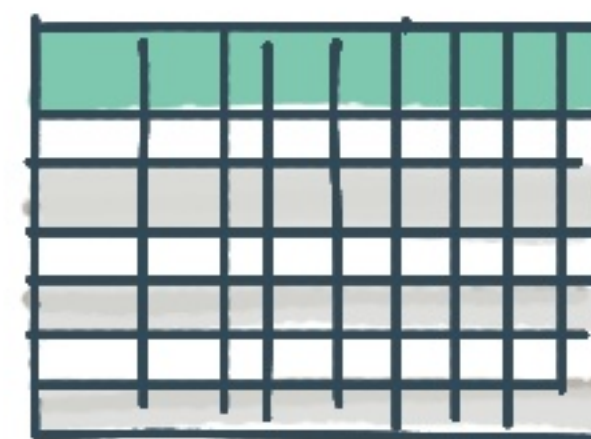
HARDWARE
DESIGN



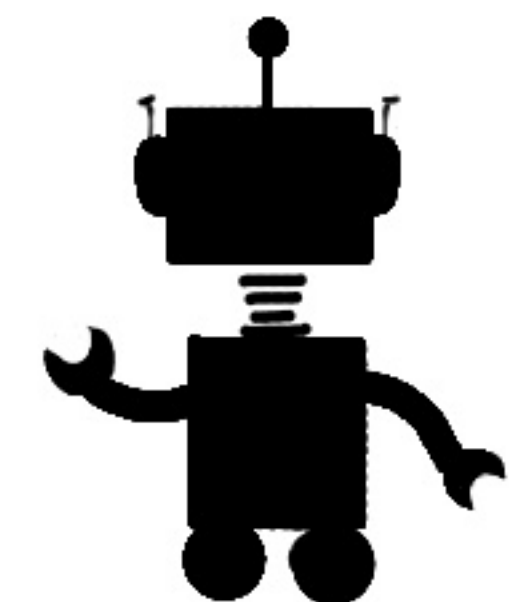
ENCRYPTION
CODE BREAKING



MACHINE LEARNING



SCHEDULING



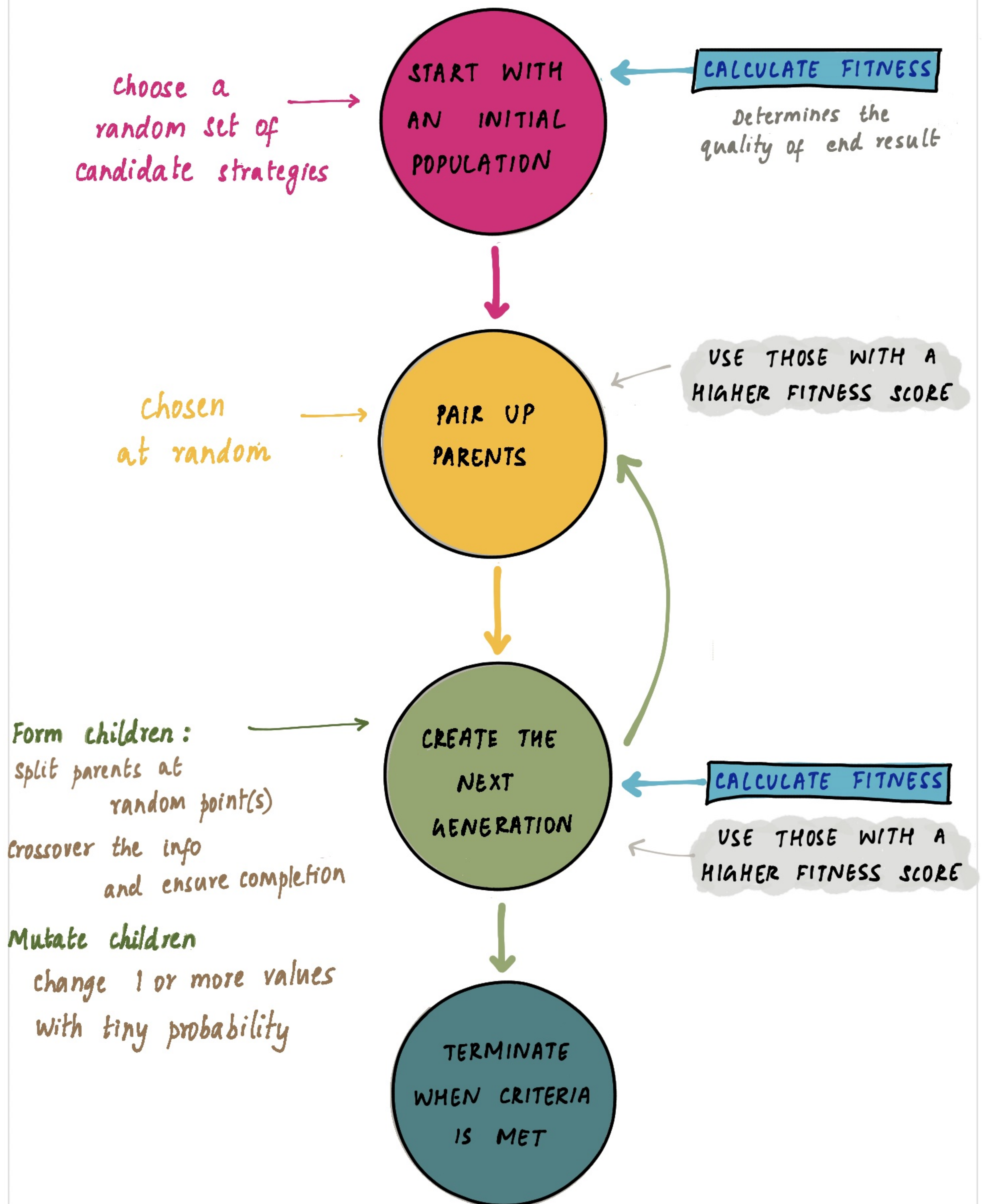
ROBOTICS

THIS IS NOW A SUB-FIELD IN ARTIFICIAL INTELLIGENCE AS WELL.

LET US NOW LOOK AT GENETIC ALGORITHMS - A WELL KNOWN TECHNIQUE

GENETIC ALGORITHMS

HERE IS A PATTERN OF HOW THEY WORK



EXAMPLE: ROUTE PLANNING

PROBLEM FIND THE SHORTEST ROUTE BETWEEN A SET OF CAKE SHOPS WHERE YOU VISIT EVERY CAKE SHOP ONLY ONCE.



INITIAL POPULATION

SOME POSSIBLE ROUTES

A B C D E F G — 1
A C G B D F E — 2
B F A E G C D — 3
G D A C B E F — 4
F A E G B D C — 5
C G E B A D C — 6

FITNESS CALCULATION

THIS WILL BE THE TOTAL TIME FROM START TO END FOR EACH ROUTE.

PAIR UP PARENTS

PAIRING COULD BE RANDOM

1-Parent 1 — A B C D E F G
4-Parent 2 — G D A C B E F

CREATE NEXT GENERATION

PAIRING ① AND ④ GIVE

Parent 1	A B	C D E	F G
Parent 2	G D	A C B	E F

CROSSOVER - SWAP AT POINTS OF SPLIT

child 1	— —	A C B	— —
child 2	— —	C D E	— —

FILL NON-DUPLICATE INFO OF ORIGINAL

child 1	— —	A C B	F G
child 2	G —	C D E	— F

ENSURE CHILD INFO IS COMPLETE

child 1	D E	A C B	F G
child 2	G B	C D E	A F

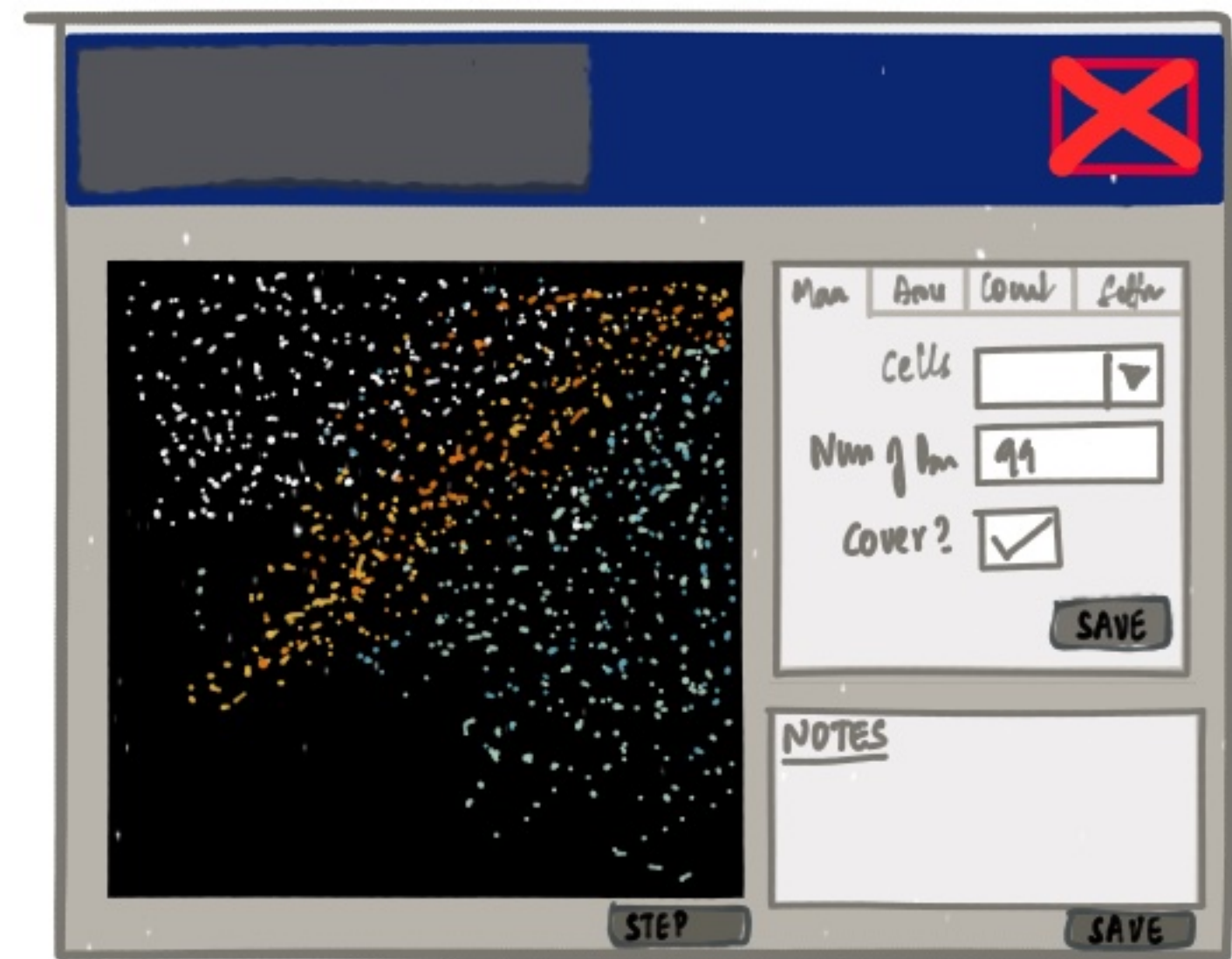
TERMINATE

DEFINE CRITERIA FOR POPULATION SIZE, FITNESS SCORE ETC

SIMULATING COMPLEX SYSTEMS

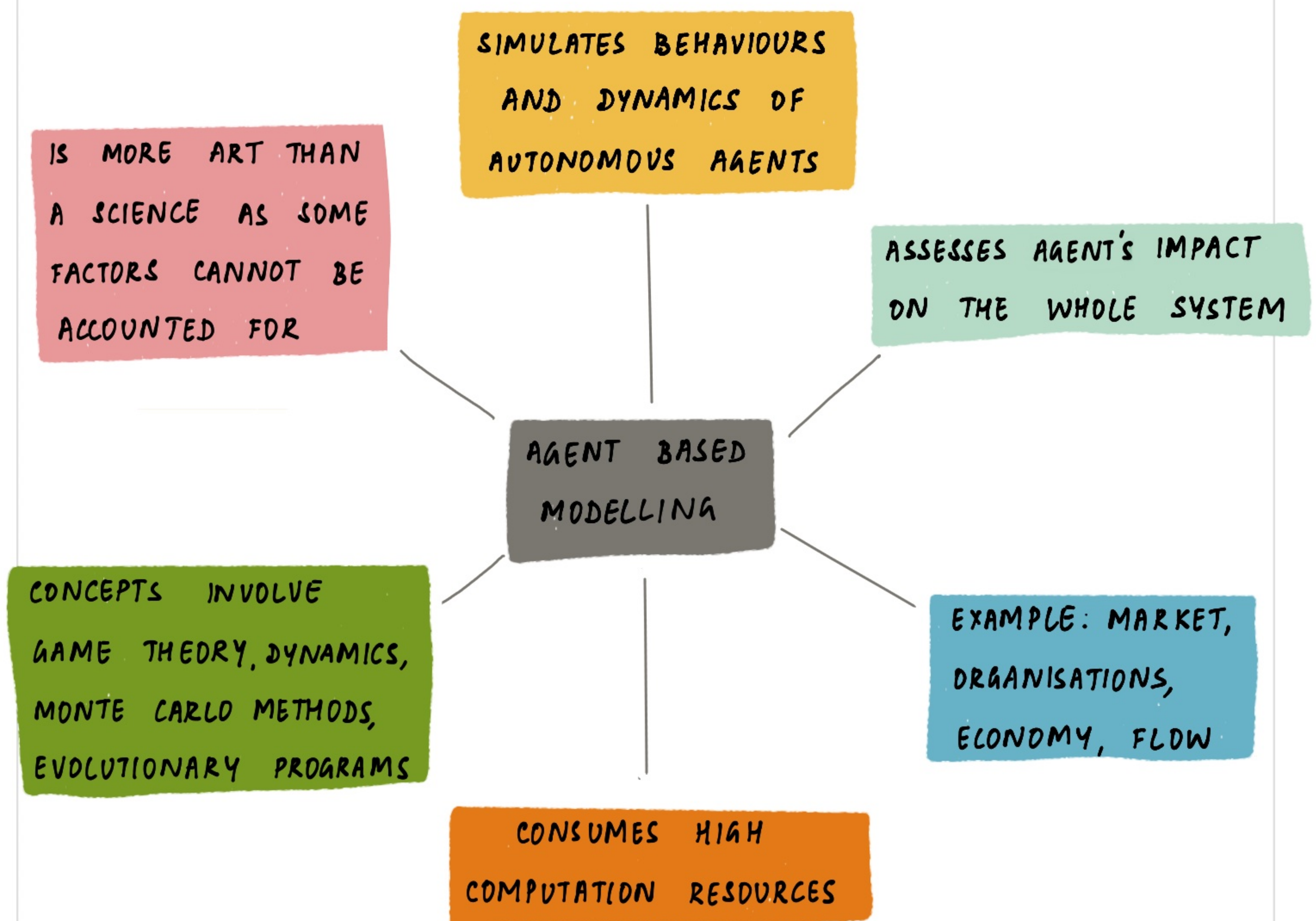
AS WITH OTHER SCIENCES,
COMPLEX SYSTEMS ALSO RELY ON
MAKING REPRESENTATIONS OF
VARIOUS CONCEPTS IN CODE.

THESE ARE CALLED MODELS.



THE RESULTS WHICH CAN BE REPLICATED ARE MORE USEFUL AND
CAN BE BETTER UTILISED TO CHECK INFERENCES OF THE RESULTS.

AN EXAMPLE OF A METHOD OF SIMULATION

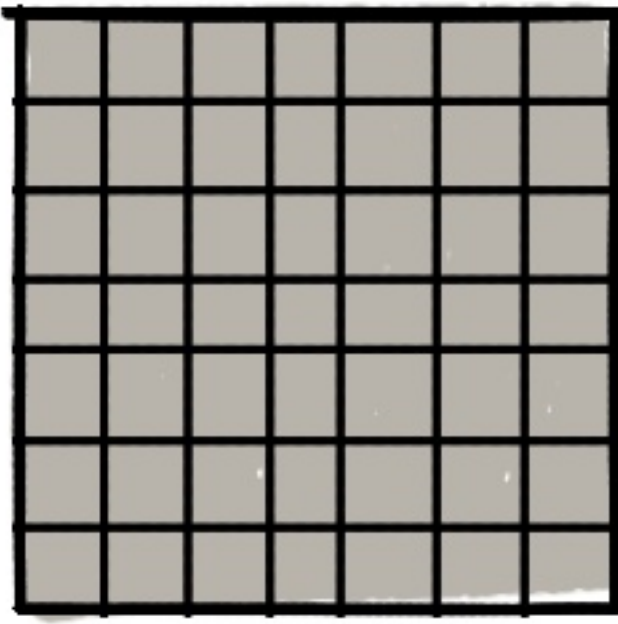


CELLULAR AUTOMATA

A COMMONLY USED MODELLING TOOL IN COMPLEX SYSTEMS

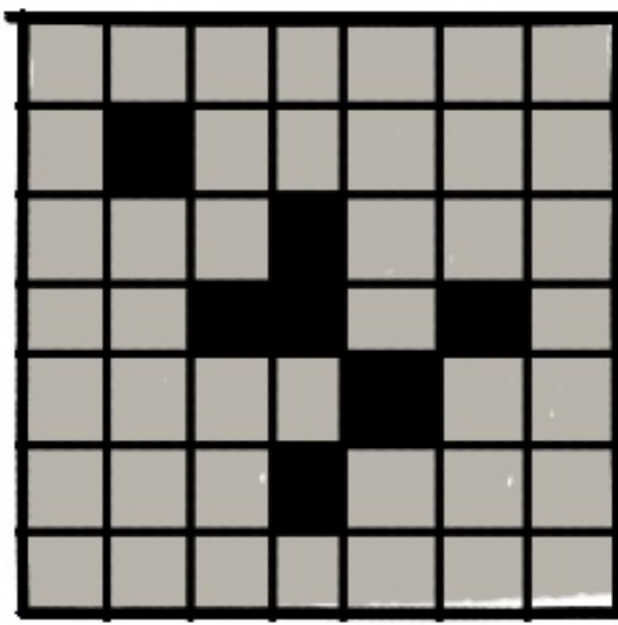
CELLULAR AUTOMATA - CA

CELLULAR AUTOMATA (AUTOMATON-SINGULAR FORM) ARE COMPLEX SYSTEMS WHERE TIME AND SPACE ARE DISCRETE.



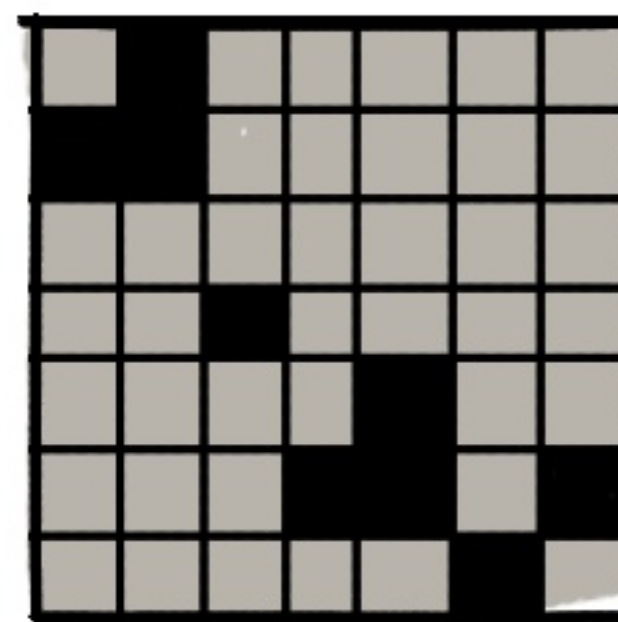
A CELLULAR AUTOMATON
CONSISTS OF A GRID OF CELLS

one, two
or more
dimensions

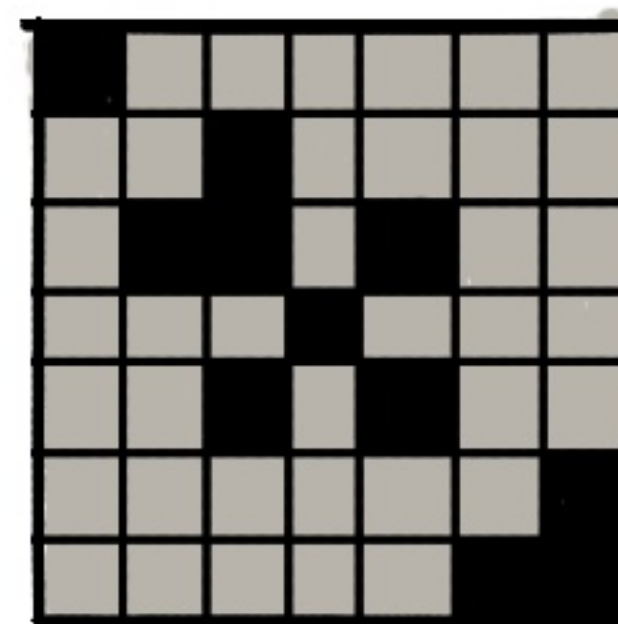


EACH CELL IS IN A STATE
OUT OF MANY POSSIBLE STATES.
HERE, ON OR OFF

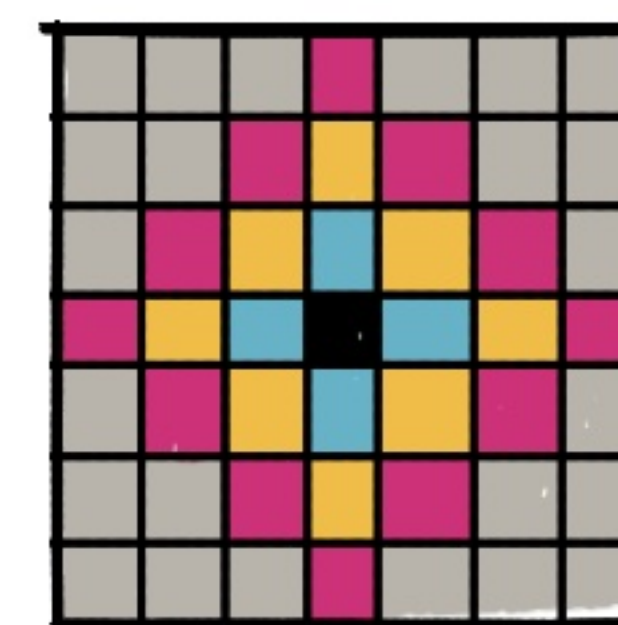
two
or more
states



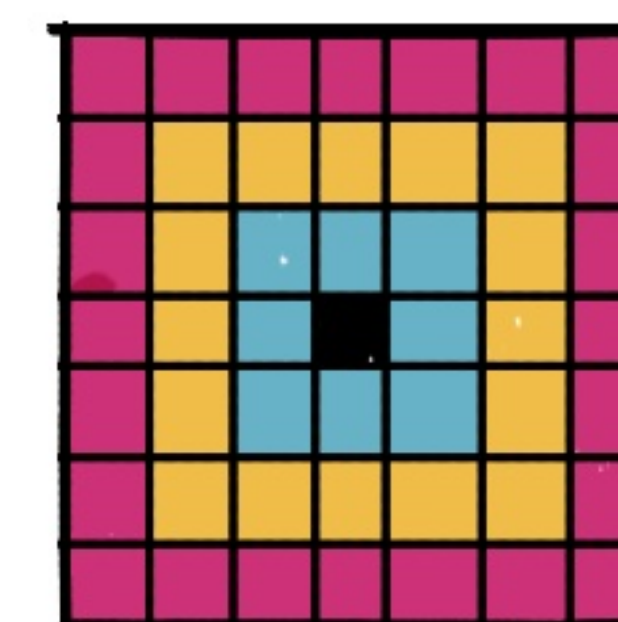
THE STATE OF EACH CELL EVOLVES
CONTINUOUSLY DEPENDING ON RULES



USUALLY, THE RULES ARE BASED ON
THE STATES OF NEIGHBOURING CELLS.



THIS IS THE VON NEUMANN
NEIGHBOURHOOD FOR THE BLACK CELL



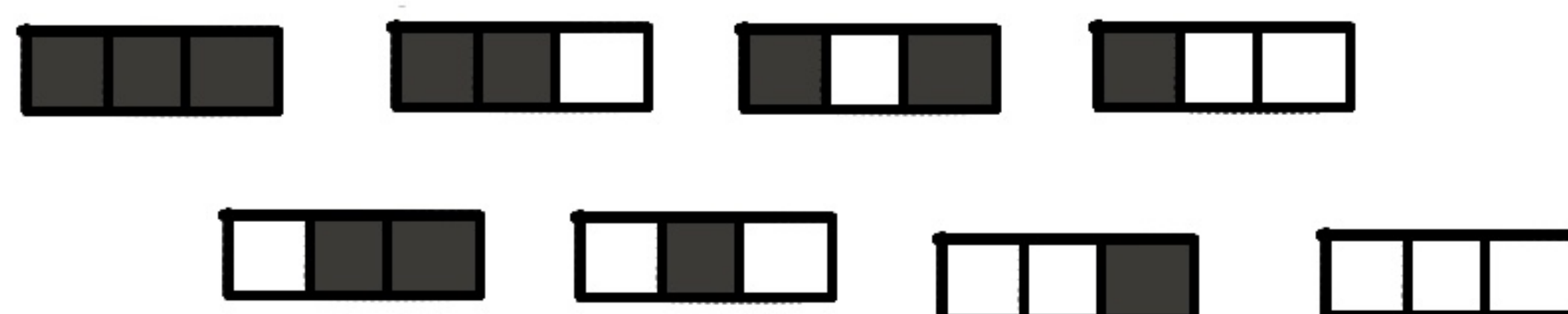
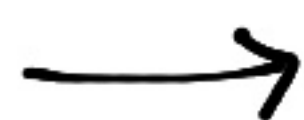
THIS IS THE MOORE NEIGHBOURHOOD
FOR THE BLACK CELL

ONE DIMENSION

ELEMENTARY CELLULAR AUTOMATA ARE ONE DIMENSIONAL.

THE NEXT STATE OF A CELL IS DECIDED BY THE STATE OF THE CELL ITSELF AND ITS TWO IMMEDIATE NEIGHBOURS.

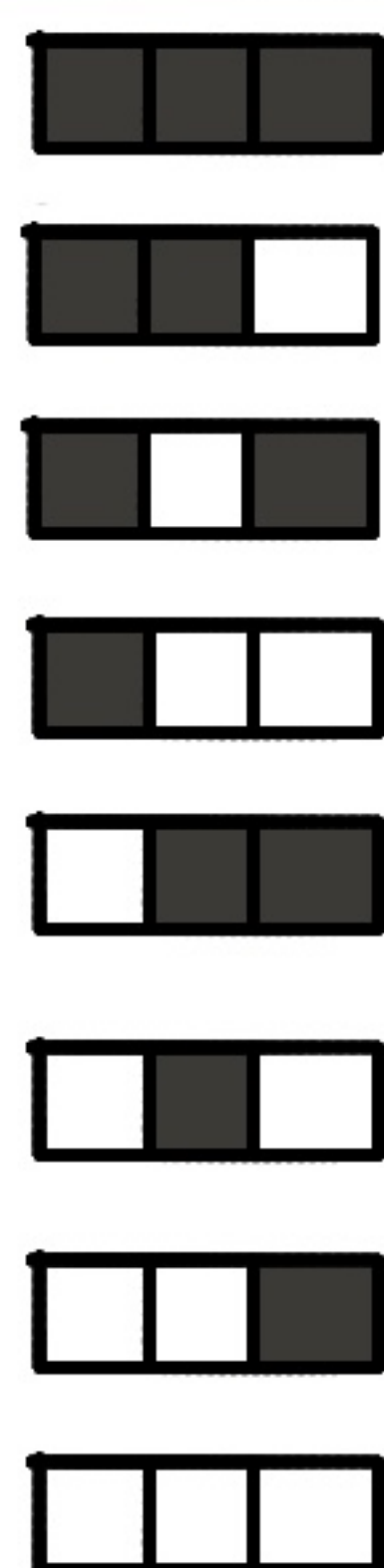
8 POSSIBLE ARRANGEMENTS
FOR 3 CELLS
WITH 2 STATES



HOW TO DEFINE A CELLULAR AUTOMATON

- LIST POSSIBLE NEIGHBOURHOODS FOR EACH CELL
- DEFINE OUTCOME/NEXT STATE OF THE CELL IN THE MIDDLE

NEIGHBOURHOODS



NEXT STATE

<input checked="" type="checkbox"/> ON	<input type="checkbox"/> OFF
<input checked="" type="checkbox"/> ON	<input type="checkbox"/> OFF
<input type="checkbox"/> ON	<input checked="" type="checkbox"/> OFF
<input type="checkbox"/> ON	<input checked="" type="checkbox"/> OFF
<input checked="" type="checkbox"/> ON	<input type="checkbox"/> OFF
<input checked="" type="checkbox"/> ON	<input type="checkbox"/> OFF
<input type="checkbox"/> ON	<input checked="" type="checkbox"/> OFF
<input type="checkbox"/> ON	<input checked="" type="checkbox"/> OFF

Two outcomes per neighbourhood

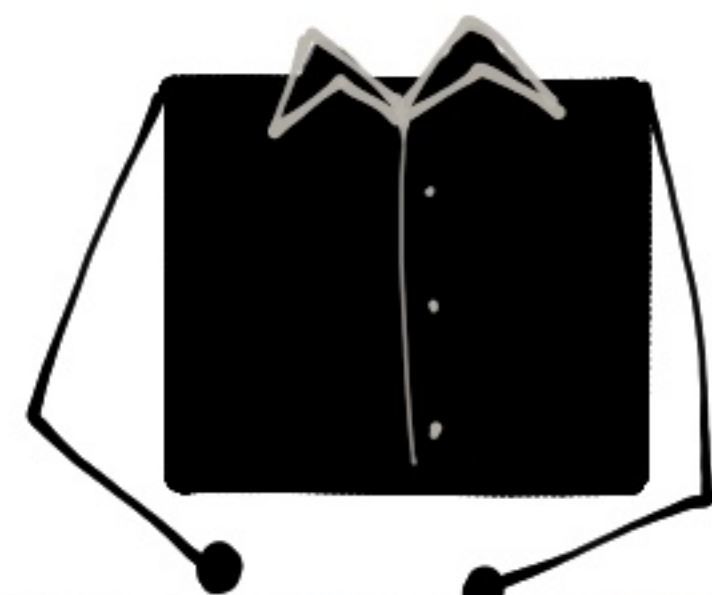
NUMBER OF POSSIBLE
ELEMENTARY
CELLULAR AUTOMATA

$$\begin{aligned} &= 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \\ &= 2^8 \\ &= 256 \end{aligned}$$

WOLFRAM & CA



STEPHEN WOLFRAM, MATHEMATICIAN AND COMPUTER SCIENTIST, STUDIED ELEMENTARY CELLULAR AUTOMATA IN GREAT DETAIL.



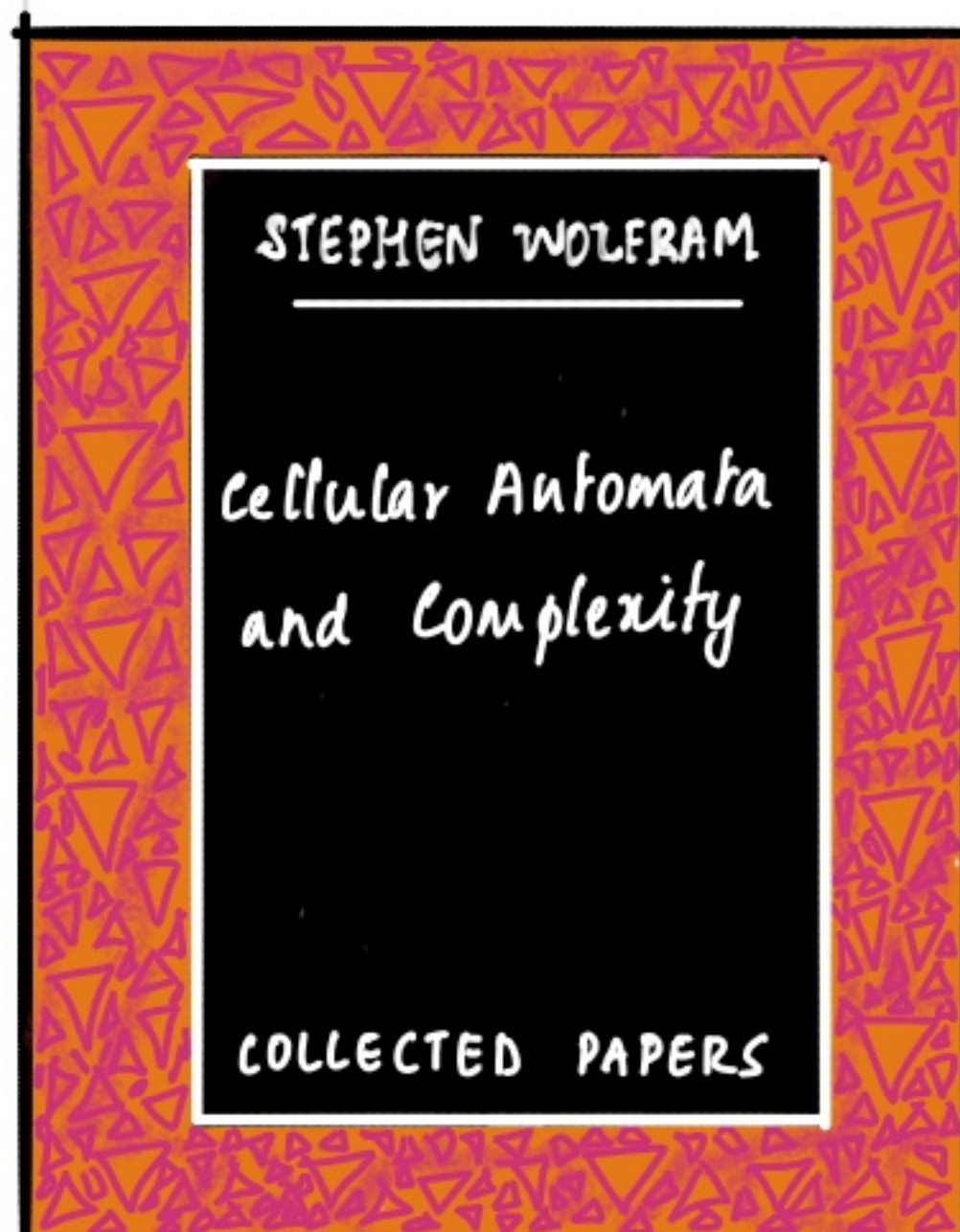
STEPHEN WOLFRAM

HE PROPOSED A NUMBERING SCHEME - WOLFRAM CODE - TO ASSIGN TO EACH OF THE 0-255 RULES.

THE SCHEME IS DEFINED IN THIS ORDER

0	0	0	0	0	1	0	0

THE OUTCOME 00000100 IS CONVERTED FROM DECIMAL TO BINARY.
THIS STRING OF DIGITS IS THE BINARY EQUIVALENT OF NUMBER 4.
THIS IS THE WOLFRAM CODE

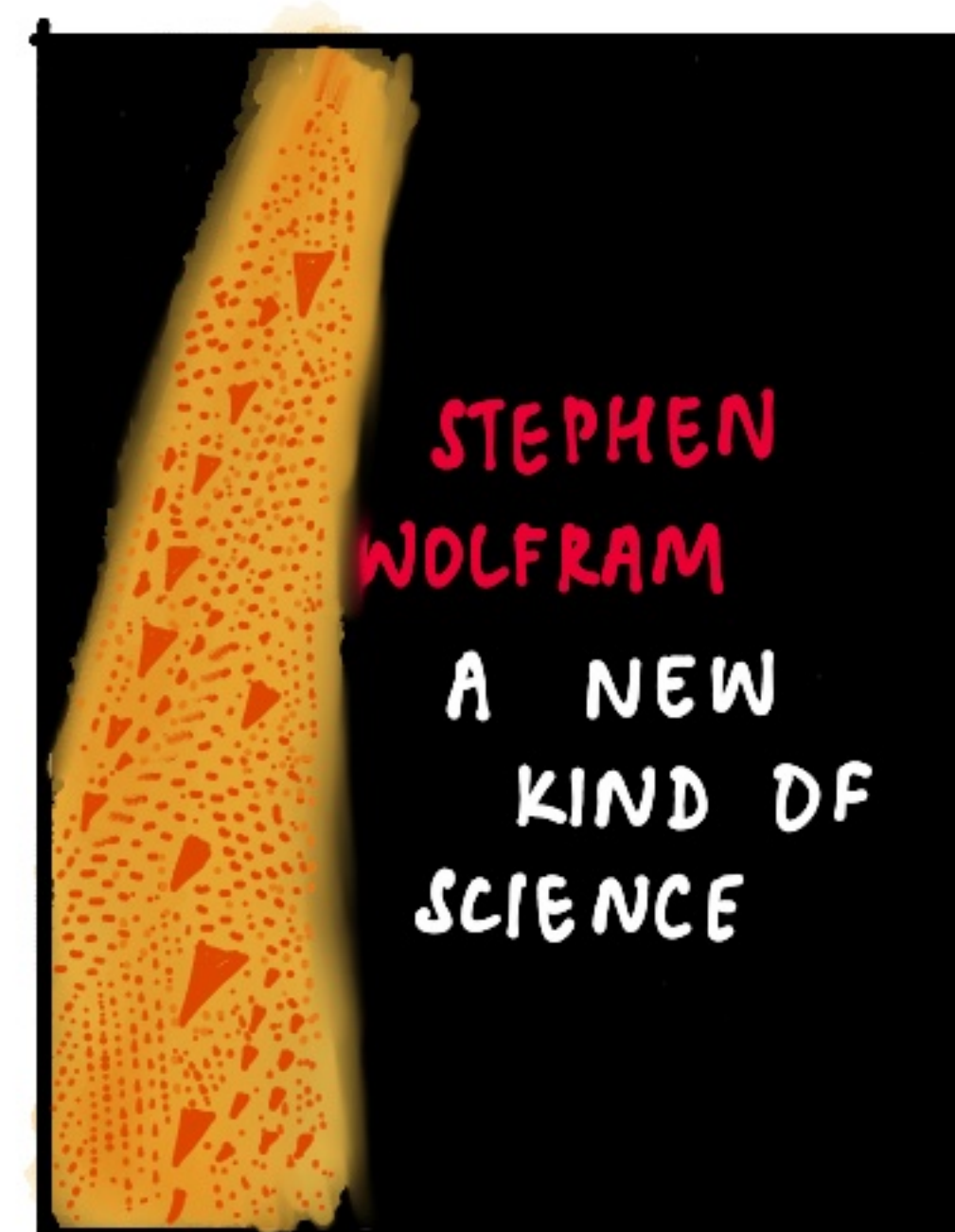


WOLFRAM USED THESE SIMPLE RULES AND STUDIED THE

- FIXED
 - OSCILLATING
 - CHAOTIC
-]

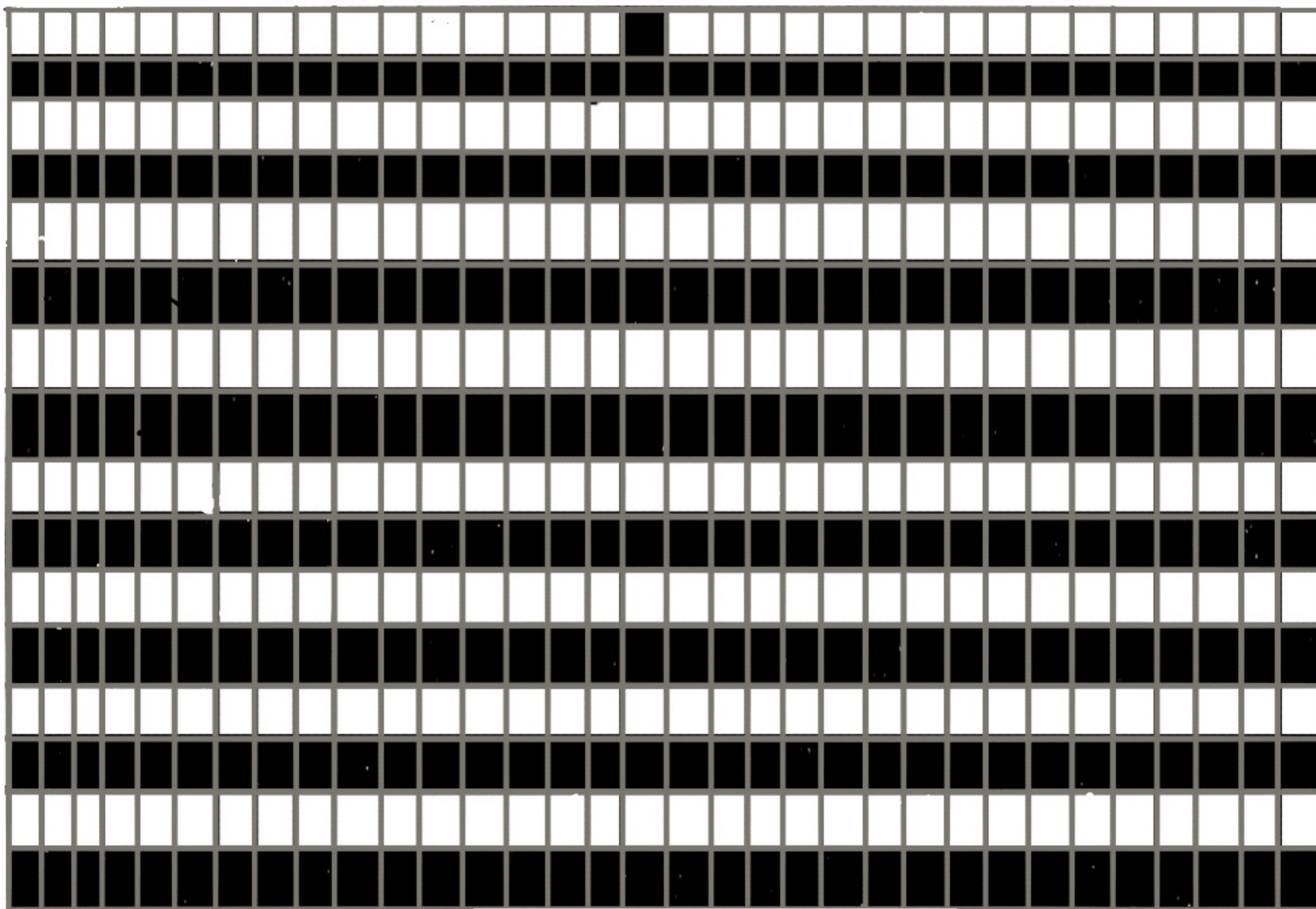
PATTERNS

THAT EVOLVED FROM THEM.



LET US LOOK AT SOME OF THESE PATTERNS AND UNDERSTAND WHAT MAKES THESE STRUCTURES POWERFUL ENOUGH TO MODEL COMPLEX SYSTEMS

EXAMPLE - RULE 31

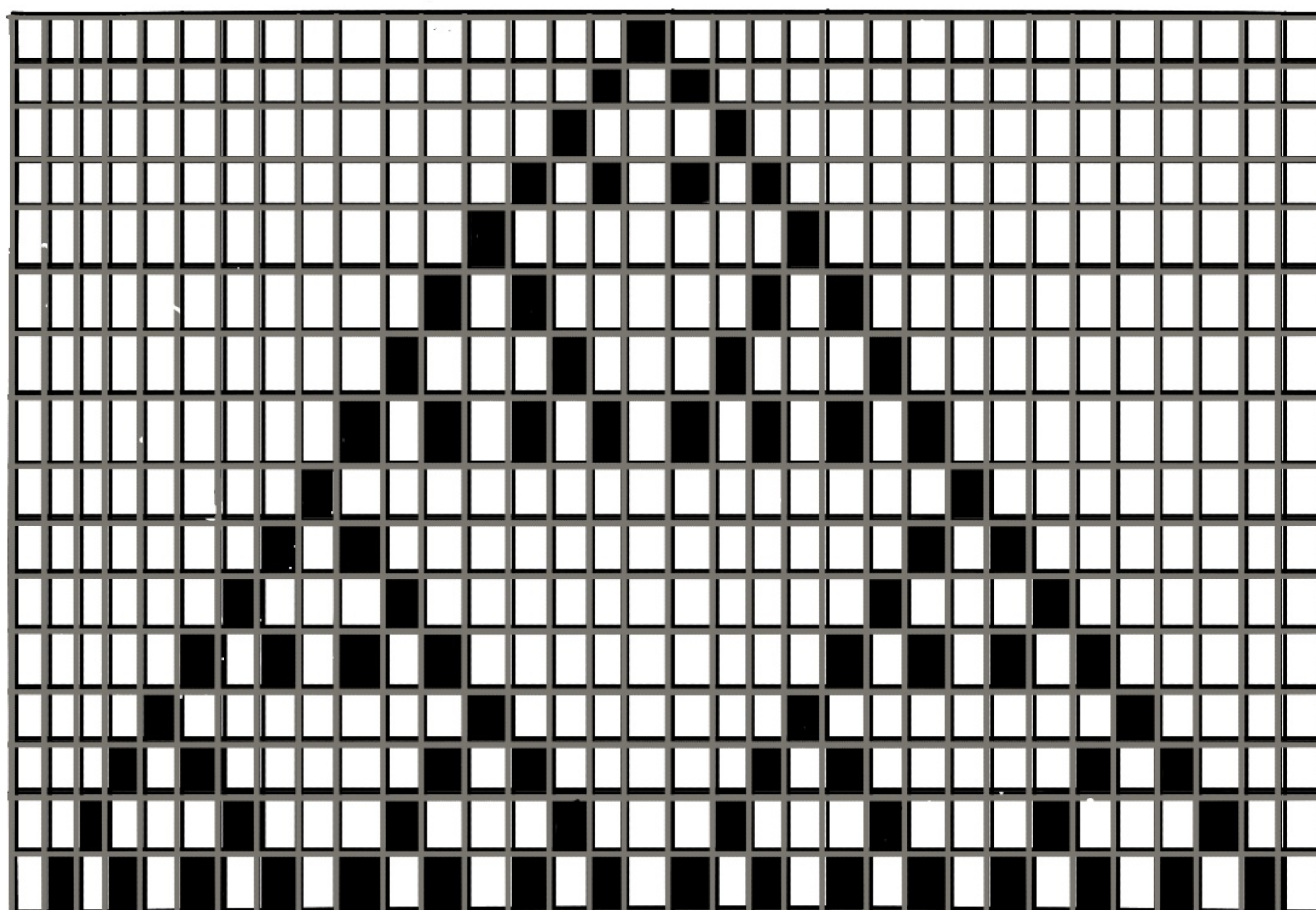


LET US START WITH A SINGLE 'ON' CELL FOR ALL EXAMPLES

- THIS RULE VERY QUICKLY SETTLES INTO A SIMPLE OSCILLATING PATTERN
- SOME RULES PRODUCE A FIXED POINT PATTERN SUCH AS RULE 77

search for '1D Elementary Cellular Automata' an online simulator from [elife-asu.github.io](https://github.com/elife-asu)

EXAMPLE - RULE 90

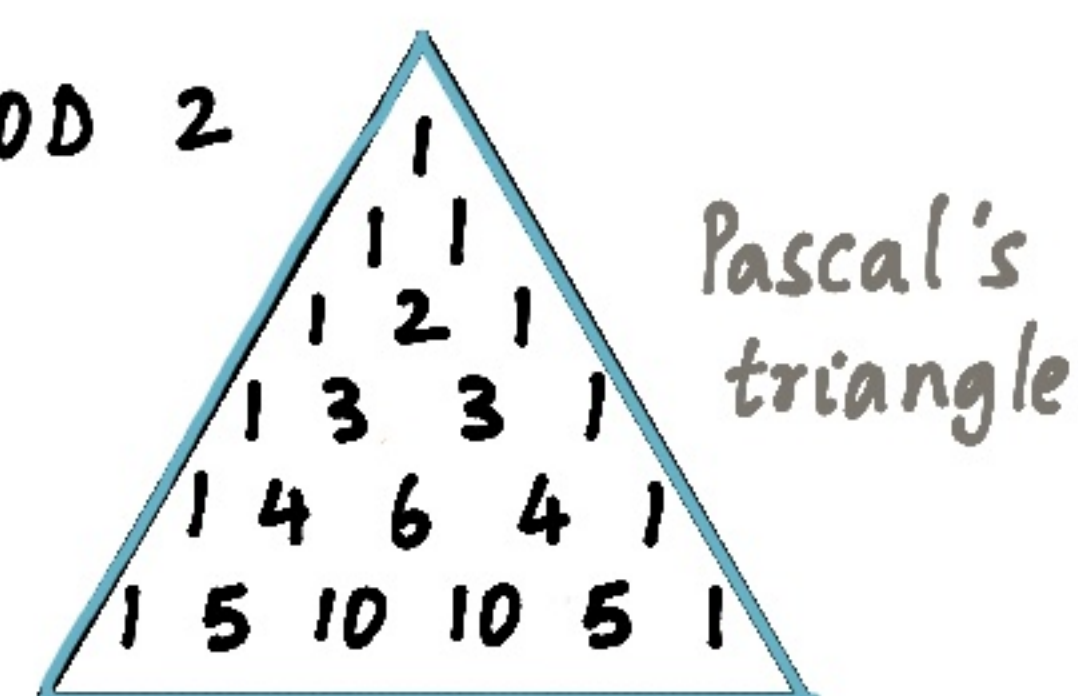


● IT FORMS A SIERPINSKI TRIANGLE FRACTAL PATTERN

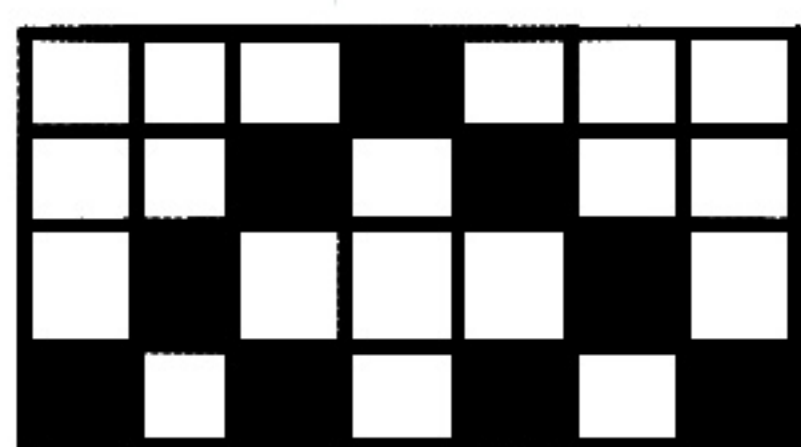
● THIS IS ALSO PASCAL'S TRIANGLE MOD 2

0 FOR EVEN NUMBERS

1 FOR ODD NUMBERS



● THE NEXT VALUE OF A CELL IS THE XOR OF ITS NEIGHBOURS



XOR = \oplus
EXCLUSIVE OR

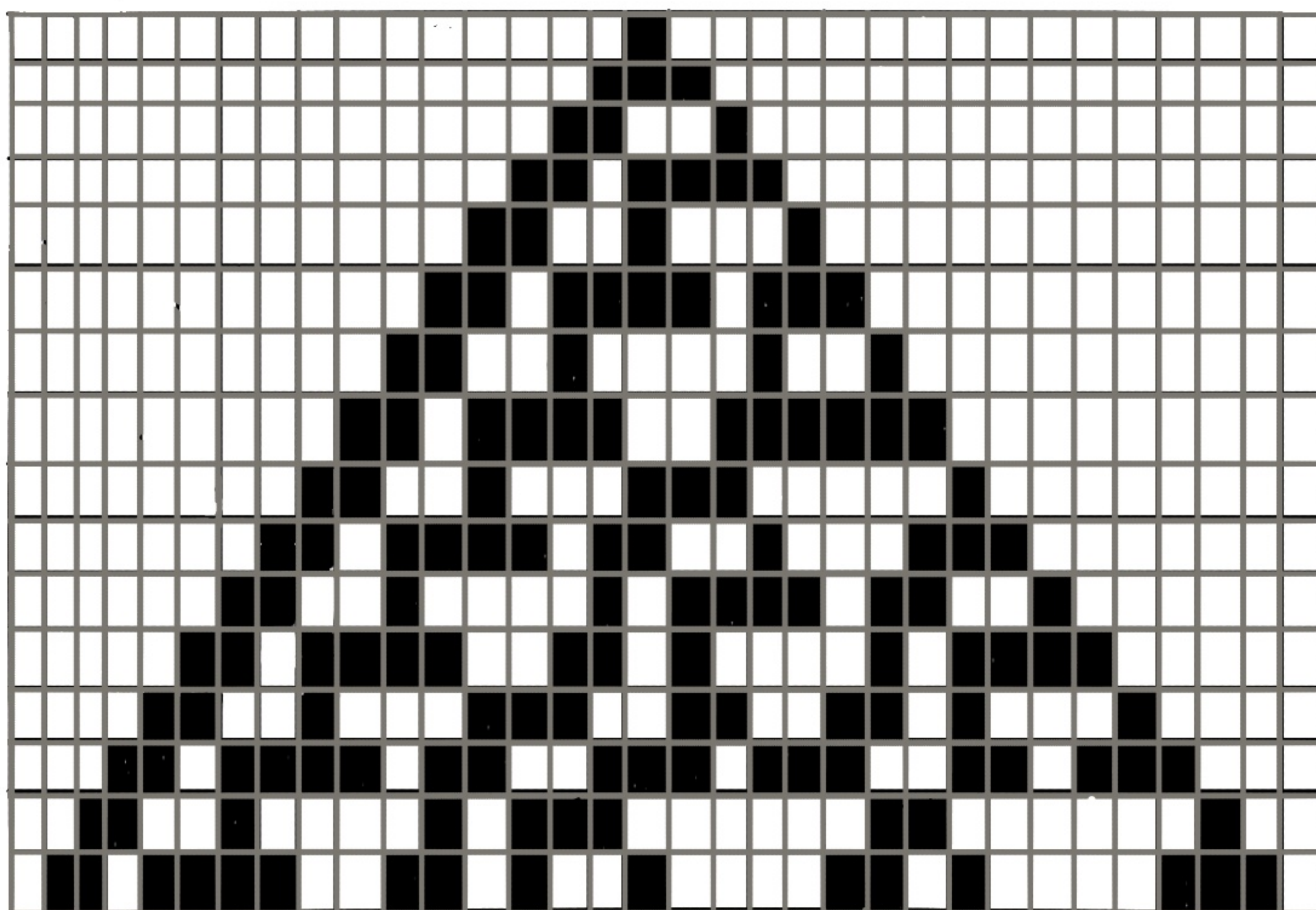
X	Y	$X \oplus Y$
1	1	0
0	0	0
1	0	1
0	1	1

XOR
Truth
table

0	0	0	1	0	0	0
0	0	1	0	1	0	0
0	1	0	0	0	1	0
1	0	1	0	1	0	1

NEXT VALUE OF 0 = $1 \oplus 0 = 1$
 NEXT VALUE OF 1 = $0 \oplus 0 = 0$
 NEXT VALUE OF 0 = $0 \oplus 1 = 1$

EXAMPLE - RULE 30



- DISPLAYS NON-REPEATING CHAOTIC BEHAVIOUR
- USED AS A (PSEUDO) RANDOM NUMBER GENERATOR
- PROPOSED USE IN PUBLIC KEY CRYPTOGRAPHY

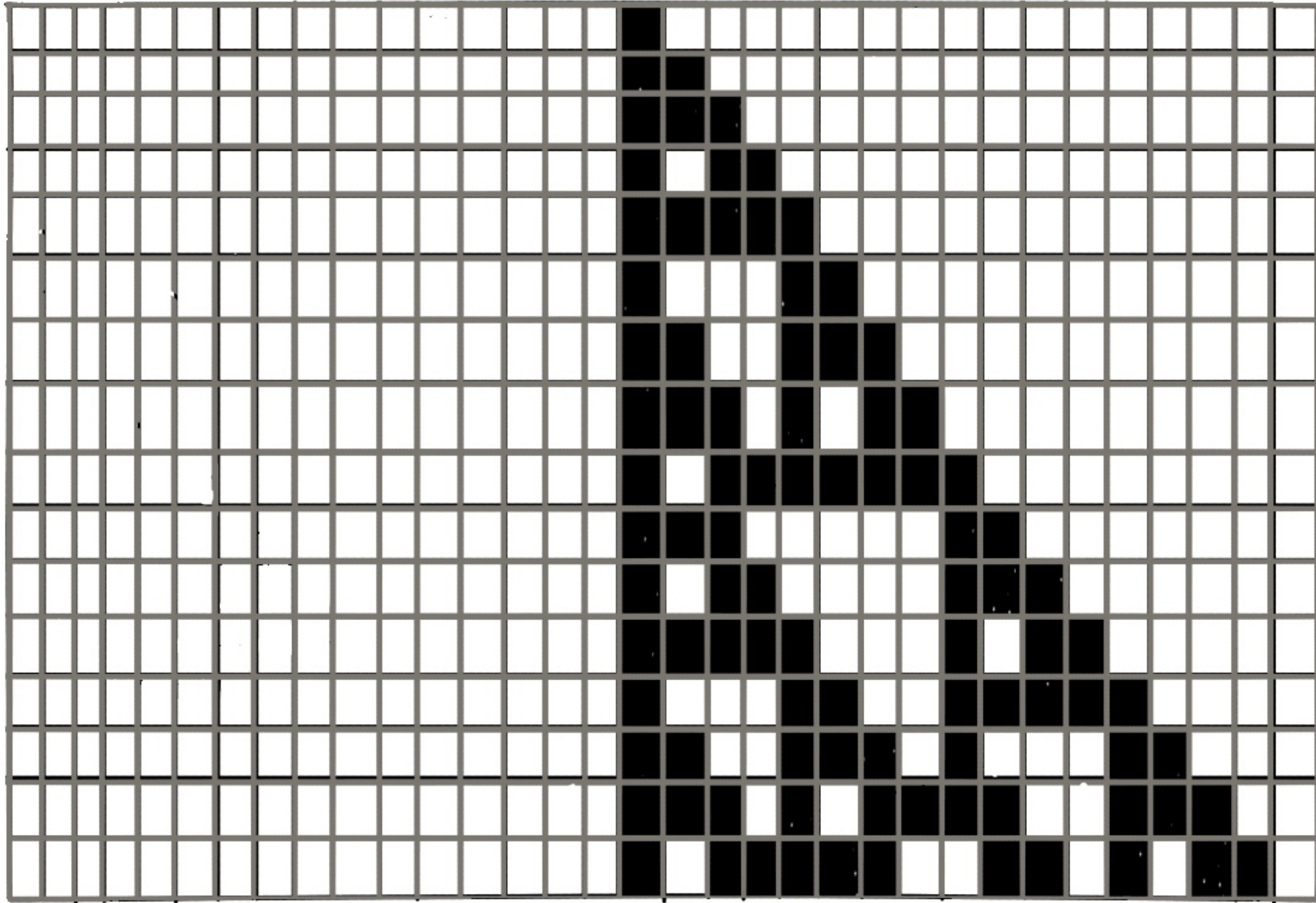
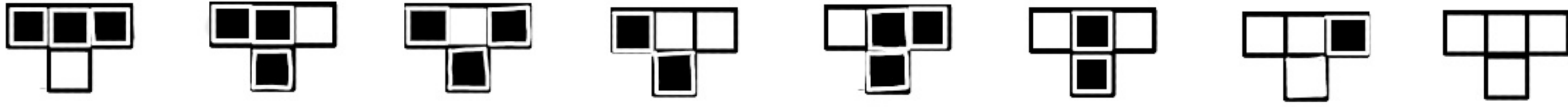
GIVEN THE RULES:

EASY TO WORK OUT THE NEXT STEP

HARD TO WORK OUT THE PREVIOUS STEP

- DISPLAYS SENSITIVE DEPENDENCE TO INITIAL CONFIG
- "CENTRAL TO HOW COMPLEXITY GETS MADE IN NATURE"
(REF TO SIMPLE RULES GIVING COMPLEX BEHAVIOUR)
- STEPHEN WOLFRAM WRITINGS.

EXAMPLE - RULE 124

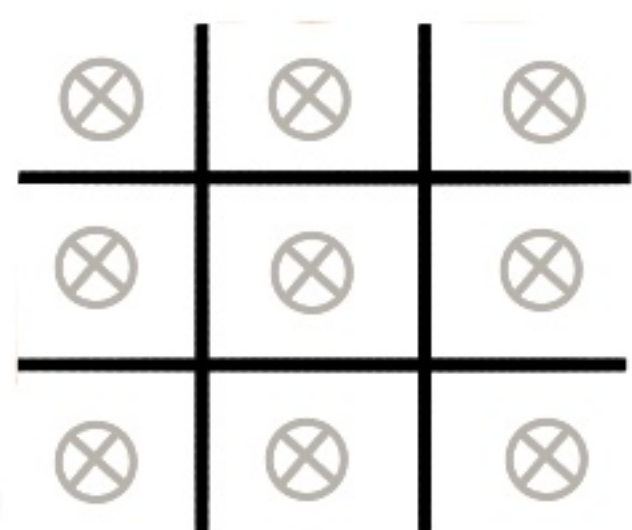


- IS THE MIRROR IMAGE OF THE MORE FAMOUS* RULE 110
- IS PROVED TO BE TURING COMPLETE (ALSO RULE 110)
SEARCH ONLINE FOR A DEMO OF
RULE 110 MARBLE COMPUTER
- DISPLAYS STRANDS OF LONG-LIVED COMPLEX STRUCTURES.

* Rule 124 was more of a personal choice

TWO DIMENSIONS

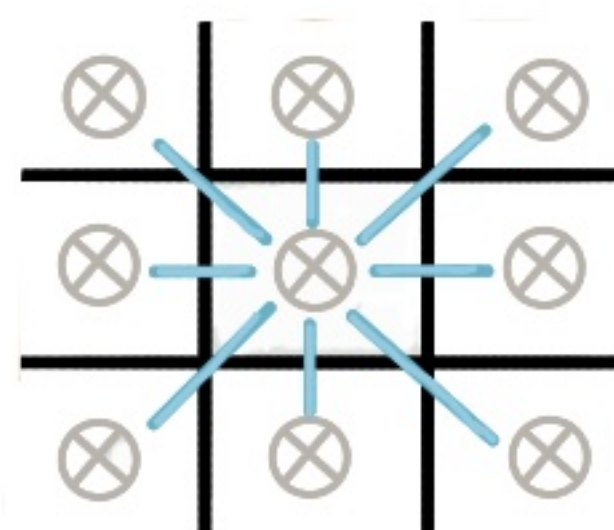
CELLULAR AUTOMATA IN TWO DIMENSIONS NEED



AN INITIAL STATE



RULES



A DEFINED NEIGHBOURHOOD

HERE ARE SOME TWO DIMENSIONAL CELLULAR AUTOMATA

BRIAN'S BRAIN

RAKE

IMMIGRATION

SEEDS

SEDIMENTAL

GAME OF LIFE

STAR WARS

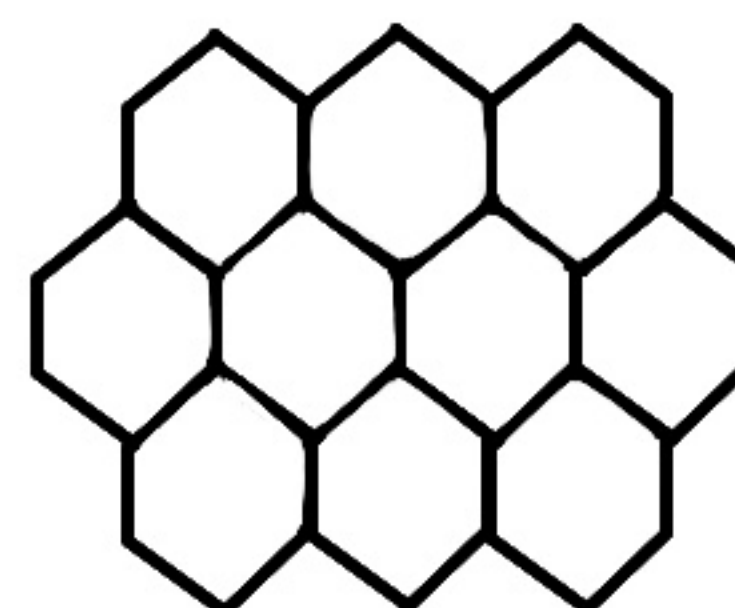
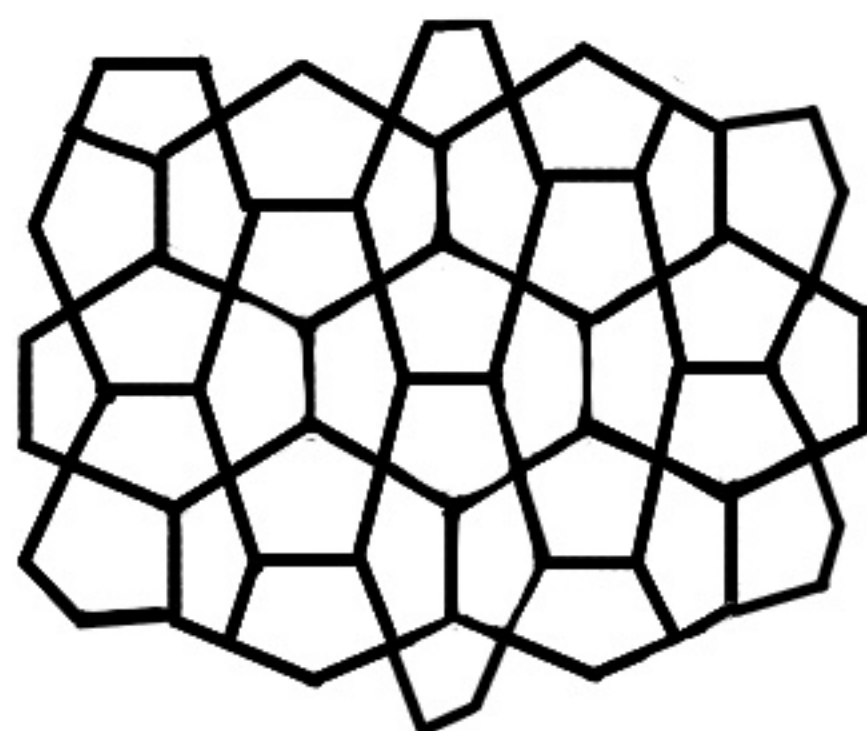
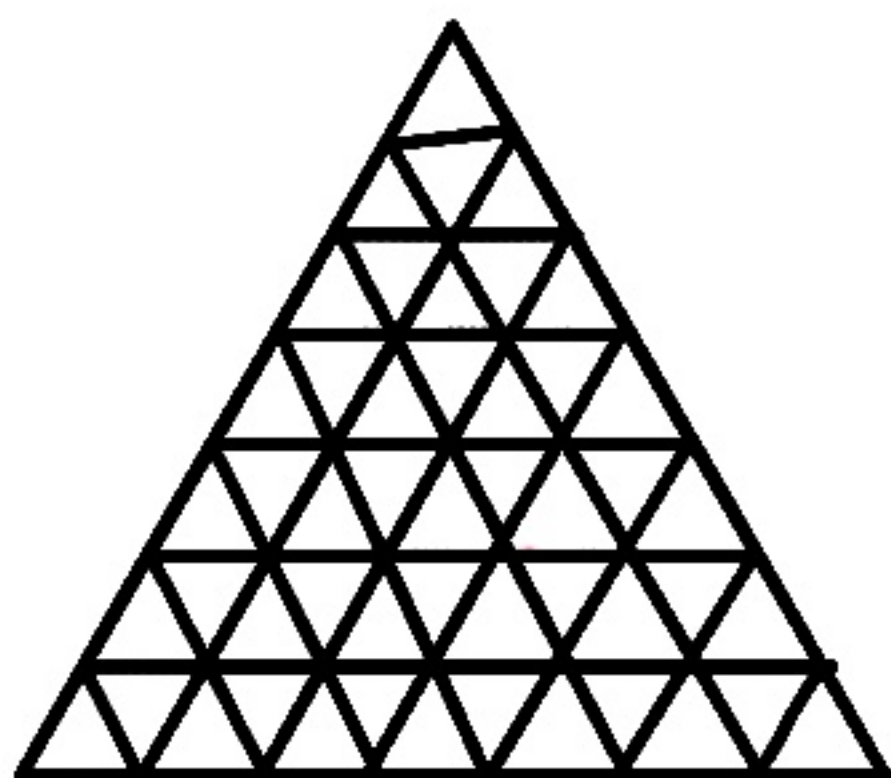
BOMBERS

HIGH LIFE

WIREWORLD

INTERESTINGLY, THE GRIDS COULD BE NON-SQUARES. THEY COULD BE TRIANGLES, PENTAGONS OR HEXAGONS. (EVEN ON PENROSE TILES!)

WORK BY PROF SUSAN STEPNEY)



THE WHOLE GRID IS UPDATED AT ONCE FOR EACH TIME STEP.

THE GAME OF LIFE

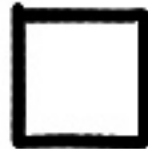


JOHN CONWAY

THE MOST WELL KNOWN OF CELLULAR AUTOMATA HAS TO BE THE GAME OF LIFE DESIGNED BY JOHN CONWAY IN 1970.

IN THE GRID, CELLS ARE IN ONE OF

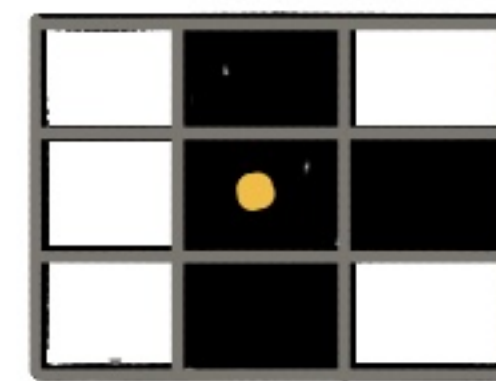
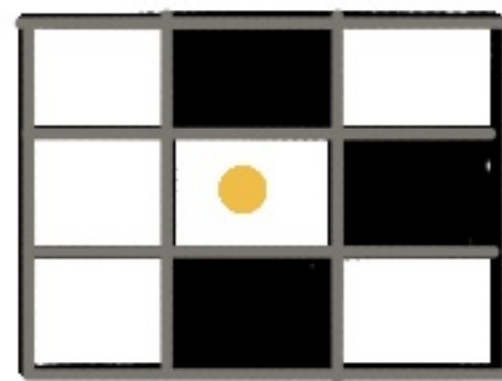
ALIVE  STATE

DEAD  STATE

GAME OF LIFE : RULES

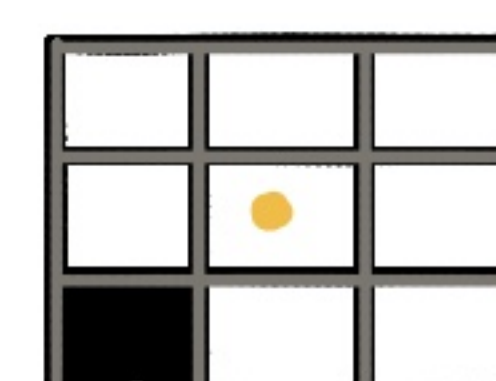
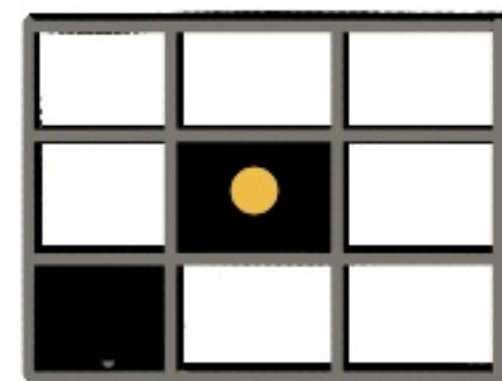
BIRTH

● A DEAD CELL WITH 3 LIVE NEIGHBOURS COMES ALIVE

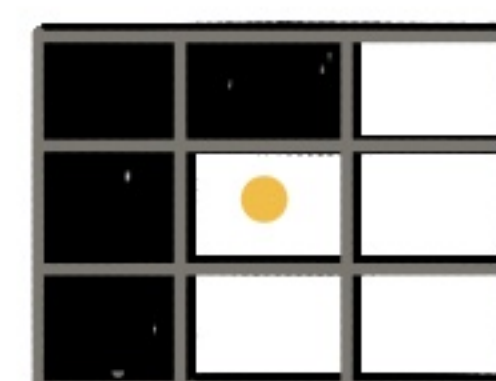
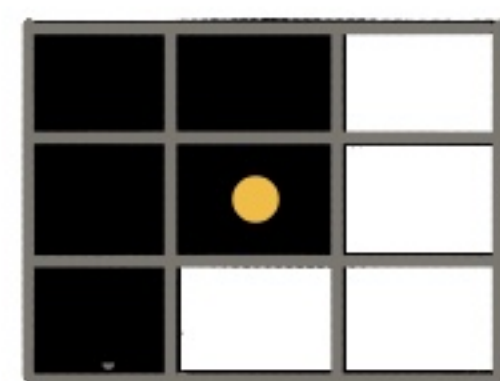


DEATH

● A LIVE CELL WITH 1 OR 0 LIVE NEIGHBOURS DIES

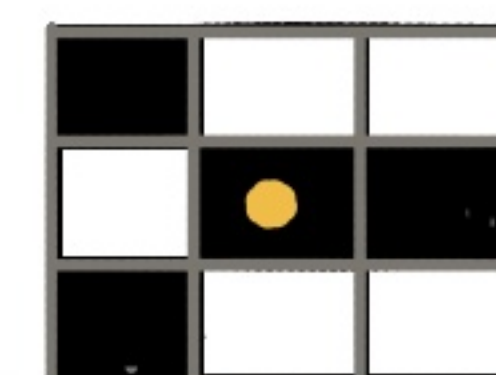
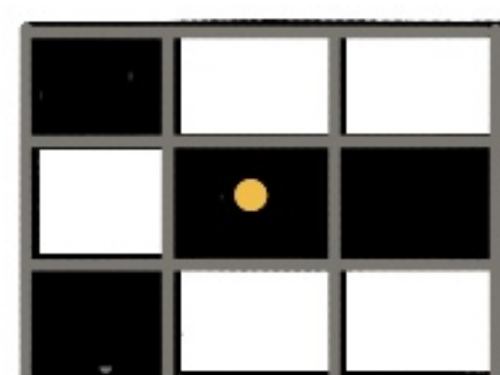


● A LIVE CELL WITH 4 OR MORE LIVE NEIGHBOURS DIES



SURVIVAL

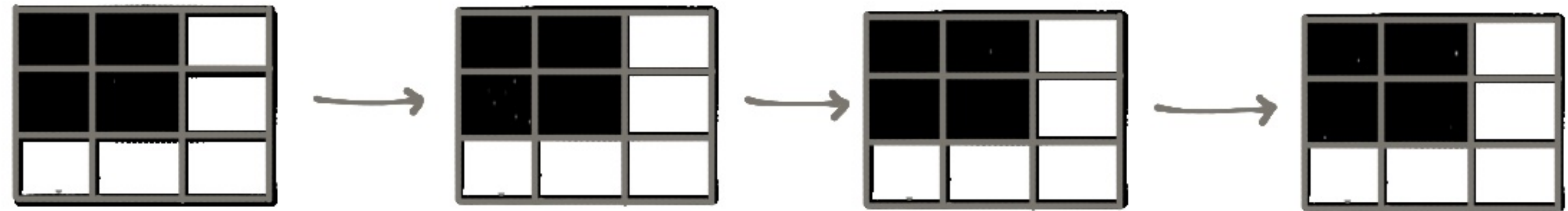
● A LIVE CELL WITH 2 OR 3 LIVE NEIGHBOURS STAYS ALIVE



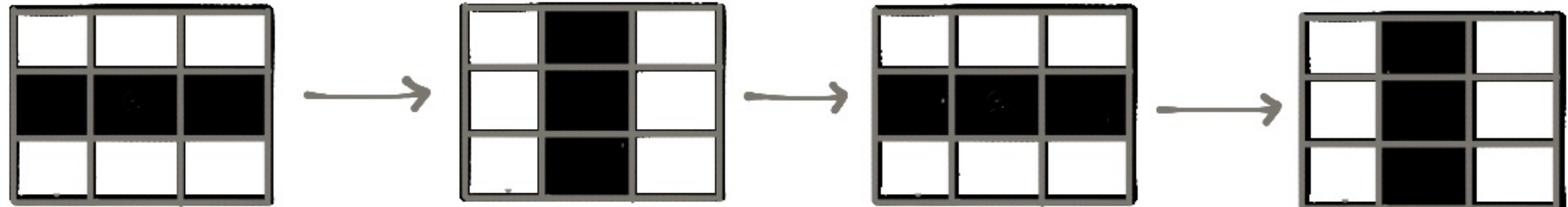
THE COMPLEXITY

THE GAME OF LIFE IS A VERY WELL THOUGHT OUT SET OF RULES THAT CAN EVOLVE MANY TYPES OF PATTERNS-

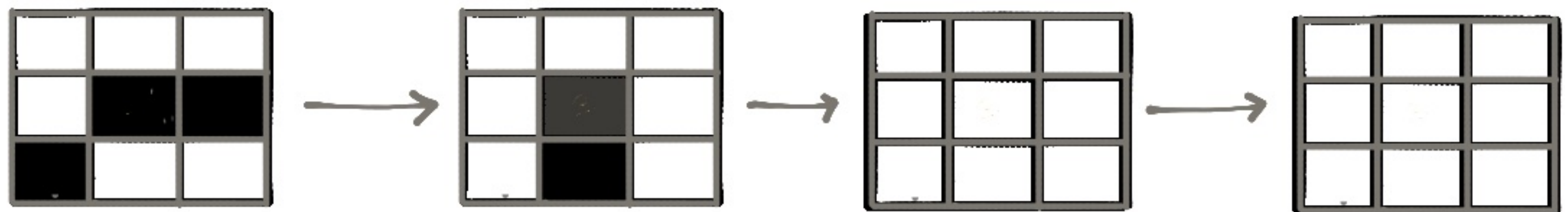
STILL



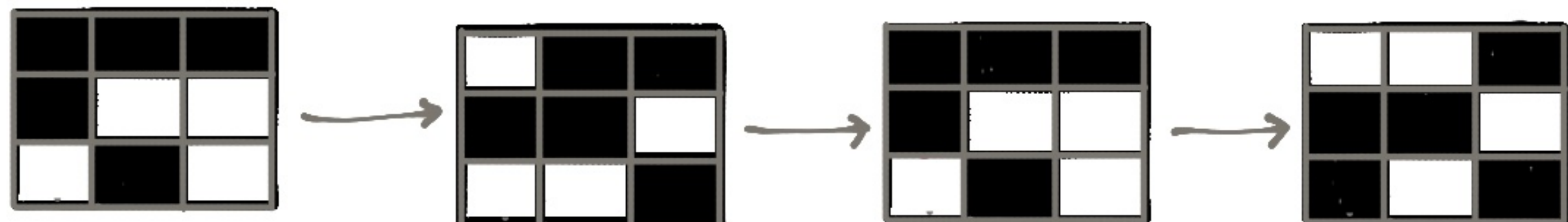
OSCILLATING



DYING



MOVING



THIS SHAPE GLIDED ACROSS THE GRID PROMPTING A SEARCH FOR MORE SUCH 'CREATURES'.

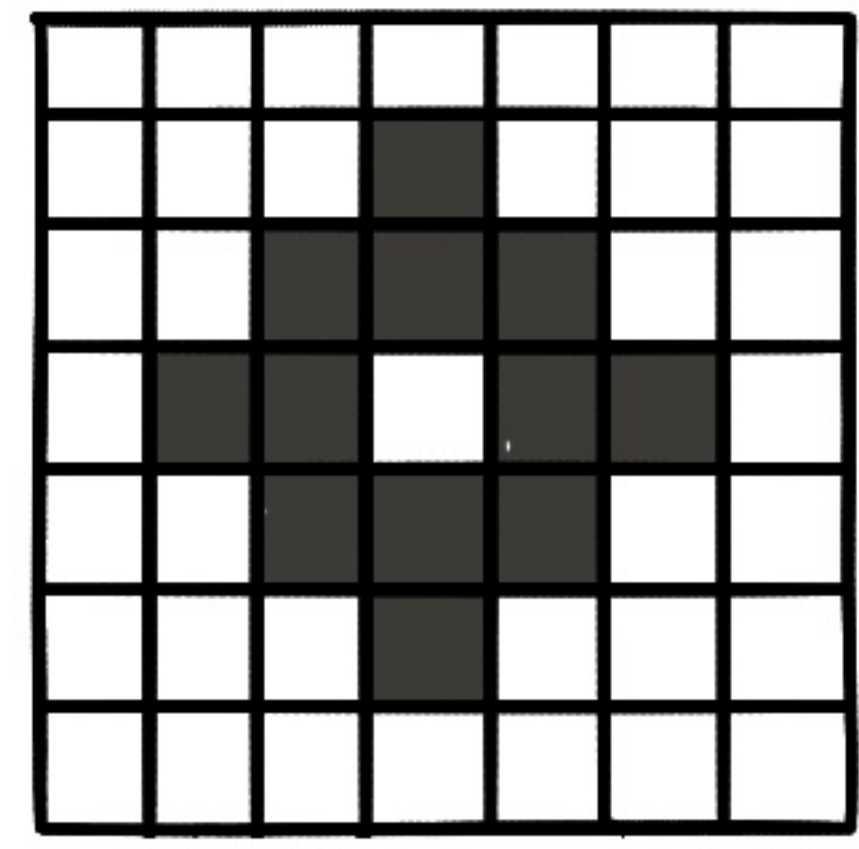
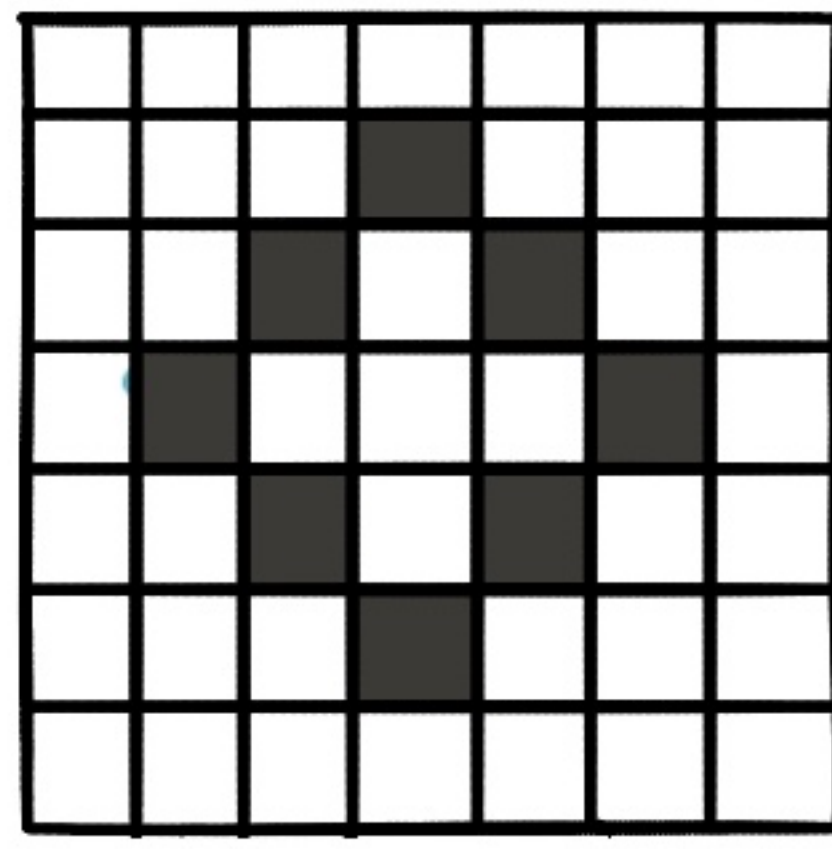
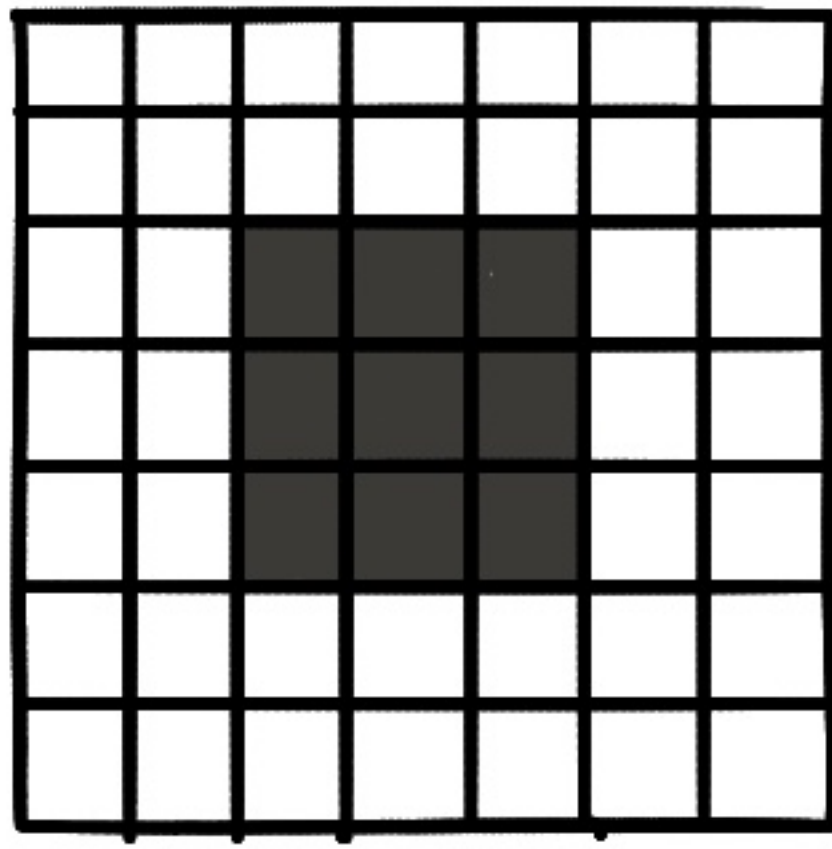
MORE COMPLEX SHAPES AND UNPREDICTABLE PATTERNS INTERACT AND UNFOLD, ALL DEPENDING ON THE INITIAL STATES OF THE CELLS.

THE EMERGENCE AND SELF ORGANISATION THAT CONWAY INTENDED TO DEMONSTRATE - THE UNPREDICTABILITY - IS NOT RANDOM BECAUSE LIFE OBEYS CERTAIN RULES.

UNSURPRISINGLY, LIFE HAS ITS OWN LEXICON AND COMMITTED GROUPS OF ENTHUSIASTS.

check out playgameoflife.com

THE LEGACY



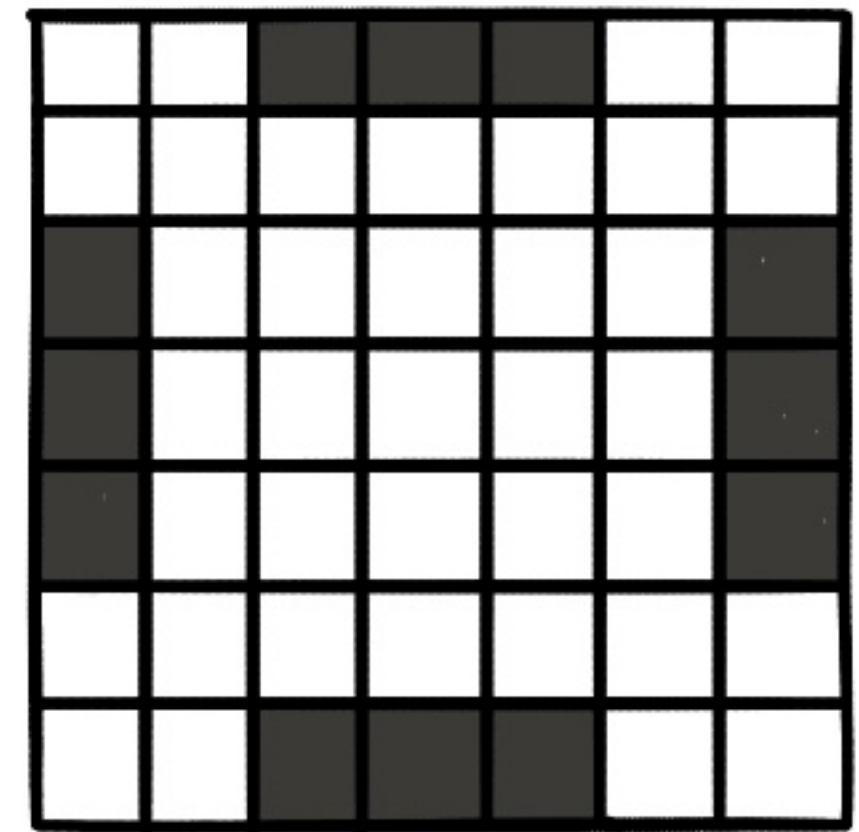
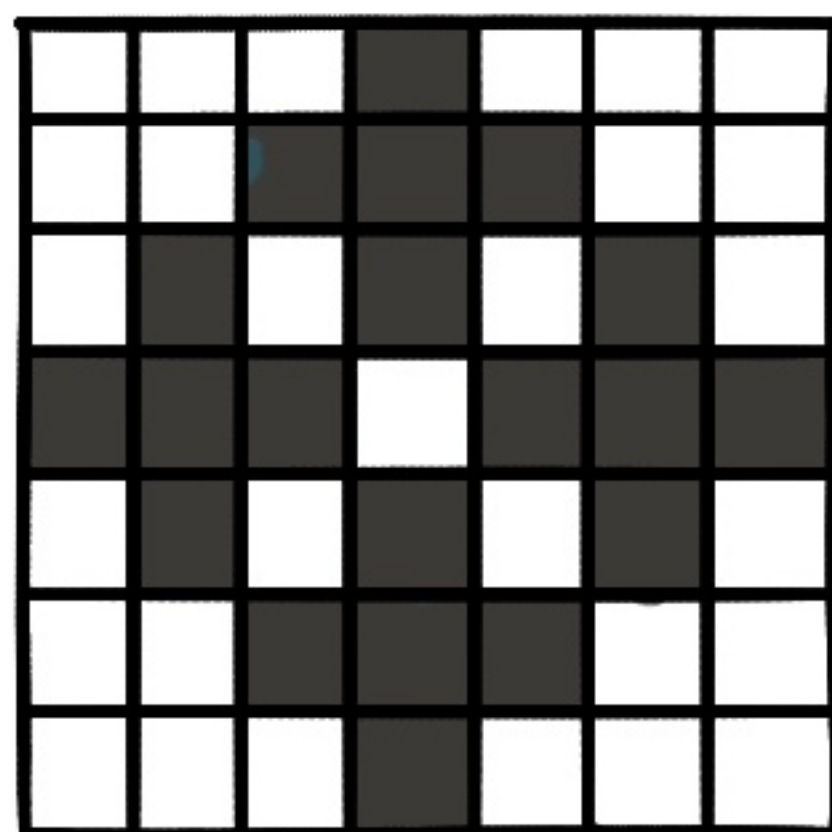
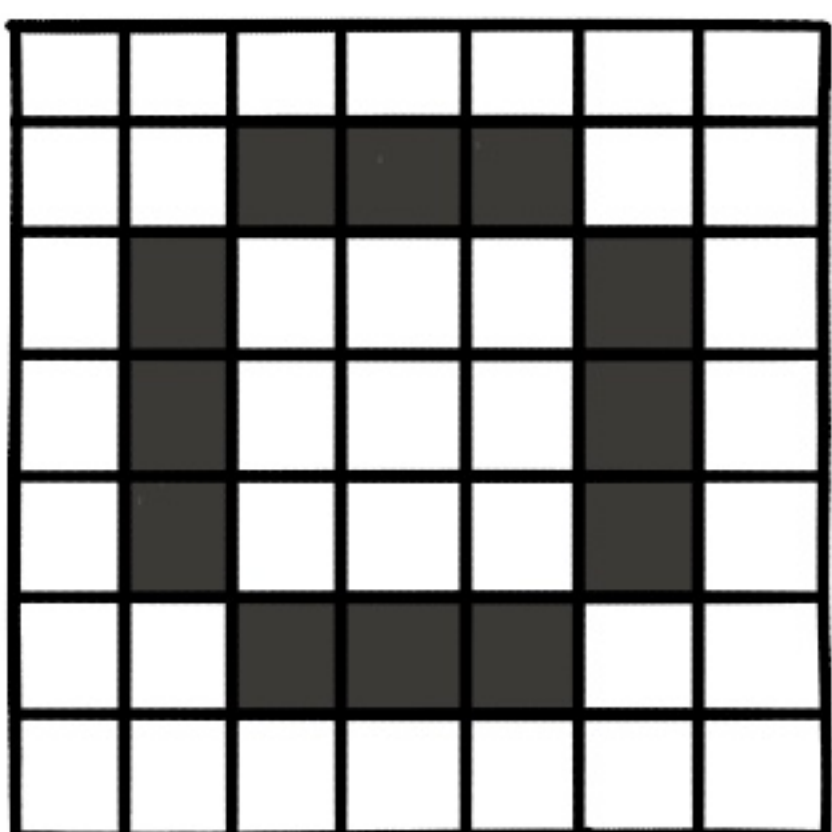
GAME OF LIFE CONTINUES TO BE POPULAR SINCE IT WAS FIRST PUBLISHED IN MARTIN GARDNER'S COLUMN IN SCIENTIFIC AMERICAN ABOUT 50 YEARS AGO.

THERE ARE PATTERNS ON THE GRID THAT CAN EMULATE COUNTERS AND LOGIC GATES IN PROGRAMMING.

THE GAME OF LIFE IS PROVED AS TURING COMPLETE & UNDECIDABLE

LIFE IS A VERY EASY TO UNDERSTAND EXAMPLE OF EMERGENT COMPLEXITY

LIFE HELPS US UNDERSTAND HOW PATTERNS IN NATURE CAN DEVELOP AND THAT IT IS POSSIBLE THAT COMPLEX FORMS CAN ARISE FROM THE SIMPLE WITHOUT BEING EXPLICITLY PROGRAMMED TO DO SO.



CA ARE IDEAL FOR:

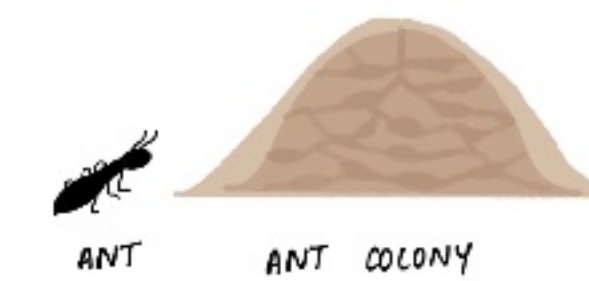
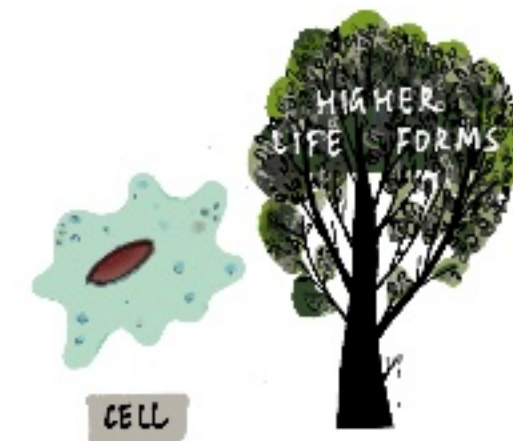
AS WE HAVE SEEN EARLIER, LIKE ANY OTHER COMPLEX SYSTEM, CELLULAR AUTOMATA ARE ALSO

✓ SIMPLE INTERACTING COMPONENTS

✓ CAPABLE OF PROCESSING INFORMATION

✓ WITH NO CENTRAL CONTROL &

✓ DISPLAY COMPLEX BEHAVIOUR FROM SIMPLE RULES



COMPLEX SYSTEMS HAVE SOME COMMON FEATURES. THEY HAVE:

SIMPLE COMPONENTS

- SIMPLER THAN THE WHOLE

INTERACTIONS

- THE PARTS ARE INTERDEPENDENT AND INTERACT WITH EACH OTHER BASED ON SIMPLE RULES

NO CENTRALISED CONTROL

- THEY ARE SELF ORGANISING

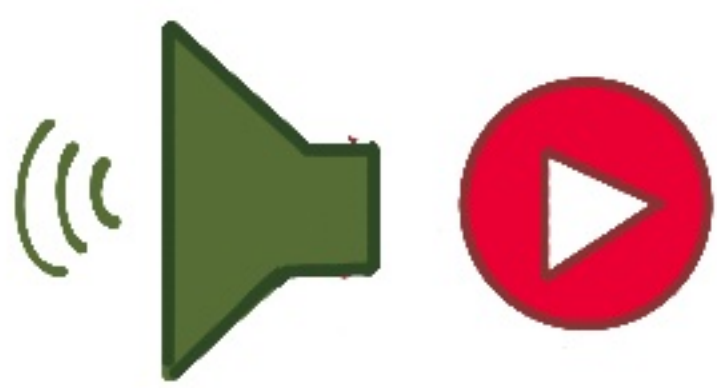
EMERGENT BEHAVIOUR

- THE COLLECTIVE BEHAVIOURS ADAPT AND EVOLVE AND ARE EVEN CHAOTIC AS THE SYSTEM LEARNS FROM ITS ENVIRONMENT

MAKING THE WHOLE GREATER THAN THE PARTS

CELLULAR AUTOMATA CAN BE USED TO:

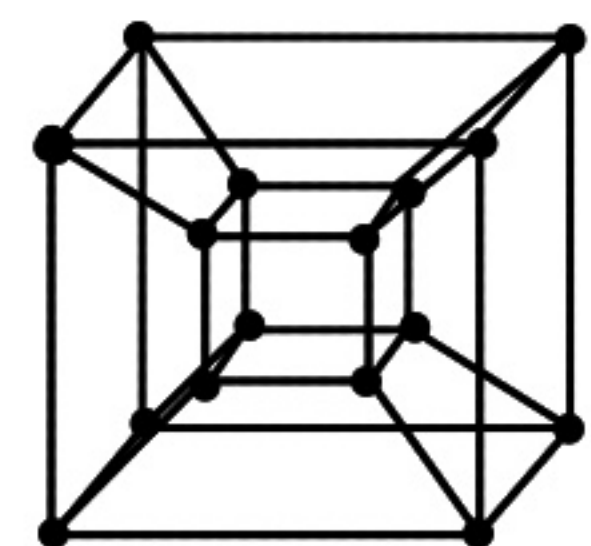
CREATE AUDIO/
VISUAL CONTENT



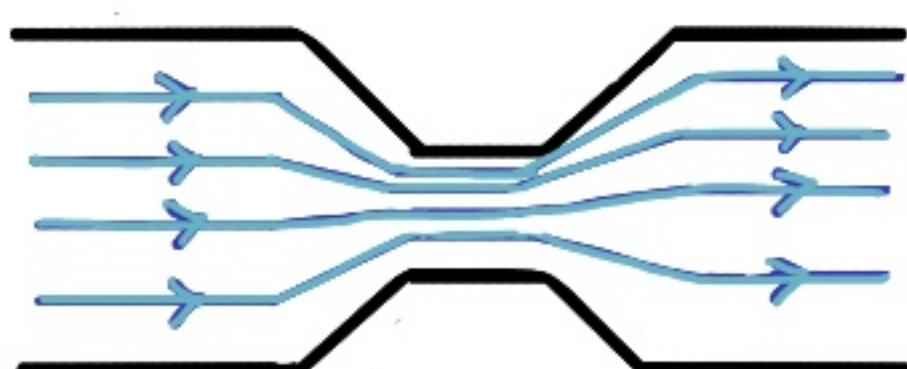
GENERATE PSEUDO
RANDOM NUMBERS

9	5	4	3	6	8	9	0
1	6	3	2	1	9	7	9
2	1	7	9	6	0	2	8
8	7	3	5	4	4	4	7
4	8	0	5	2	5	6	6
2	4	1	0	1	0	4	2

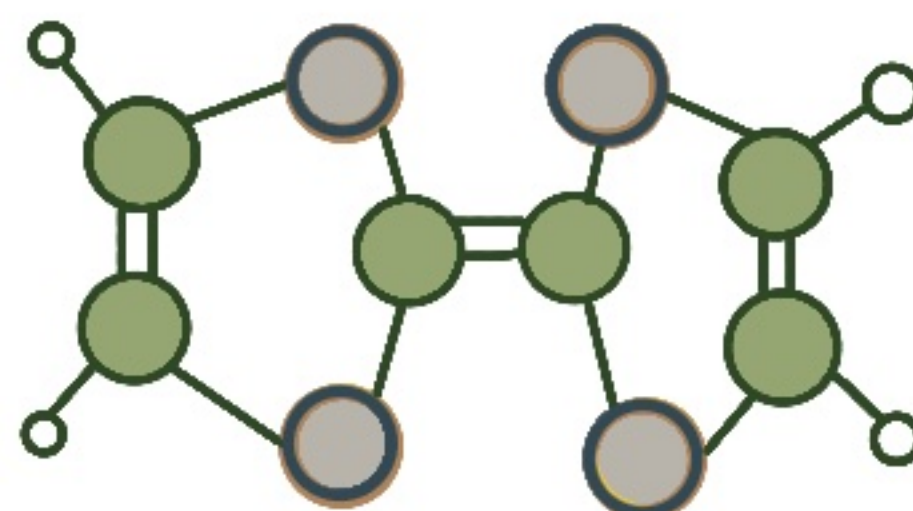
BUILD
PARALLEL COMPUTERS



MODEL
PHYSICAL SYSTEMS



BUILD
MOLECULAR COMPUTERS



SIMULATE
BIOLOGICAL PROCESSES



A BRIEF OUTLOOK

COMPLEXITY IS A VERY YOUNG SCIENCE STILL TRYING TO ESTABLISH ITS ROOTS.

ON ONE HAND, THERE IS RESEARCH AND COMPUTING RESOURCES BEING INVESTED IN COMPLEXITY SCIENCES. IT HAS GENERATED MUCH INTEREST THROUGH IDEAS IN ARTIFICIAL INTELLIGENCE, CELLULAR AUTOMATA, ARTIFICIAL LIFE ETC.

ON THE OTHER, THERE IS SKEPTICISM AND DOUBT ABOUT THE GOALS AND THE BASIC BUILDING BLOCKS FOR THIS SCIENCE.

COMPLEXITY HAS APPLICATIONS SUCH AS DESIGNING EVACUATION ROUTES AND MODELLING TRAFFIC PATTERNS.

IT IS FULL OF POSSIBILITIES — DEVELOPING A COMMON VOCABULARY TO ACCURATELY DEFINE THE PHENOMENA, A NEW TYPE OF MATHEMATICS TO DEPICT THE INTERACTIONS, AND IMPORTANTLY, THE CYCLE OF HYPOTHESIS AND TESTING.

WILL COMPLEXITY HELP US GAIN SIGNIFICANT INSIGHT INTO OUR WORLD? WILL A DIFFERENT NEWTON COME ALONG AND INVENT A HYPERCALCULUS TO BUILD A UNIFIED THEORY?

ONLY TIME WILL TELL.

MORE TO EXPLORE

THIS IS BY NO MEANS AN EXHAUSTIVE LIST. COMPLEXITY SCIENCE HAS AFFECTS MANY FIELDS. IT IS GROWING AND IT EMBRACES NUMEROUS CONCEPTS.

HERE ARE A HANDFUL

- GAME THEORY, PRISONER'S DILEMMA
- MANDELBROT SETS (FRACTALS)
- NORBERT WIENER'S CYBERNETICS
- ALAN TURING'S MORPHOGENESIS
- NOAM CHOMSKY'S UNIVERSAL GRAMMAR
- ANALOGIES AND LEARNING - M. MITCHELL'S COPYCAT PROGRAM

MY REFERENCES

Online Courses

Introduction to Complexity complexityexplorer.org

Analysing Complexity - coursera.org

Books

Chaos: Making a new science - James Gleick

Complexity: A guided tour - Melanie Mitchell

Complexity a very short introduction - John H Holland

Complex Systems latest - quantamagazine.org/tag/complex-systems

Papers/Articles

Simplicity and complexity in the description of nature: Murray Gell-Man - iscte-iul.pt

What is Complexity? - Murray Gell-Man - complexity.martinsewell.com

Measures of Complexity - Seth Lloyd - mit.edu

Science and Complexity - Warren Weaver -

A Brief History of Systems Science, Chaos and Complexity - resilience.org

Chaos - plato.stanford.edu

What are complex systems - cssociety.org

What is complexity science - complexityexplained.github.io

Chaos

Double Pendulum demo - myphysicslab.com

Video: Butterflies, Chaos and Fractals - Professor Raymond Flood

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